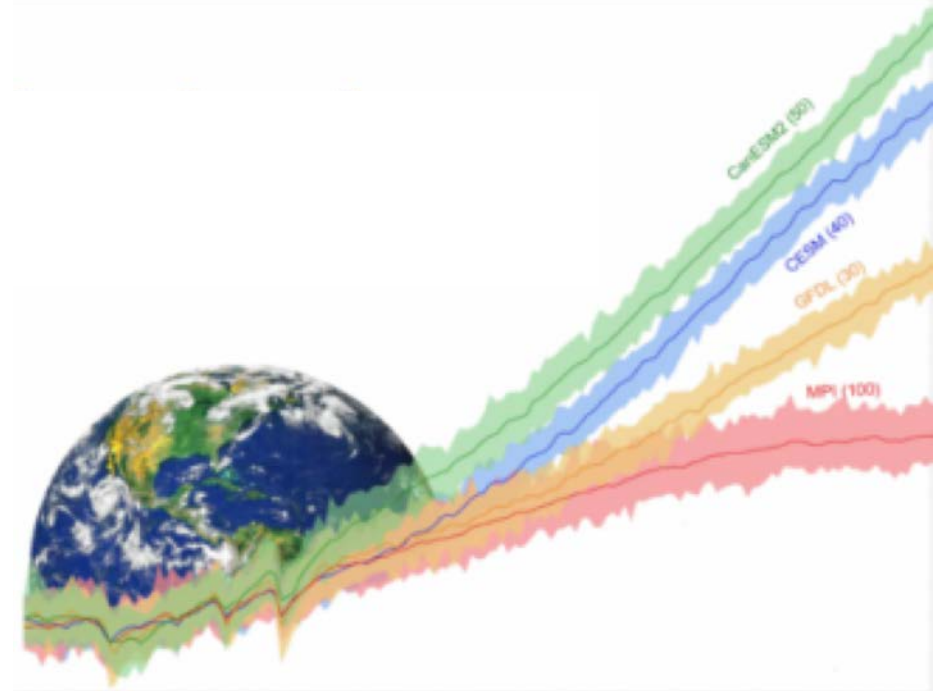


# Large ensemble testbed

Evaluating pCO<sub>2</sub> interpolation methods

Luke Gloege



# Air-Sea CO<sub>2</sub> exchange

pCO<sub>2</sub><sup>atm.</sup>



pCO<sub>2</sub><sup>atm.</sup>

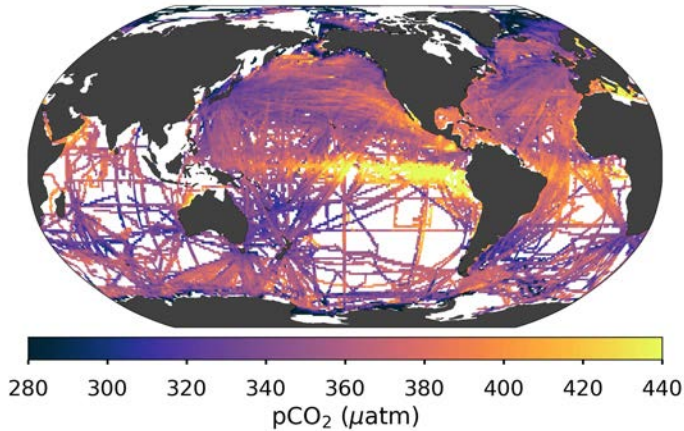


pCO<sub>2</sub><sup>ocean</sup>

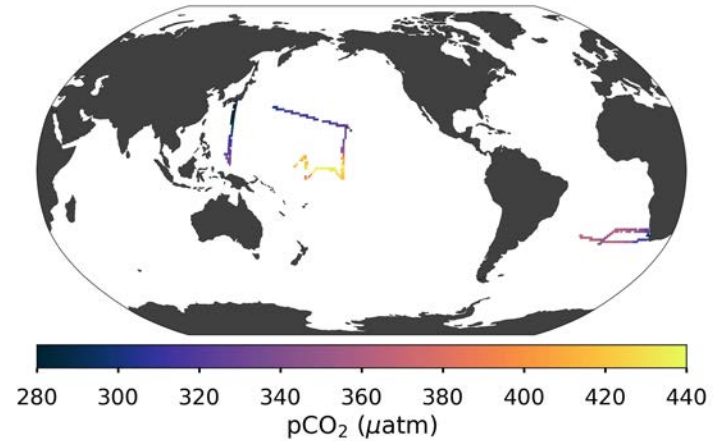
pCO<sub>2</sub><sup>ocean</sup>

# Surface Ocean CO<sub>2</sub> Atlas

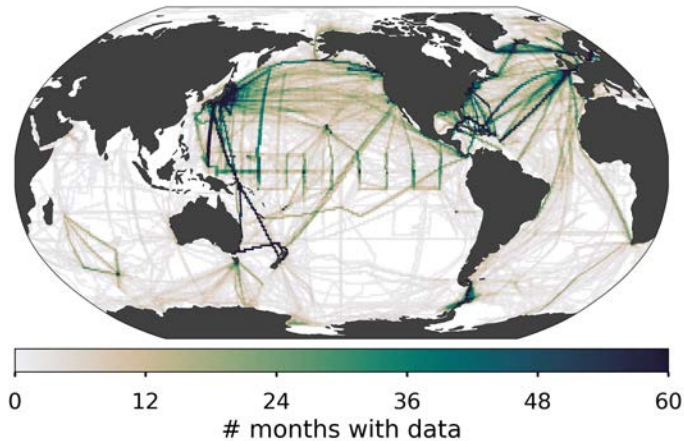
**Global average (1982-2015)**



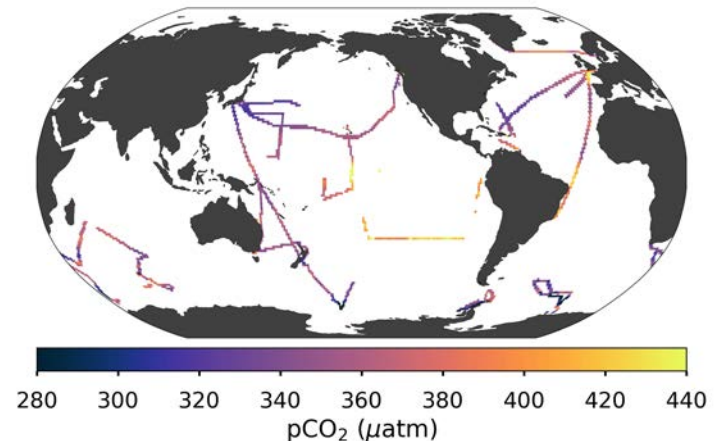
