Moist entropy: an idealized framework for poleward moisture transport

Defined on surfaces of constant moist entropy (moist isentropes), the general circulation collapses to a single hemispheric cell in which mass moves poleward from the tropics. Equivalent potential temperature is a typical measure of moist entropy and depends on 3 key variables:

\[
\theta_e \approx \frac{T}{p} \left( L_v r \frac{p_u}{p} \right) R_a / c_p d
\]

Water tags (CESM) show ocean evaporation largely following moist isentropic surfaces

Each moist isentrope (contours) defines a moisture transport pathway with a length that depends on the surface geometry.

Surface length describes total rainout and predicts isotopic changes seasonally

Water vapor isotope ratios (\( x, \delta \)) in CESM, averaged along moist isentropic surfaces (colors, units K), match predictions from simple Rayleigh distillation (lines), as expected if poleward moisture transport is moist isentropic and mixing negligible (a).

Individually, air temperature, moisture content (i.e. rainout), and the isotopic composition of the moisture source cannot predict seasonal isotopic changes (b). Shifts in moist isentropic surface geometry, indicating changes in total effective rainout, can (a).

Implications for detecting changes in the global circulation with isotopes

If moisture flux divergence = evaporation (E) – precipitation (P), the isotope ratio of atmospheric moisture \( R_x \) in zone x is given by

\[
R_x = I_x + \exp(-\lambda dx) \times R_x^1
\]

\( I_x \) describes isotopic imbalance between local E and P

\( R_x^1 \) is the isotope ratio of the zone upstream

\( \lambda \) is \((E-P)/F\), the inverse of the moisture length scale, and \( F \) is the moisture flux

If both E-P and atmospheric moisture scale with Clausius-Clayperon (e.g. temperature),

\[
\Delta \lambda / \lambda = -\Delta T / T
\]

or \( \lambda \) will change proportionally with the meridional wind.

If local isotopic variations are small, the ratio of isotope ratios from neighboring regions will track this change.