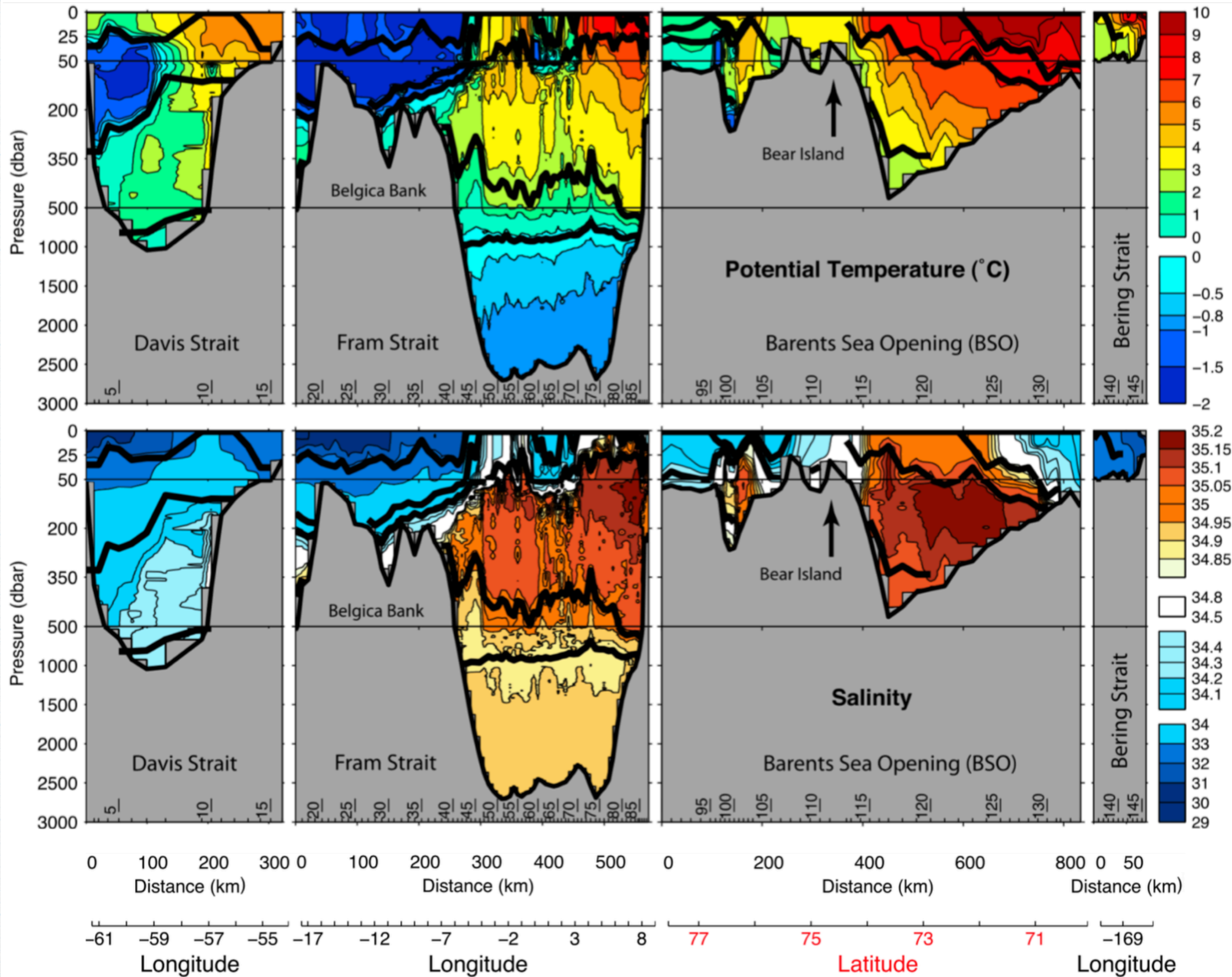


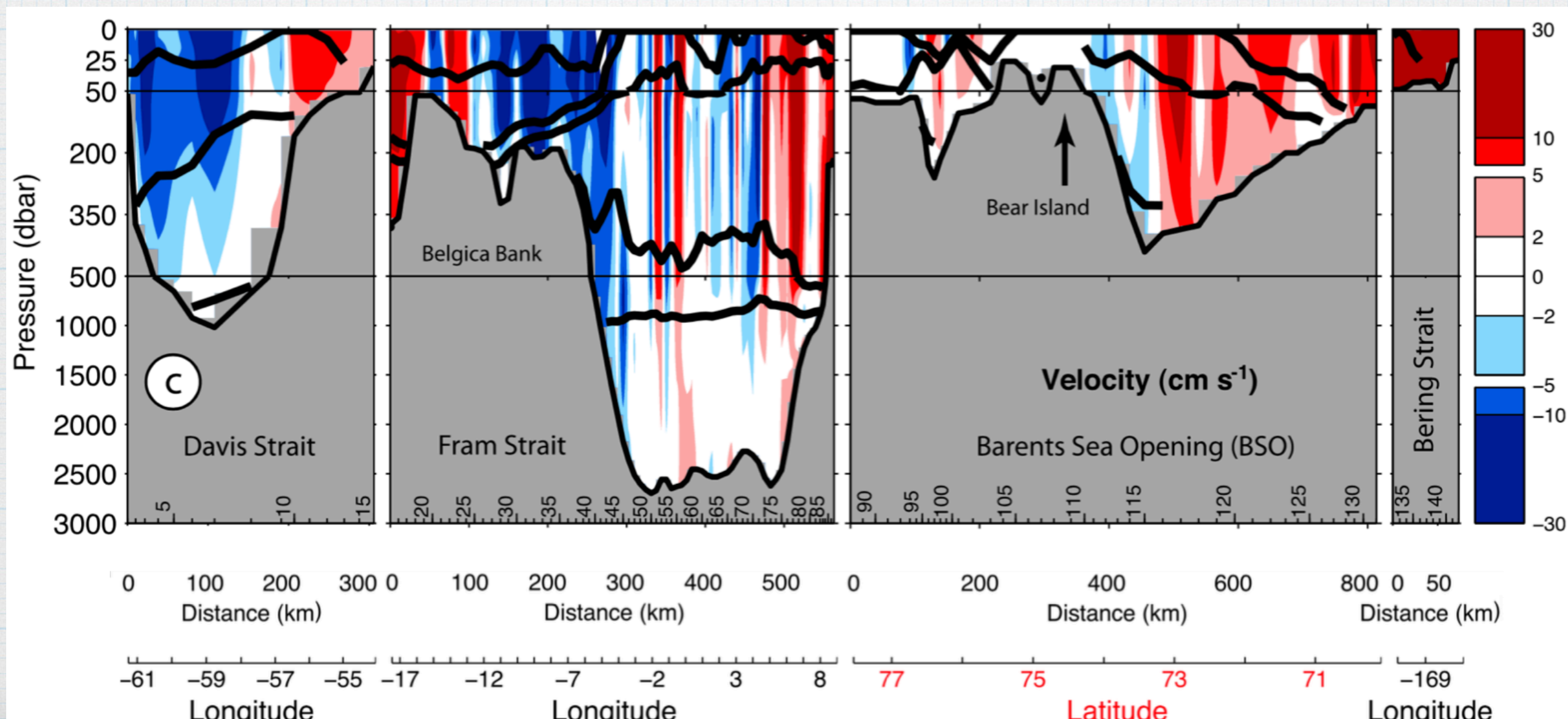


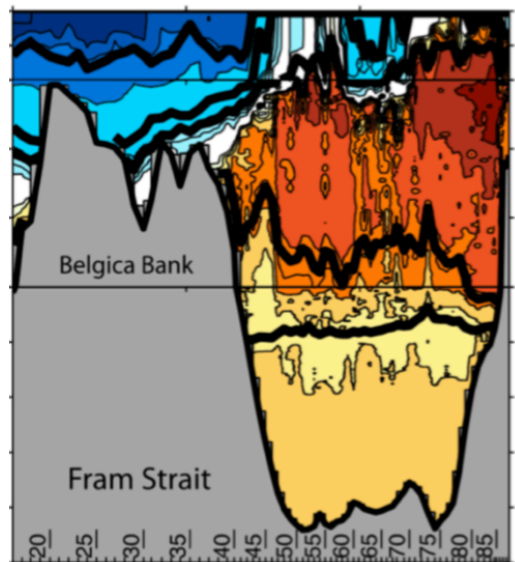
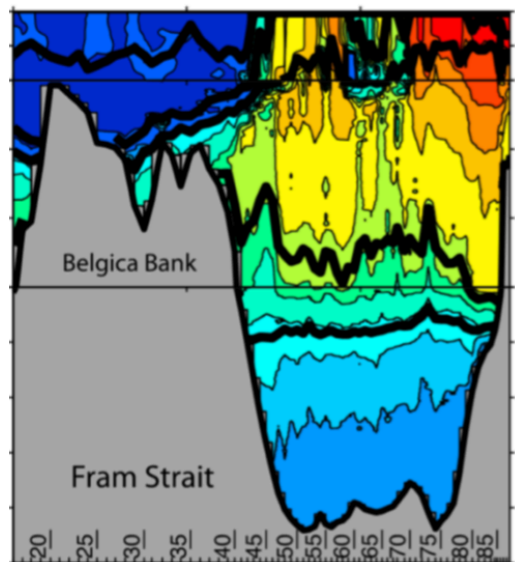
JOHNS HOPKINS
KRIEGER SCHOOL
of ARTS & SCIENCES

Conceptual Constraints on Polar MOCs

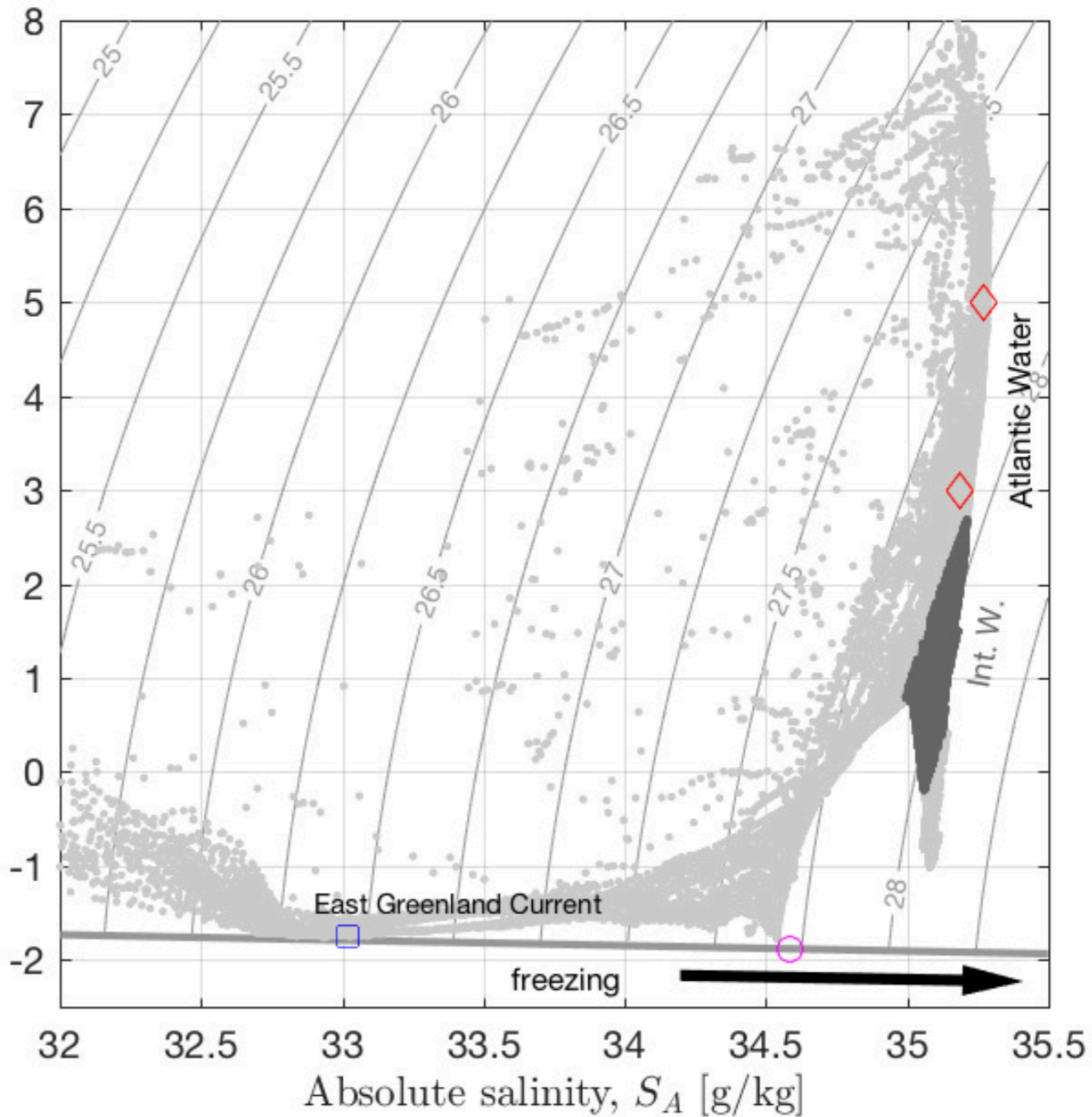
Tom Haine
Earth & Planetary Sciences,
Johns Hopkins University, Baltimore, MD



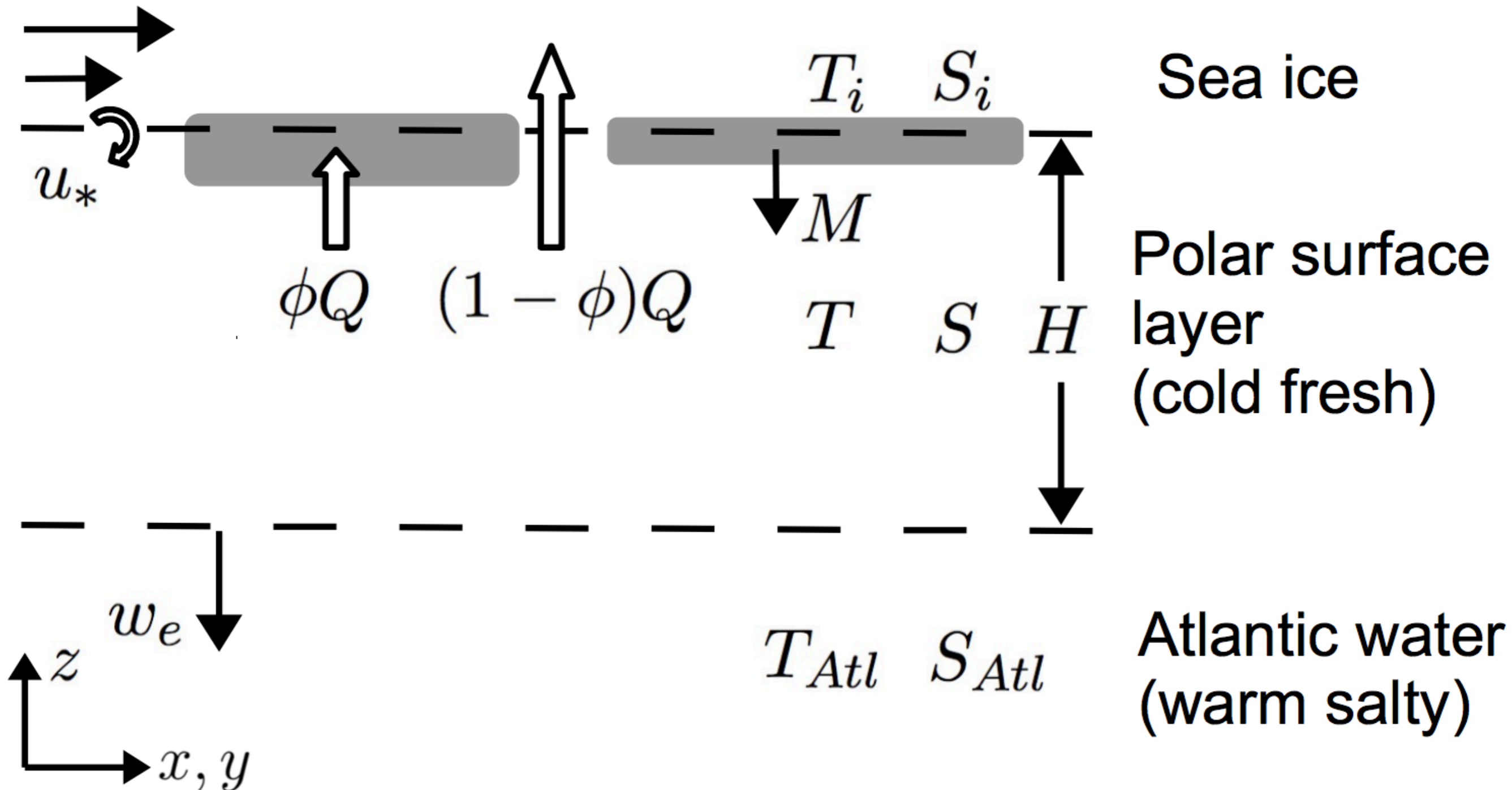




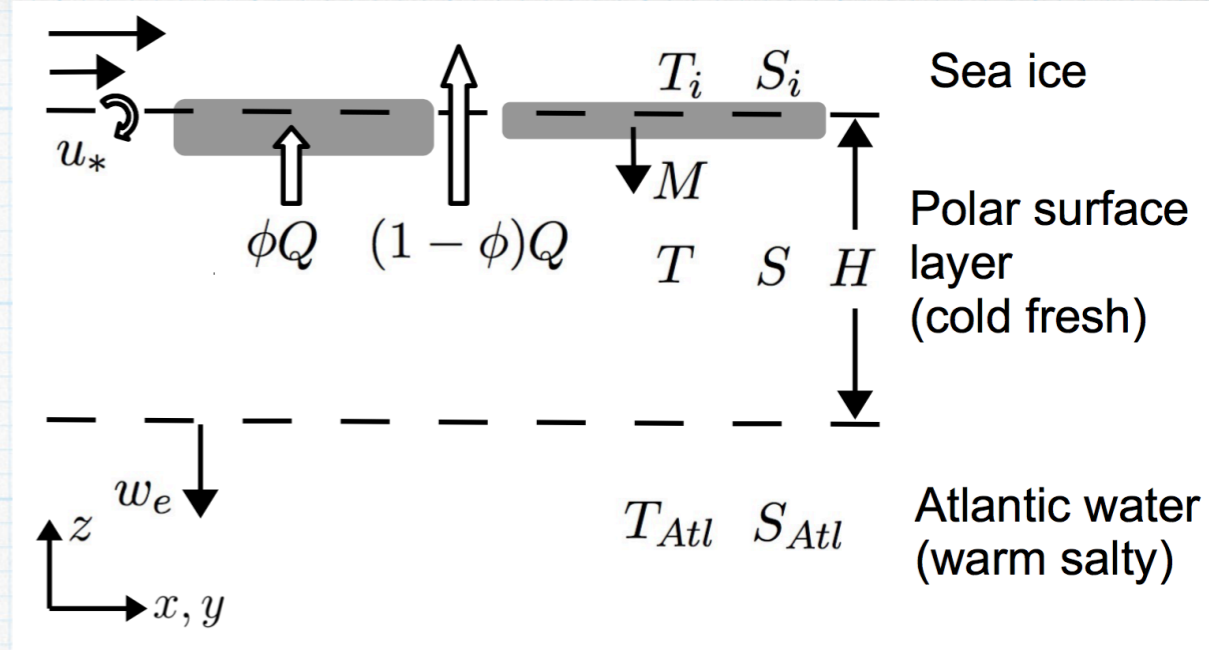
Conservative temperature, Θ [$^{\circ}\text{C}$]



Simple conceptual upper ocean model of Atlantic Water melting sea ice, e.g., in the Eurasian Basin



Fluxes of heat and freshwater



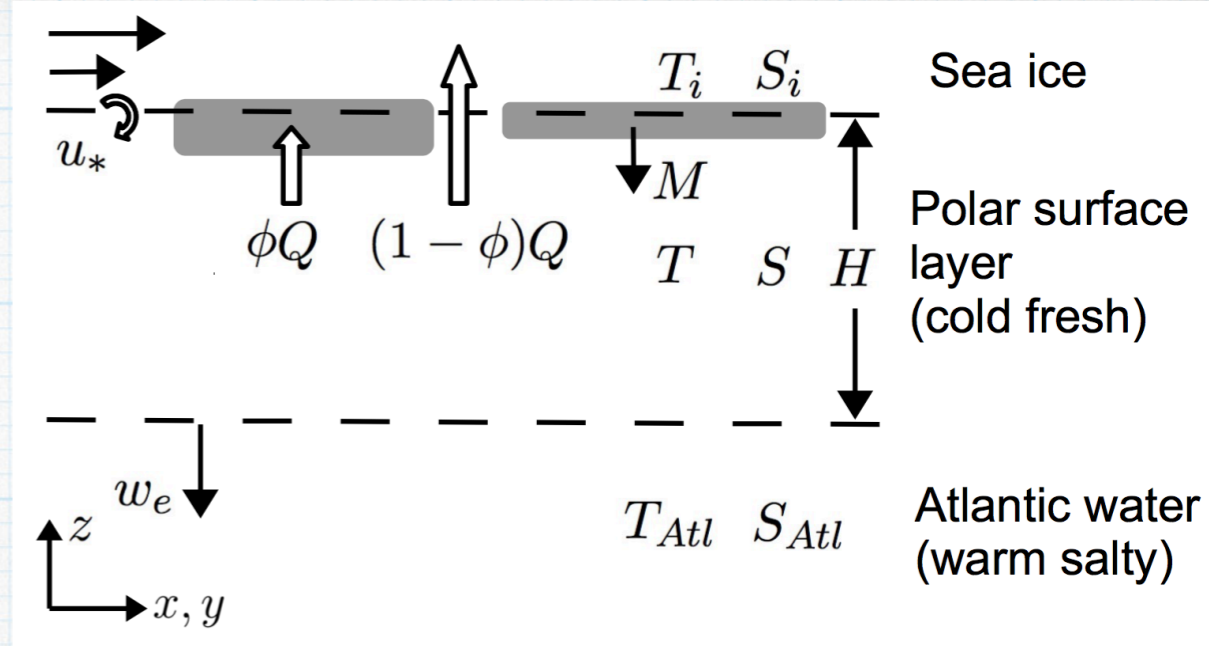
$$Q = Q_a + \rho_i M_i [L + c(T - T_f) + c_i(T_f - T_i)]$$

$$\mathcal{F} = -\frac{\rho_i}{\rho} M_i (S - S_i)$$

$$M = (\rho_i / \rho) M_i$$

$$M = \phi \frac{Q}{\rho [L + c(T - T_f) + c_i(T_f - T_i)]}$$

Evolution equations:



$$\begin{aligned}\frac{dH}{dt} &= w_e + M, \\ H \frac{dT}{dt} &= w_e \Delta T - \frac{Q}{\rho c}, \\ H \frac{dS}{dt} &= w_e \Delta S - M(S - S_i)\end{aligned}$$

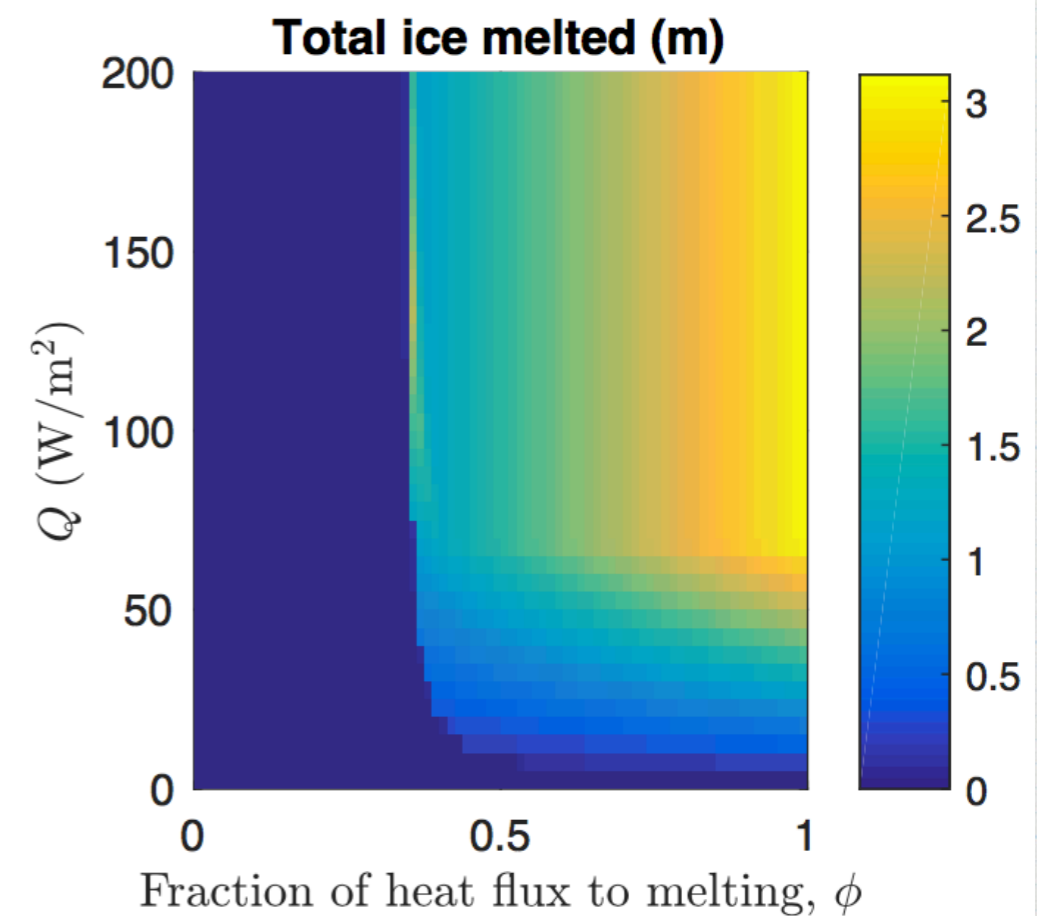
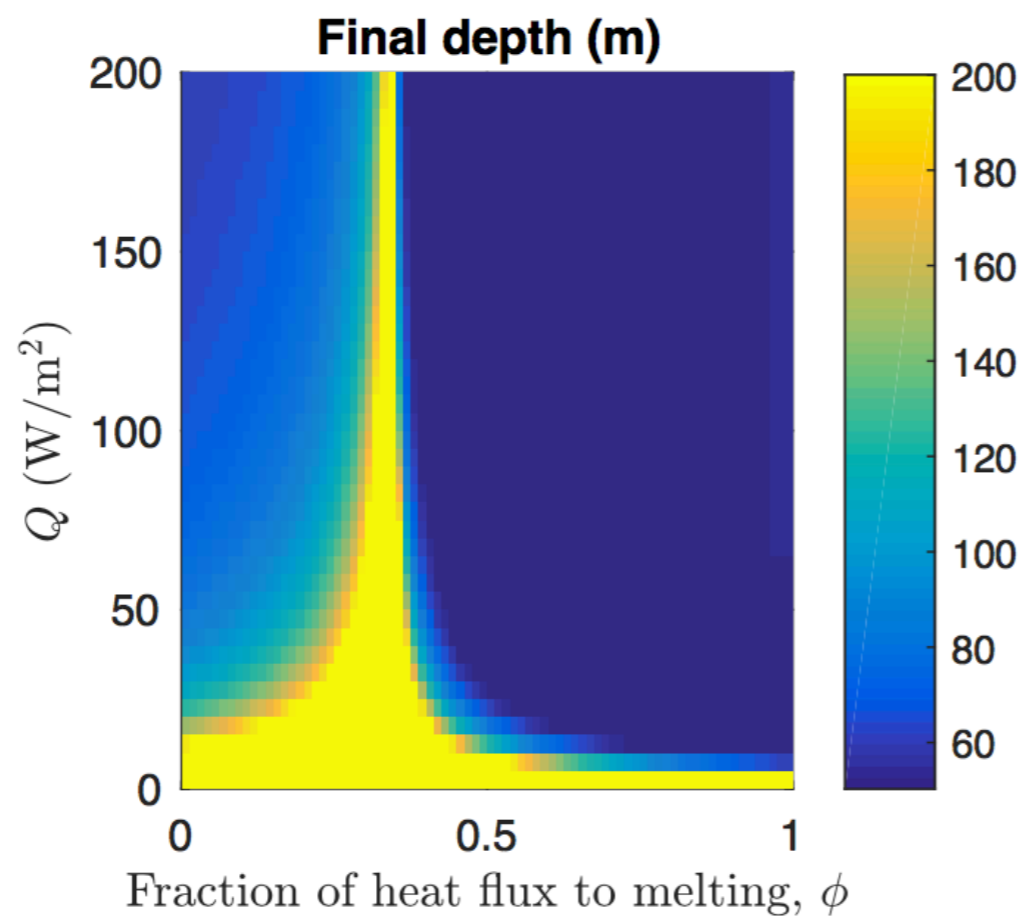
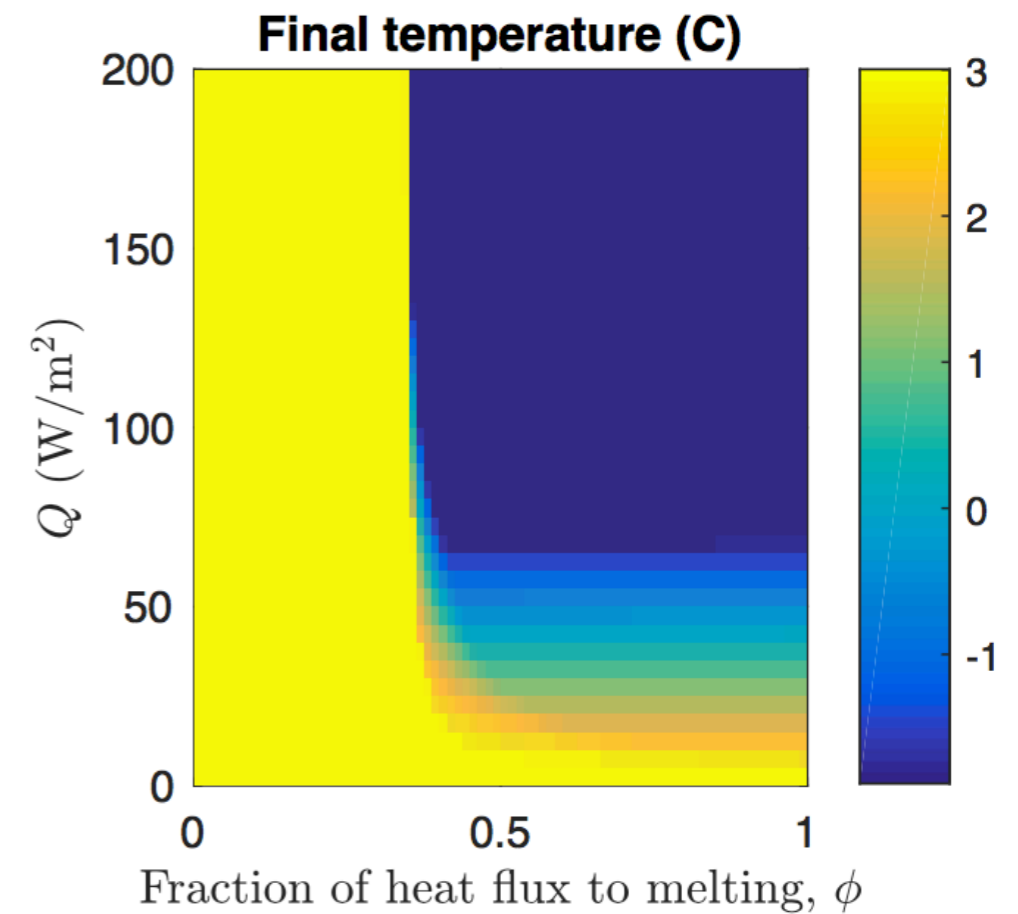
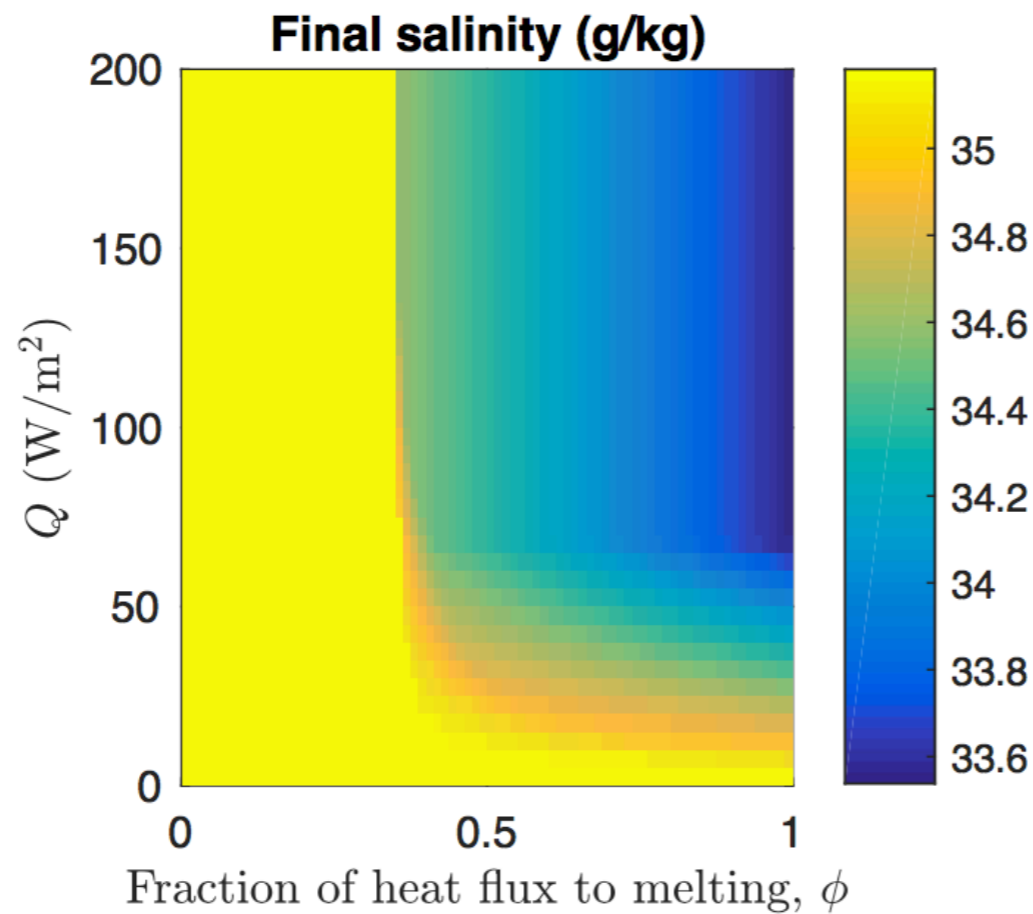
$$\Delta \rho = \rho(T_{Atl}, S_{Atl}) - \rho(T, S)$$

$$\begin{aligned}w_e &= \frac{\rho}{g \Delta \rho} \left(\frac{2m_0 u_*^3}{H} - \epsilon B \right) \\ \epsilon &= \begin{cases} 1 & \text{for } B \geq 0, \\ 0.05 & \text{otherwise.} \end{cases}\end{aligned}$$

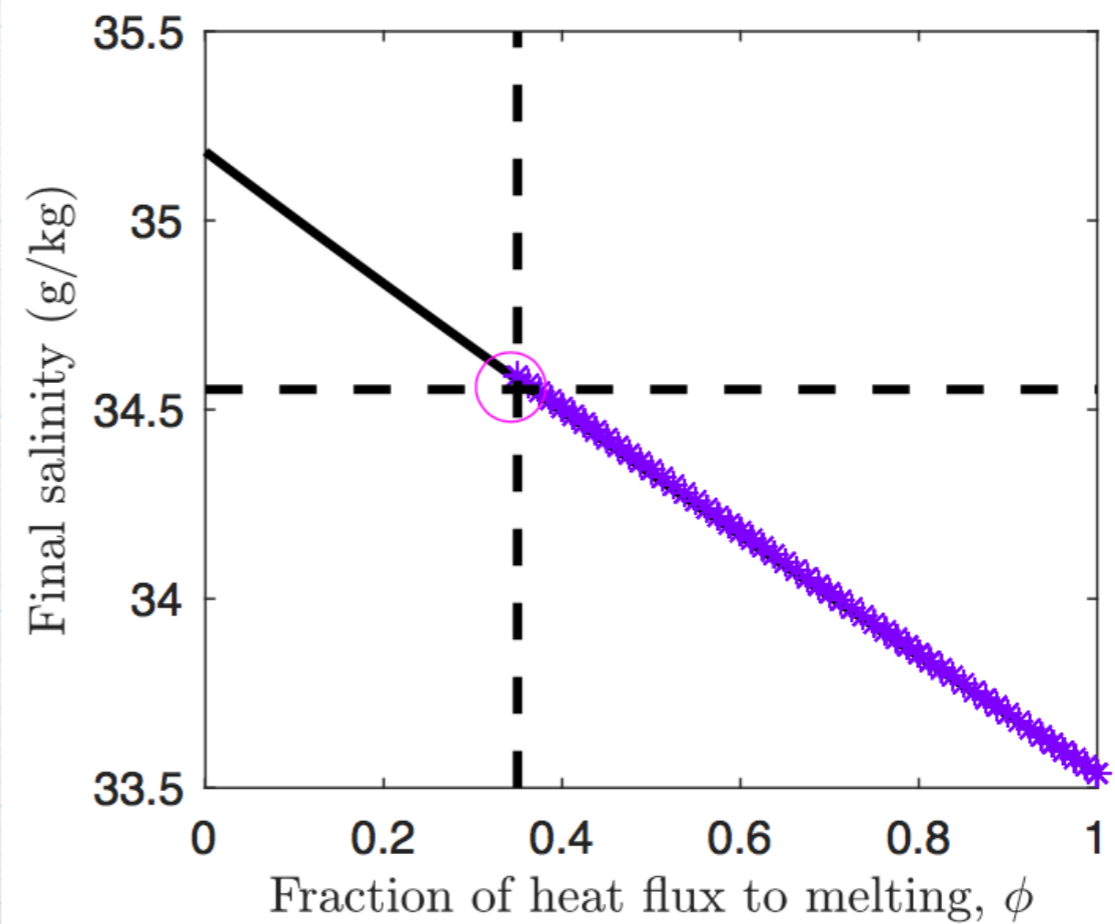
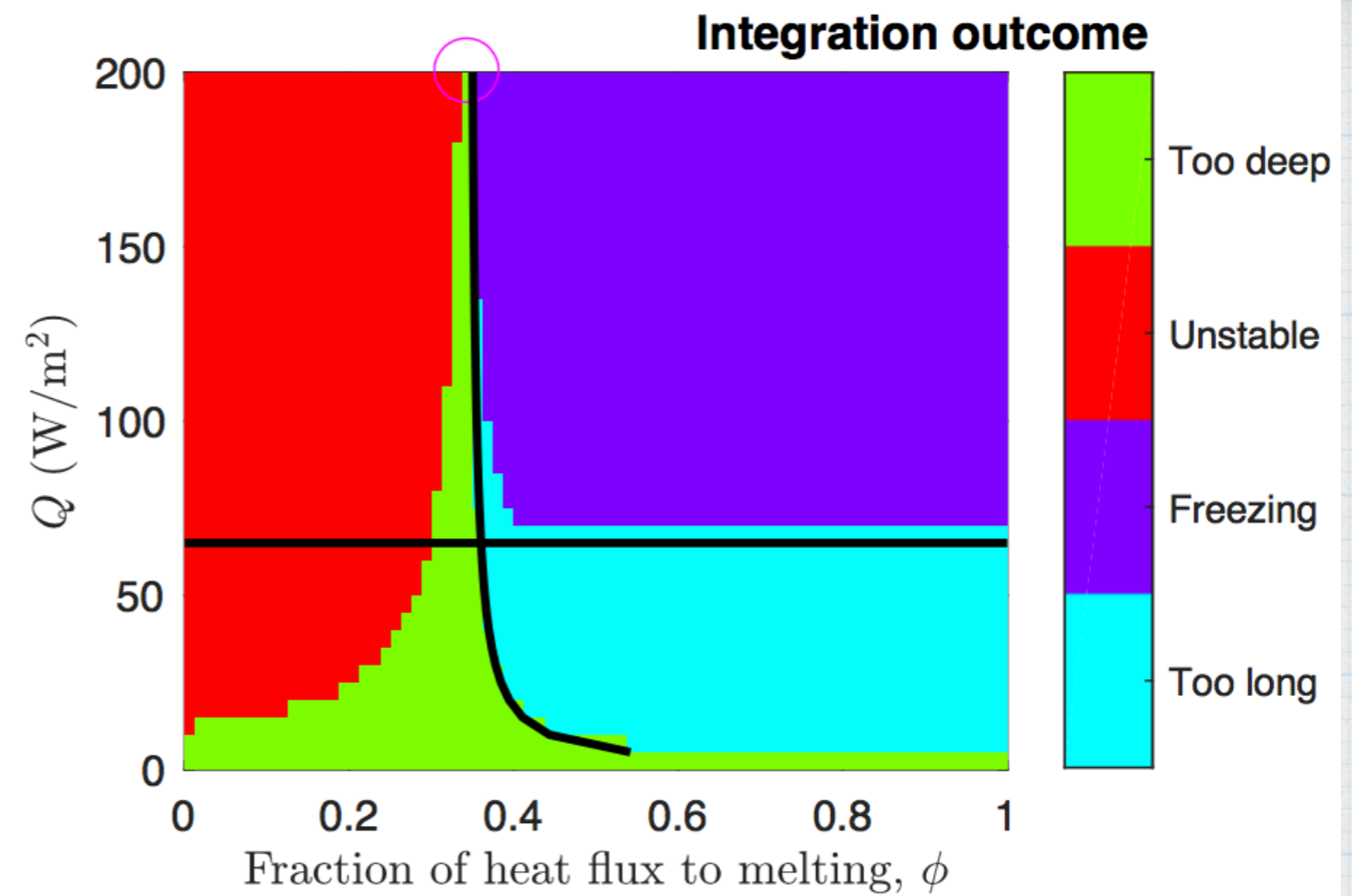
$$B = g \left[\frac{\alpha Q}{\rho c} + \beta M (S - S_i) \right]$$

Solutions:

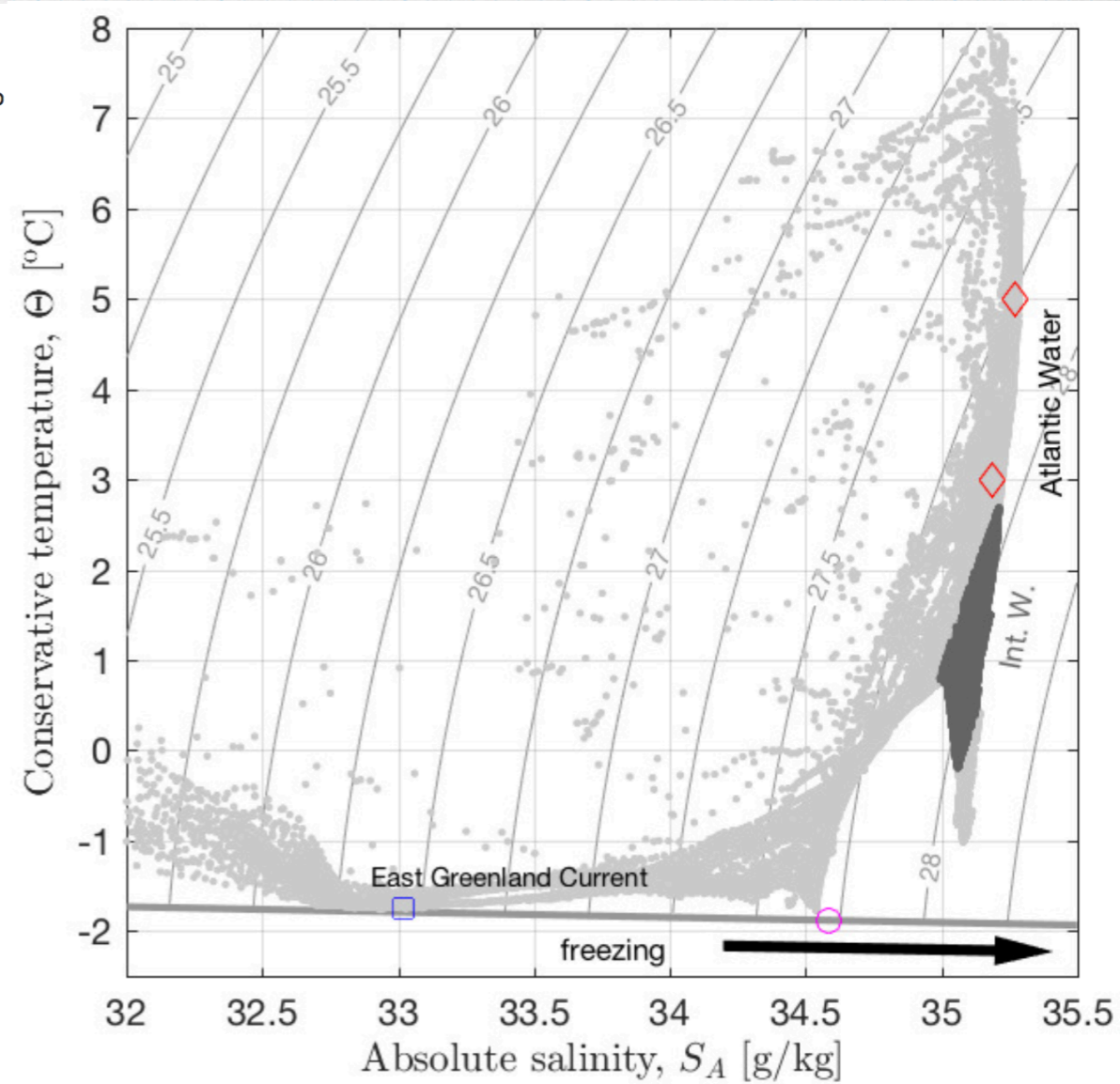
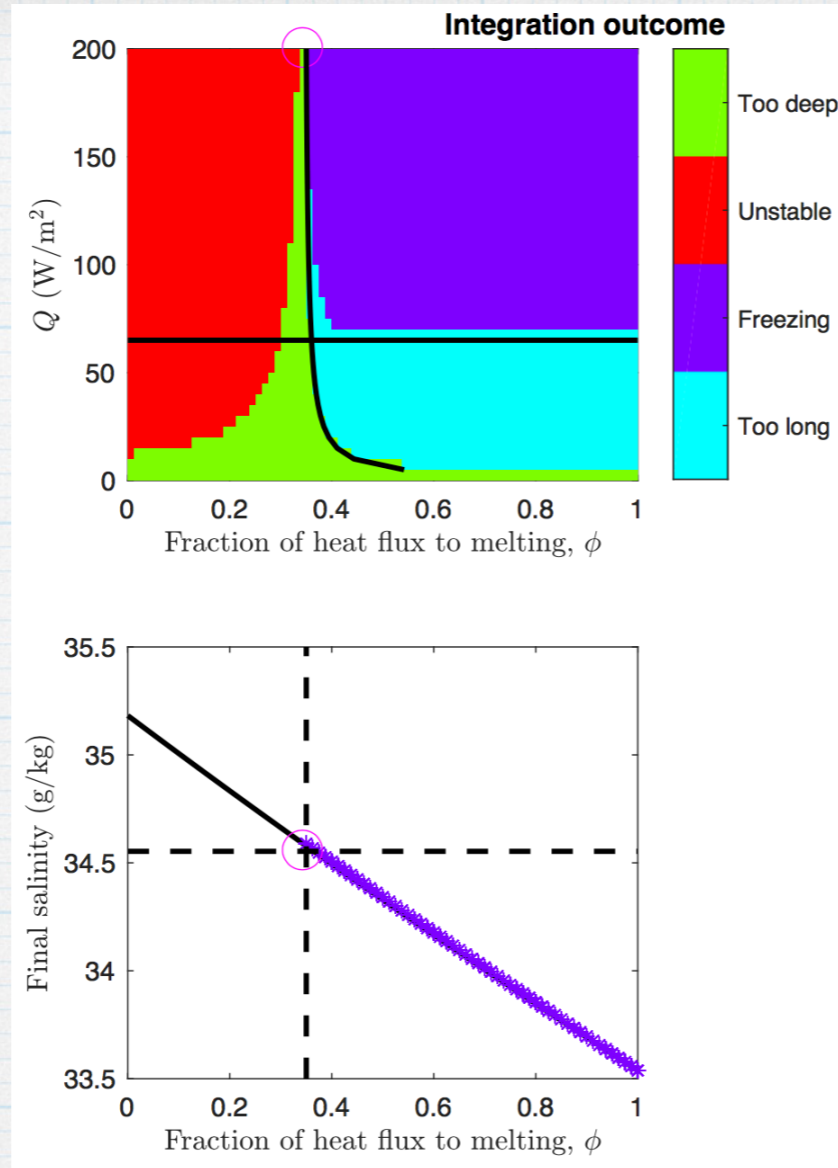
[For many
(ϕ , Q)
pairs]



Solution categories:



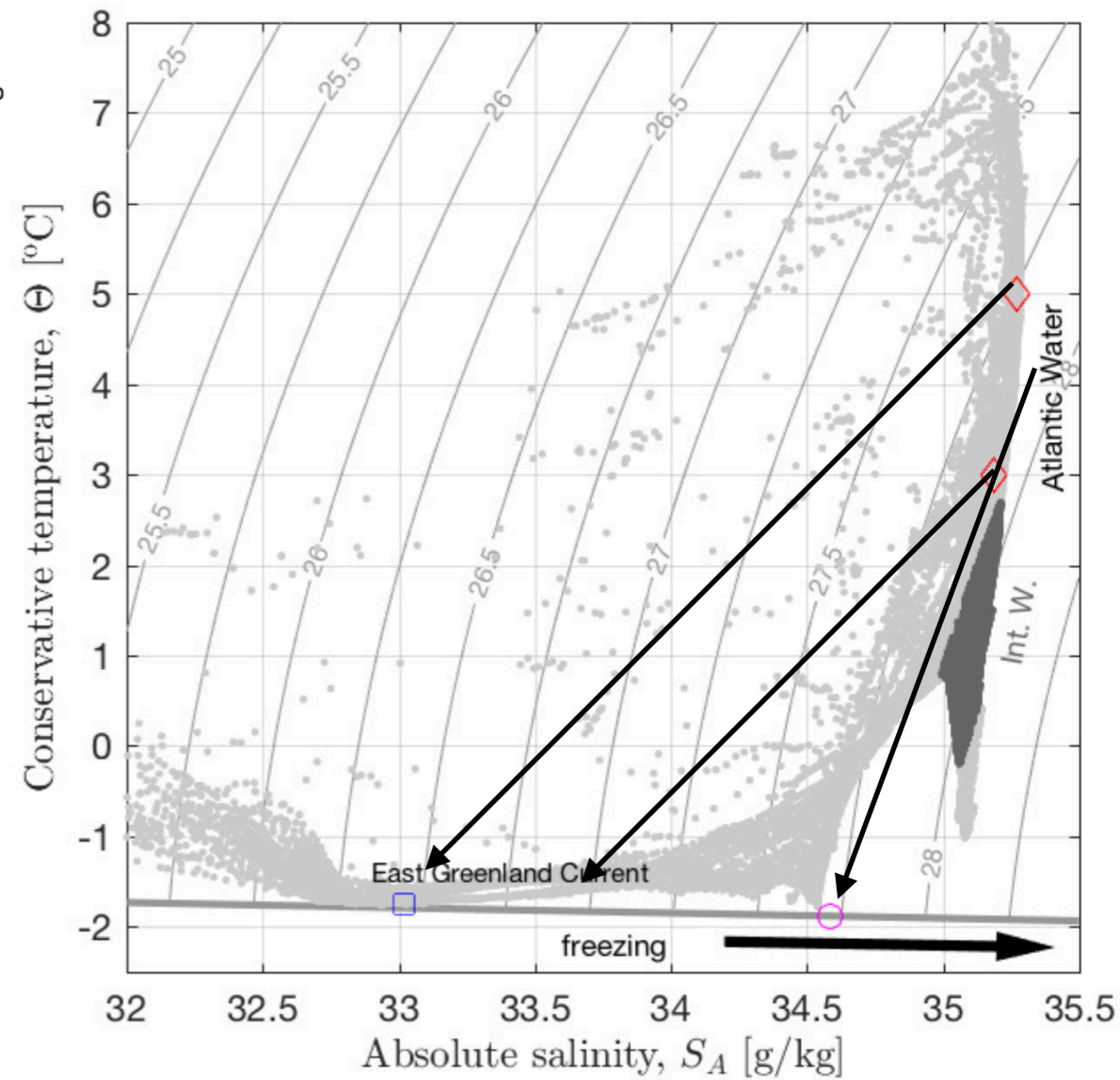
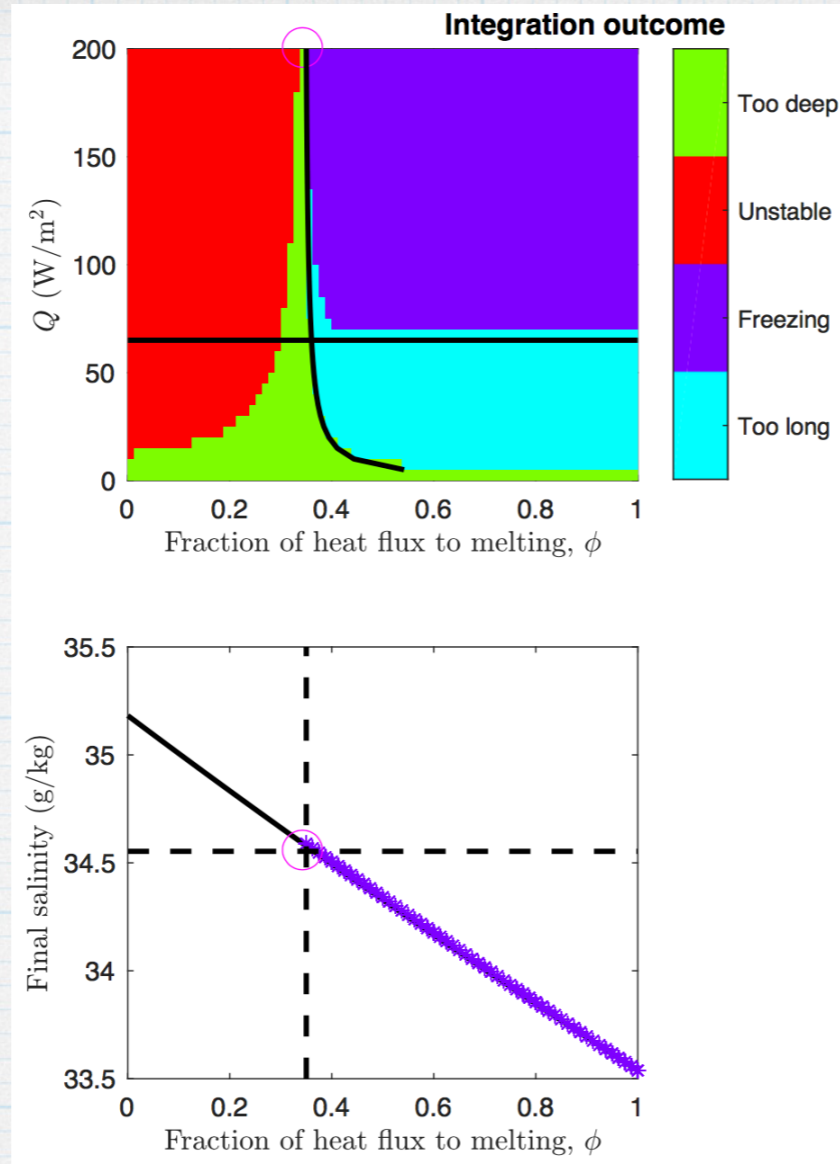
Properties of "EGC" water



$$S_1 = \frac{[L + c_i (T_f - T_i)] S_{Atl} + \phi c (T_{Atl} - T_f) S_i}{[L + c_i (T_f - T_i)] + \phi c (T_{Atl} - T_f)} \approx \frac{L S_{Atl}}{L + \phi c (T_{Atl} - T_f)}$$

$$\phi_{min} = \frac{-\alpha [L + c(T - T_f) + c_i(T_f - T_i)]}{\beta c (S - S_i)} \approx \frac{-\alpha L}{\beta c S}$$

Properties of "EGC" water



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Remarks

- * Conceptual model for properties of EGC (fresh polar outflow) water that fits the data well.
- * Comparison with Bert Rudels' formula. Similar fit to data, but different rationale.
- * Importance of partial melting of remotely-formed sea ice.
- * What sets the properties of the intermediate water?