**January 1989**



**Number of months with data**

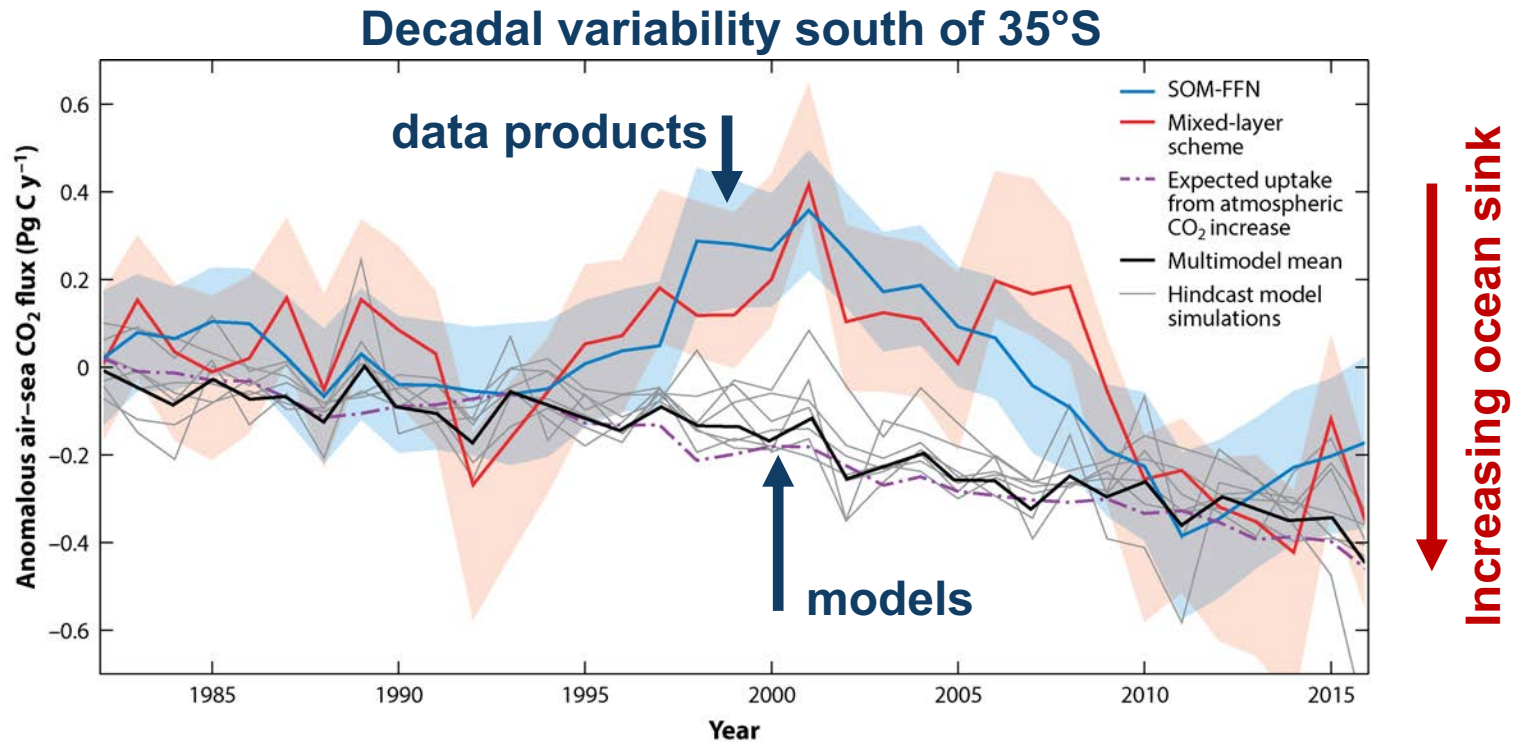


**January 2010**



# Models and data products mismatch

- Data products are more variable than models
- Different interpretation for evolution of ocean carbon sink
- Which is correct : models or data products?

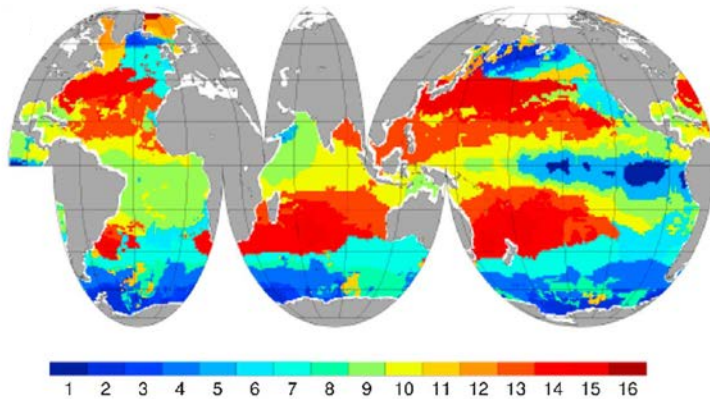


AR Gruber N, et al. 2019.  
*Annu. Rev. Mar. Sci.* 11:159–86

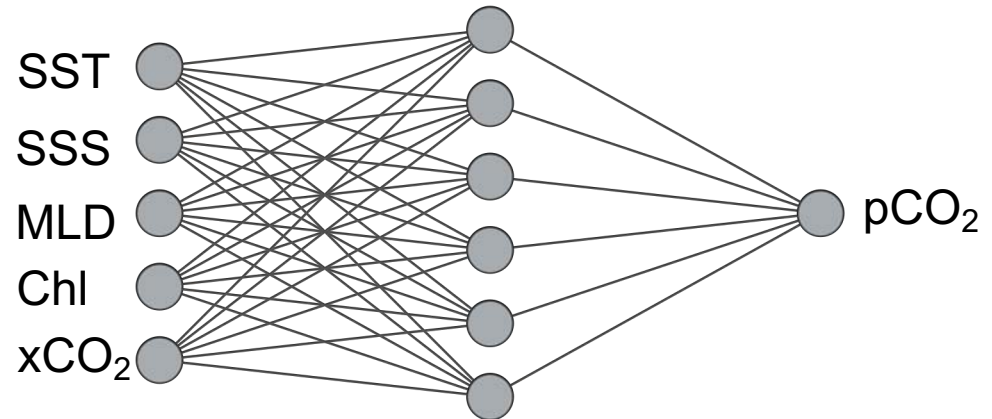
Gruber, Landschützer, and Lovenduski (2019).

# Two-step neural network (SOM-FFN)

**SOM : Self organizing map**



**FFN : feed-forward neural network**



1. Climatological pCO<sub>2</sub>, SSS, SST, and MLD
2. Data grouped using self organizing map

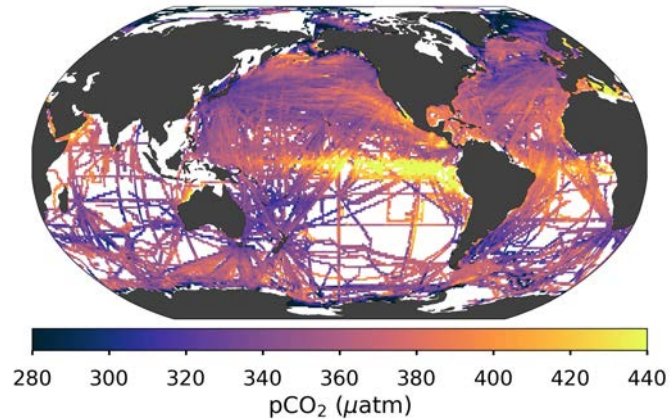
- Learns a non-linear relationship between global features and pCO<sub>2</sub>
- Inputs are proxies for processes affecting ocean pCO<sub>2</sub>

Landschützer et al. 2013, 2014, 2016

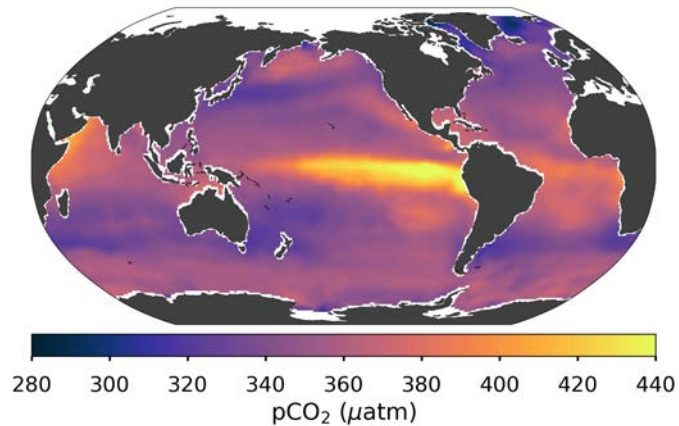


# Comparing SOM-FFN and SOCAT

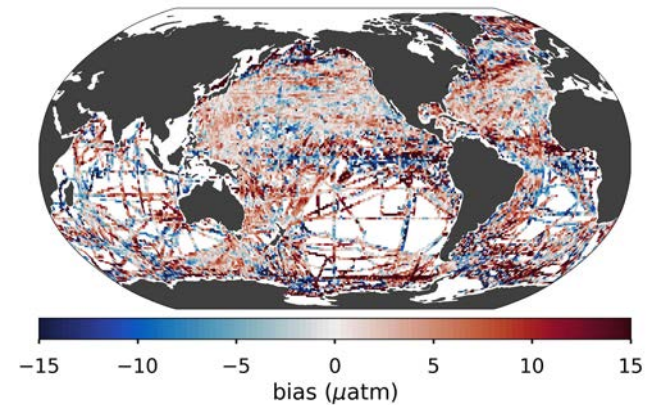
## SOCATv2019 data



## SOM-FFN product



## Bias (global avg. 2.15 µatm)



Bakker et al. 2016 EESD; Sabine et al. 2013

Landschützer et al. 2013, 2014, 2016

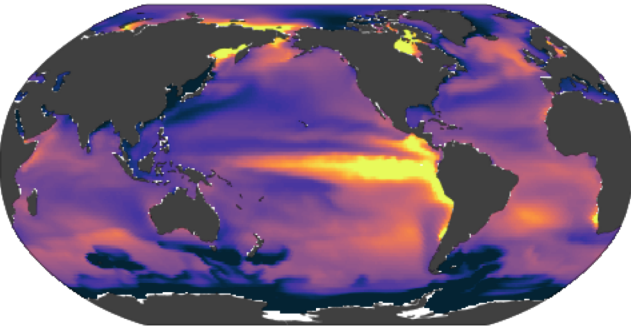
# How large ensembles can help

- Evaluate performance across different climate states
- **100 randomly selected ensemble members**
  - CanESM2 (25)
  - CESM (25)
  - GFDL (25)
  - MPI (25)
- Each climate state is equally likely
- Only considering 1982-2015



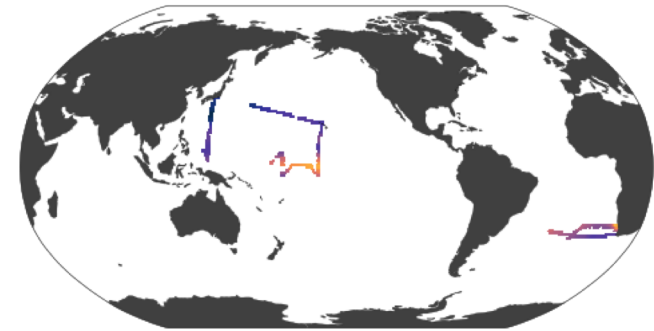
# Large ensemble pCO<sub>2</sub> testbed

CESM 002



x100 members  
■■■■■■■■■■▶

1. Sample model member as SOCAT monthly pCO<sub>2</sub> product



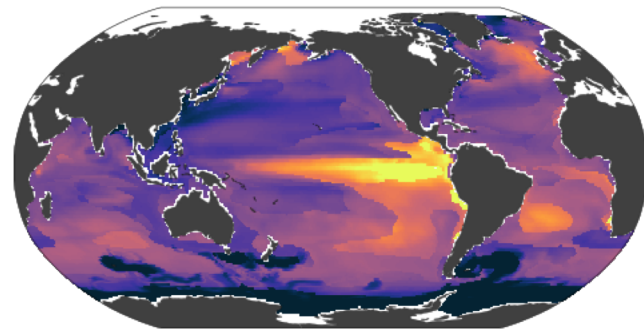
2. Train, evaluate, test reconstruction method at sampled locations



4. Statistically compare reconstructed pCO<sub>2</sub> to model truth. Each spatial point is temporally decomposed

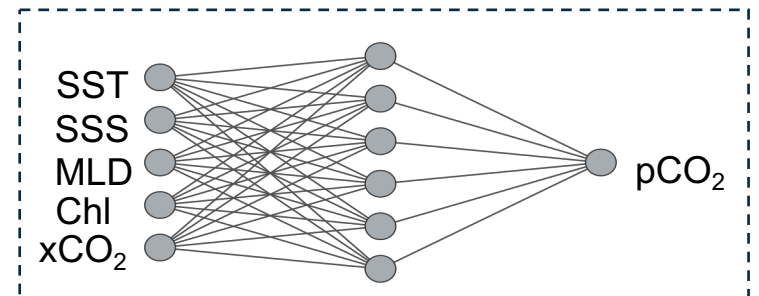


3. Estimate monthly varying pCO<sub>2</sub> on global scale using trained model



reconstruction

◀ x100 members

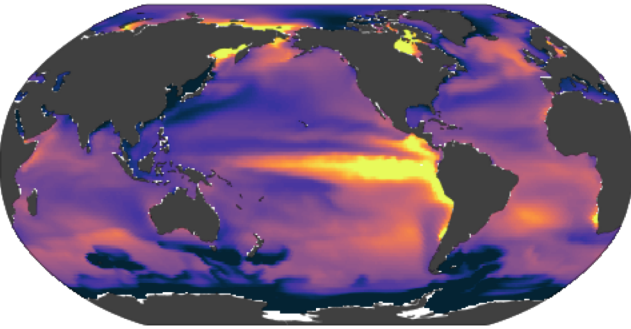


Neural network reconstruction method



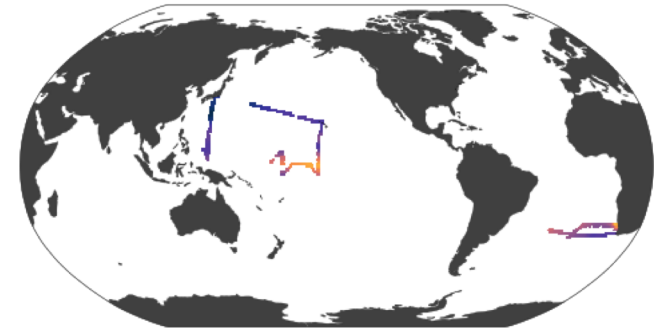
# Large ensemble pCO<sub>2</sub> testbed

CESM 002



x100 members  
■■■■■■■■■■▶

1. Sample model member as SOCAT monthly pCO<sub>2</sub> product

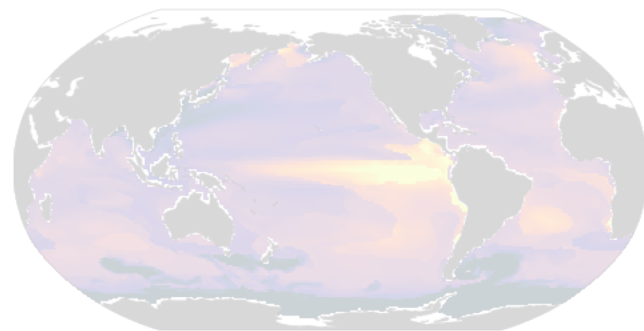


2. Train, evaluate, test reconstruction method at sampled locations

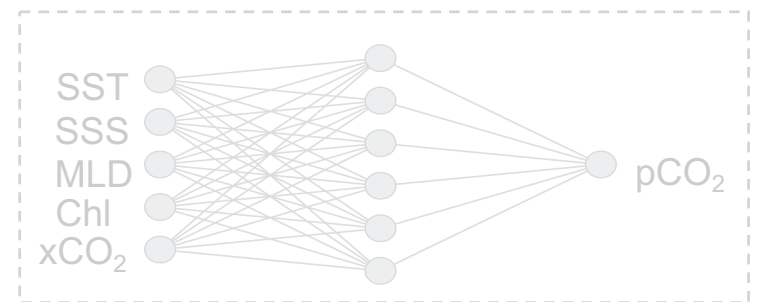


3. Estimate monthly varying pCO<sub>2</sub> on global scale using trained model

◀ x100 members



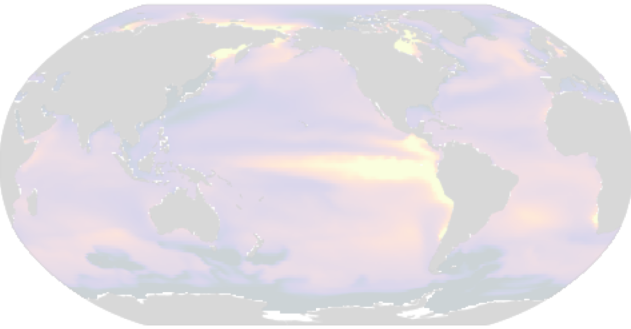
reconstruction



Neural network reconstruction method

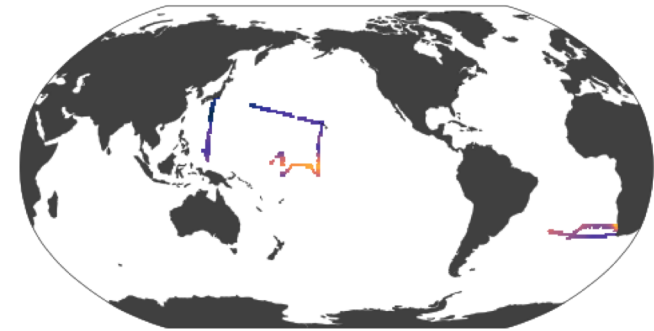
# Large ensemble pCO<sub>2</sub> testbed

CESM 002



x100 members  
----->

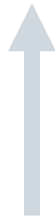
1. Sample model member as  
SOCAT monthly pCO<sub>2</sub> product



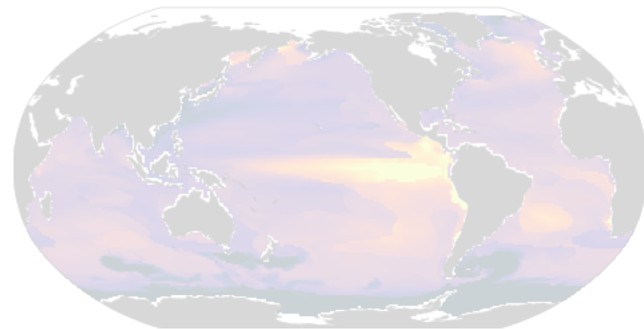
2. Train, evaluate, test  
reconstruction method  
at sampled locations



4. Statistically compare  
reconstructed pCO<sub>2</sub> to model  
truth. Each spatial point is  
temporally decomposed

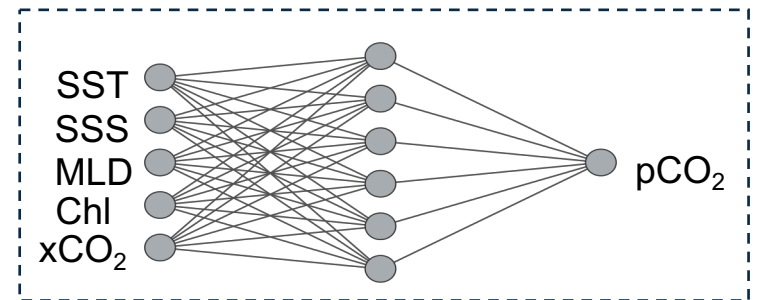


3. Estimate monthly  
varying pCO<sub>2</sub> on global  
scale using trained  
model



reconstruction

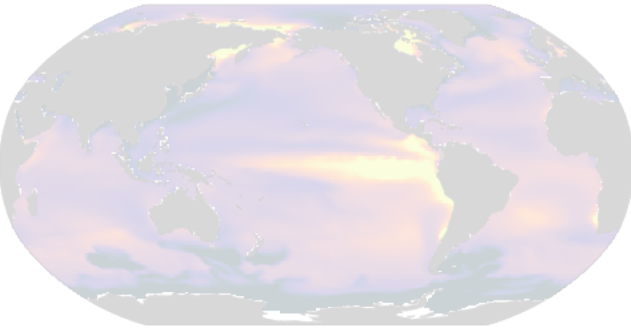
-----<  
x100 members



Neural network reconstruction method

# Large ensemble pCO<sub>2</sub> testbed

CESM 002



x100 members  
----->

1. Sample model member as SOCAT monthly pCO<sub>2</sub> product



2. Train, evaluate, test reconstruction method at sampled locations

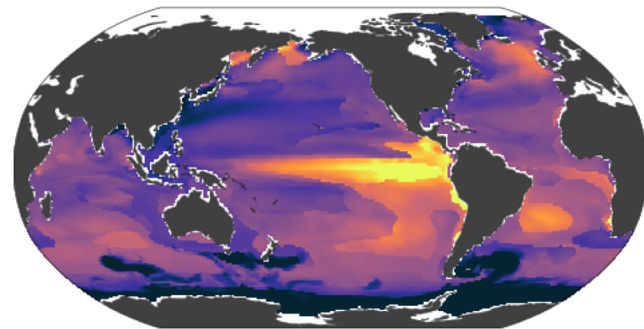


4. Statistically compare reconstructed pCO<sub>2</sub> to model truth. Each spatial point is temporally decomposed

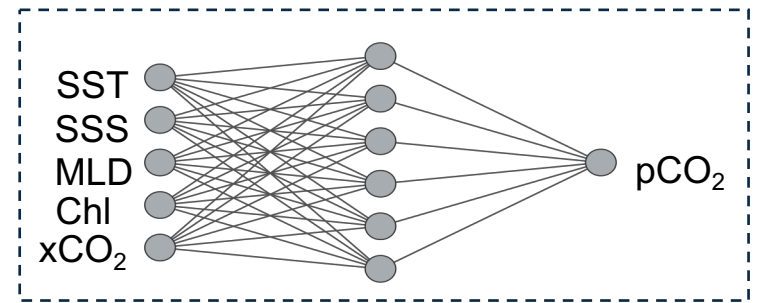


3. Estimate monthly varying pCO<sub>2</sub> on global scale using trained model

-----<  
x100 members



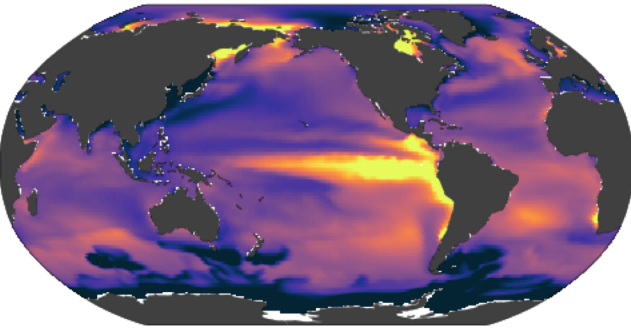
reconstruction



Neural network reconstruction method

# Large ensemble pCO<sub>2</sub> testbed

CESM 002



x100 members  
----->

1. Sample model member as SOCAT monthly pCO<sub>2</sub> product

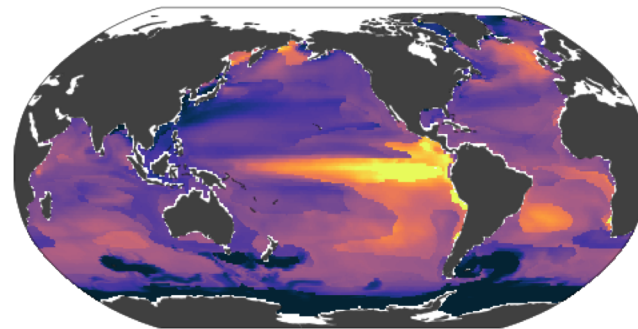


2. Train, evaluate, test reconstruction method at sampled locations

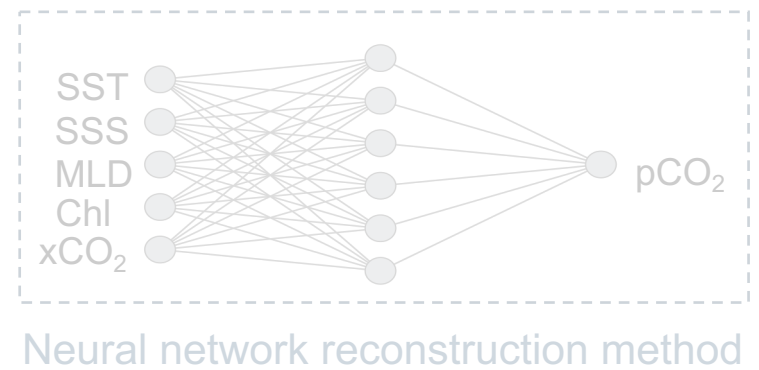


3. Estimate monthly varying pCO<sub>2</sub> on global scale using trained model

-----<  
x100 members



reconstruction



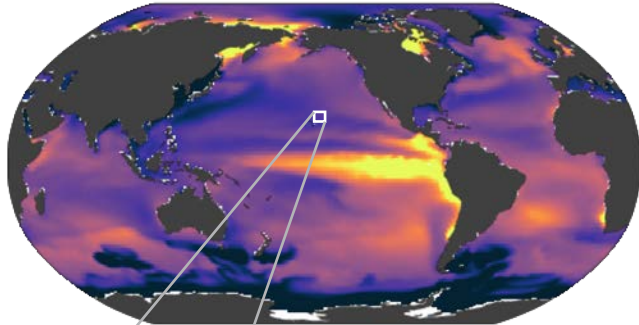
Neural network reconstruction method

4. Statistically compare reconstructed pCO<sub>2</sub> to model truth. Each spatial point is temporally decomposed

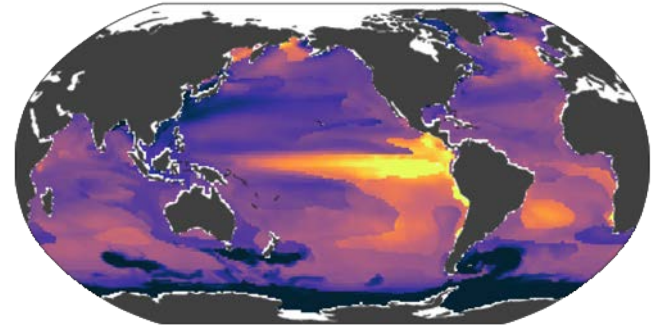


# Temporal decomposition

Ensemble member



Reconstruction



Each location in each member and reconstruction decomposed into seasonal, decadal, and sub-decadal variability

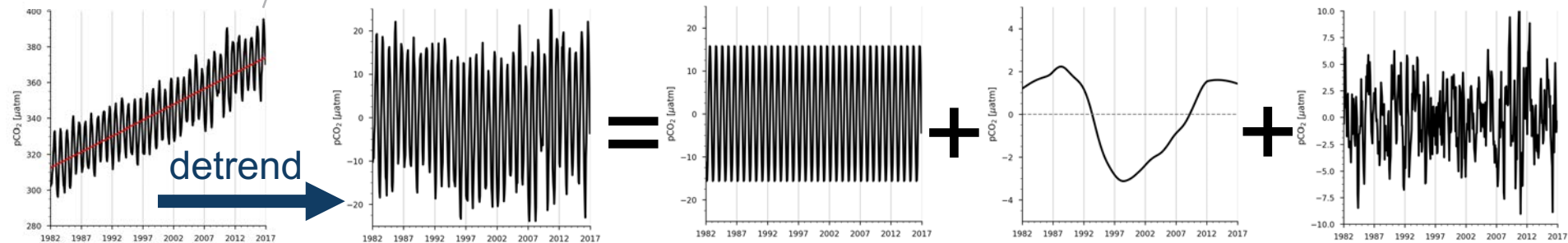
Full Signal

Detrended

Seasonal

Dec. var.

Sub-dec. var.



Cleveland et al. (1990) *Journal of official statistics*.



# Statistical metrics

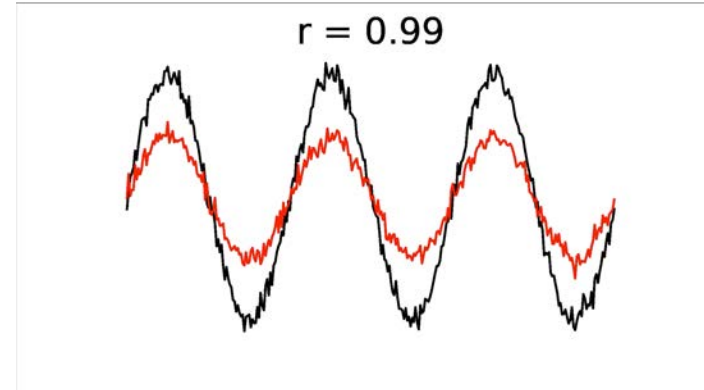
Model Reconstruction

## Phasing

Is reconstruction in phase with model?

Correlation

$$r = \frac{\text{cov}(m,r)}{\sigma_r \sigma_m}$$

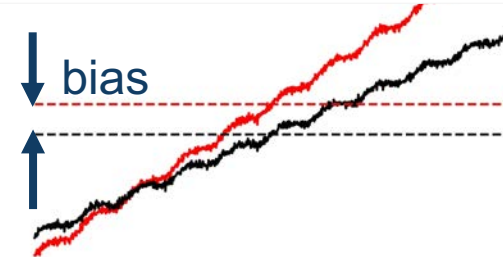


## Long-term mean

is there a systemic offset?

Bias

$$\text{Bias} = \bar{m} - \bar{r}$$

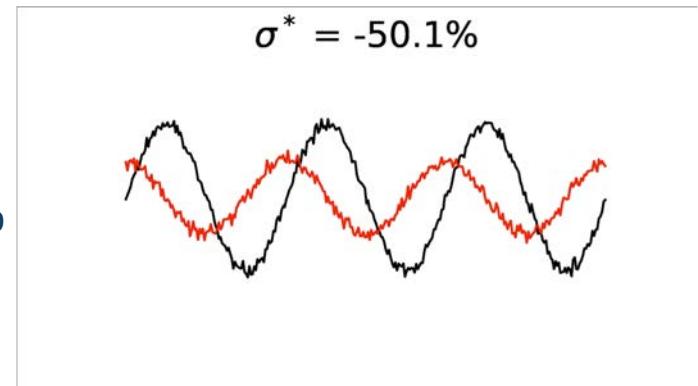


## Variability

does reconstruction capture observed variability?

Normalized STD

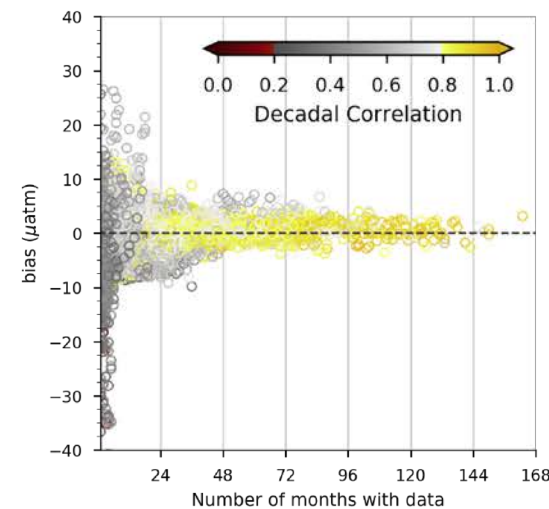
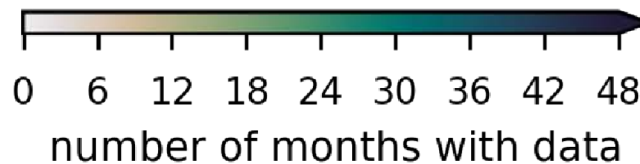
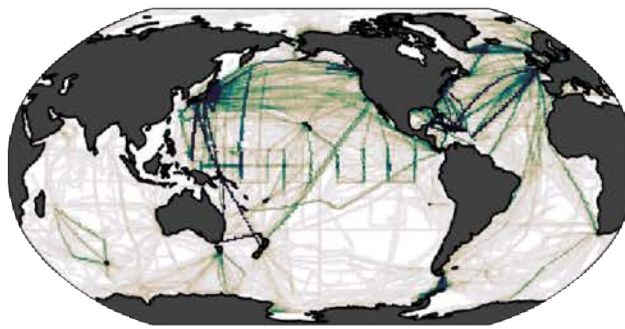
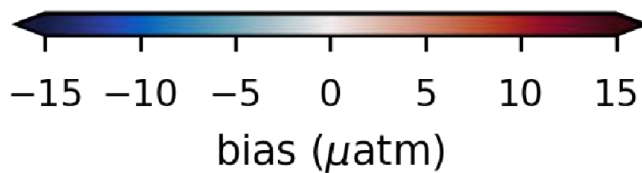
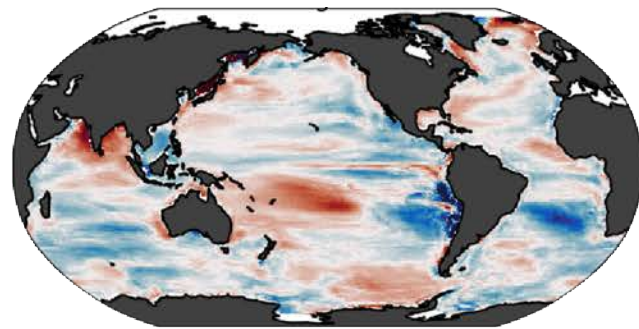
$$\sigma^* = \left[ \left( \frac{\sigma_r}{\sigma_m} \right) - 1 \right] * 100\%$$



# Bias and number of observations

Is the reconstruction offset from the model?

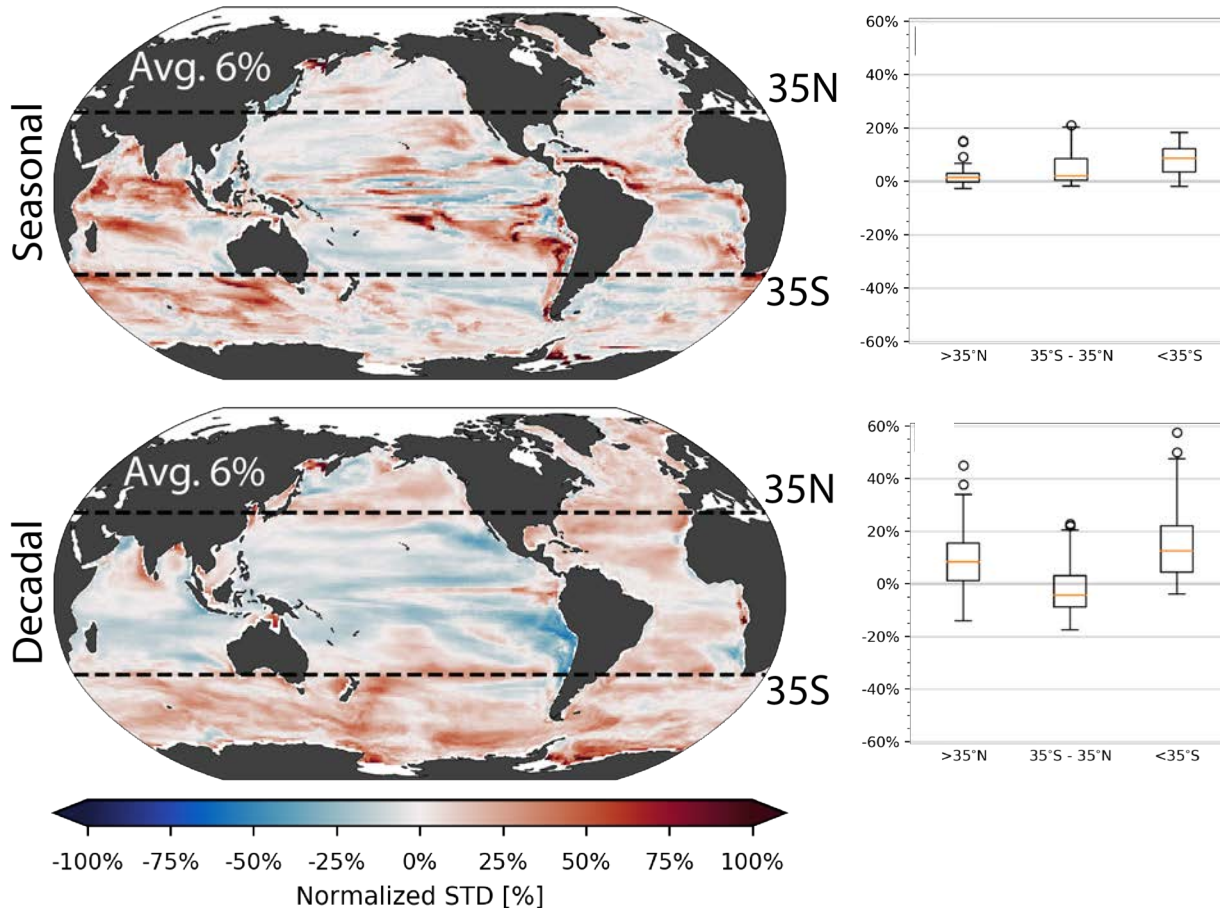
Global avg =  $-0.44 \mu\text{atm}$



- Bias spatially varying but global average is low
- Less spread in bias in regions with more data
- Higher decadal correlation in regions with more data

# Normalized standard deviation

Does the reconstruction capture the model's variability?

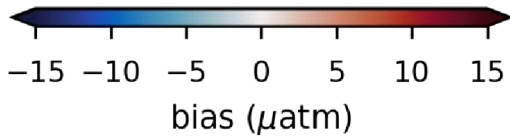
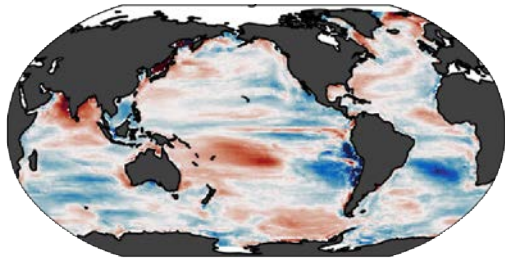


- Overestimates decadal variability in Southern Ocean by about 12%
- Reconciles gap between models and SOM-FFN

# Conclusions

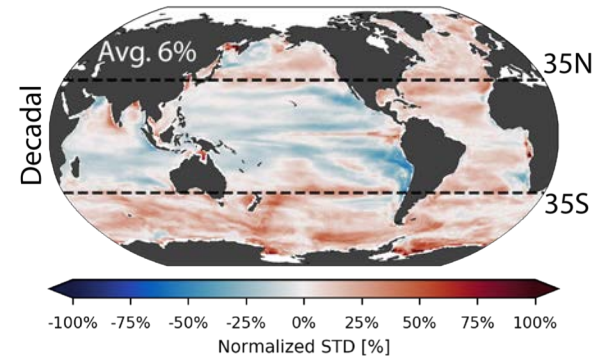
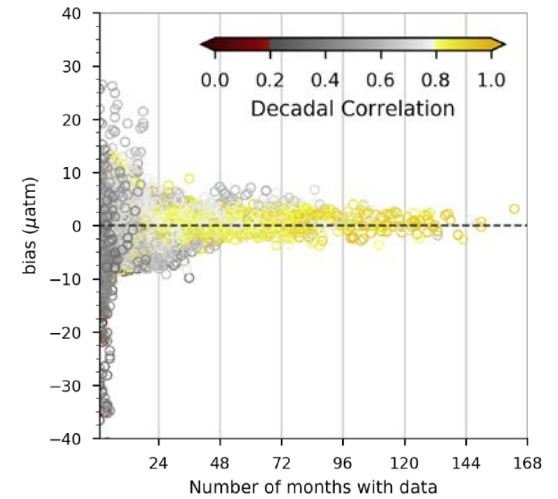
performance dependent on data density

Global avg =  $-0.44 \mu\text{atm}$



Bias is spatially heterogeneous, but negligible on a global scale

Overestimation of decadal variability reconciles the discrepancy with models



**This testbed serves a platform to develop and test new methodologies**



# Acknowledgements

**Galen McKinley**

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**Nikki Lovenduski**

University of Colorado

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**Amanda Fay**

Columbia University / LDEO

**Steve Jones**

University of Bergen

**Christian Rödenbeck**

Max Planck Institute for biogeochemistry

**Thomas Frölicher**

Physics Institute, University of Bern

**Yohei Takano**

Max Planck Institute for Meteorology

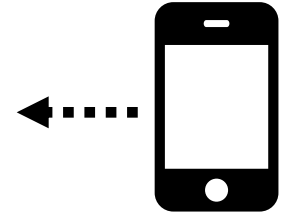
**Sarah Schlunegger**

Princeton University



Lamont-Doherty Earth Observatory  
COLUMBIA UNIVERSITY | EARTH INSTITUTE

Take a picture to  
access the testbed



## Testbed URL

[figshare.com/s/4337ae68dccbcf34e14c](https://figshare.com/s/4337ae68dccbcf34e14c)

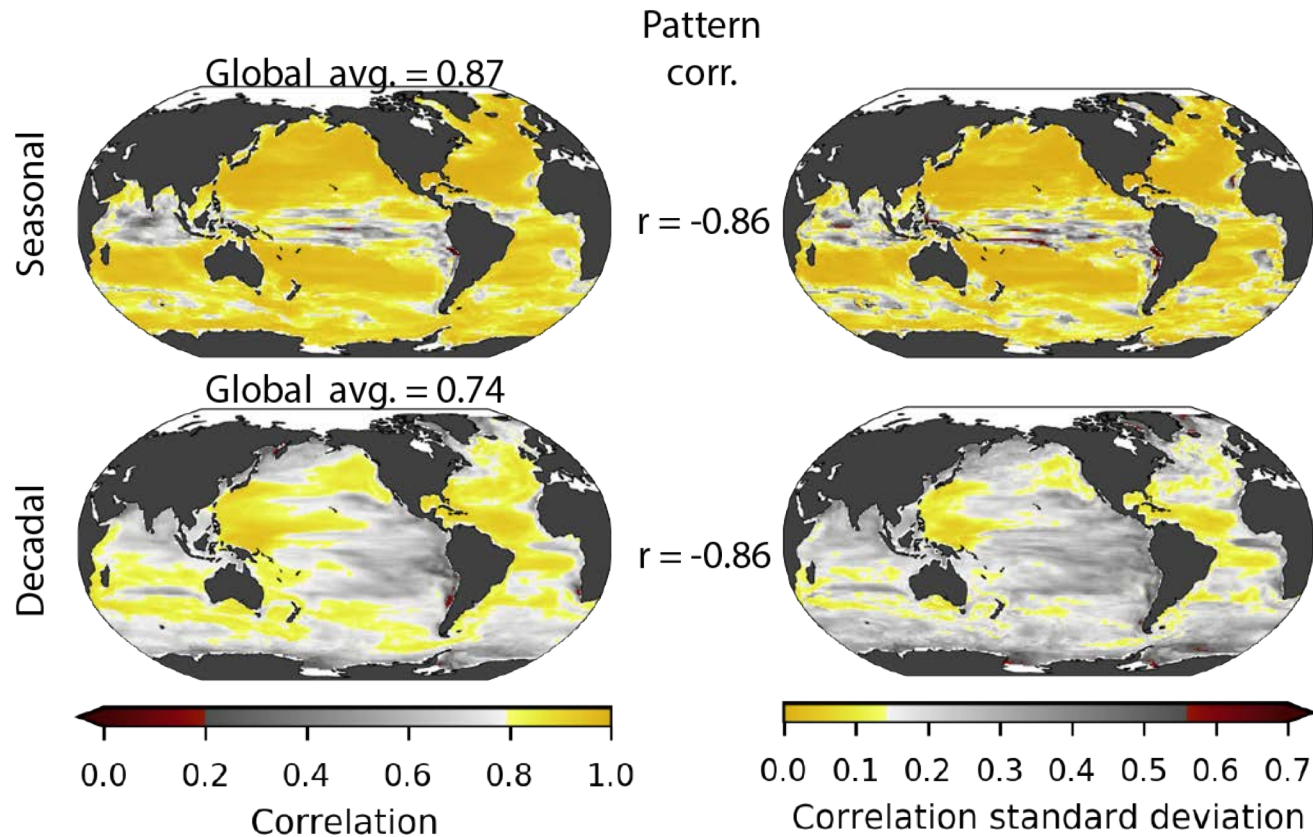
## Email

[gloege@ldeo.columbia.edu](mailto:gloege@ldeo.columbia.edu)

# Extra slides

# Correlation

Is the reconstruction in phase with the model?



- Higher correlations in sub-tropics
- Correlations are consistent across ensemble members

# