### Transit Times in the North Atlantic DWBC Measured Using the Tracer Pair <sup>129</sup>I/CFC-11

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# <sup>129</sup>I Tracer Characteristics

- $t_{1/2}$  = 1.6 x 10<sup>7</sup> y
- Measured by AMS (IsoTrace: Univ. Toronto)
- 250 ml samples
- \$200/sample for AMS
  - Sample collection; cheap
  - Nuclear fuel reprocessing plant source Sellafield (UK) & La Hague (France)

#### **BNFL Sellafield**





































Core has uniform flow, u; interior has zero flow; mixing between regions is parameterized as relaxation with time scale,  $t_{mix}$ ;  $\alpha = \delta_b/\delta_i$  (= 0.1 in DWBC).

Tracer continuity equations:

$$\frac{\partial c_{b}}{\partial t} + u \frac{\partial c_{b}}{\partial x} + \frac{1}{t_{mix}} (c_{b} - c_{i}) = S$$
$$\frac{\partial c_{i}}{\partial t} - \frac{\alpha}{t_{mix}} (c_{b} - c_{i}) = S$$

 $C_b$  and  $C_i$  are tracer concentrations in boundary current and interior, respectively; S is tracer source or sink. Similar to Pickart et al. (1989); Rhein (1994); Doney and Jenkins, 1994.









## **Conclusions**

- Boundary current model advection times (t<sub>adv</sub>) of 5–7 y (u = 3 and 2 cm/s, respectively) and mixing times (t<sub>mix</sub>) of 3.5–7 y (intermediate to low mixing regimes) are all consistent with <sup>129</sup>I/CFC-11 results for the DWBC at Line W and the Labrador Sea.
- Values of u = 5 cm/s; t<sub>mix</sub> = 1 y are consistent with best-fit values in models of Pickart et al., 1989; Doney and Jenkins, 1994; core velocity is similar to mean velocities from direct measurements. However, other tracer studies imply lower spreading rates.
  - Line W <sup>129</sup>I/CFC-11 results (2010-2012) will further constrain advection and mixing times.

#### Transit Time Distributions for Boundary Current Model:

$$c(x,t) = \int_{0}^{n} c_{0}(t-t')G(x,t')dt'$$

 $\begin{array}{l} c_o(t) = time \ varying, tracer \ concentration \ at \ r = 0 \\ c(x, t) = interior \ tracer \ concentration \\ G(x, t) \ is \ the \ TTD \ at \ location \ x \end{array}$ 

$$G(x,t) = G_1 \delta(t - t_{adv}) + G_2 \Theta(t - t_{adv})$$

$$G_1 = e^{-t_{adv}/t_{mix}}$$

$$G_2 = \frac{\alpha}{\zeta t_{mix}} e^{-(1+\zeta^2)t_{adv}/t_{mix}} I_1(2\zeta t_{adv}/t_{mix})$$

$$t_{adv} = x/u = \text{advective time to reach point x}$$

 $\zeta^{2} = (\alpha u / x)(t - x / u)$   $I_{1} = \text{modified Bessel function of first order,}$   $\delta = \text{Dirac delta function}$   $\Theta = \text{Heaviside function}$ 



Waugh and Hall JPO 2005





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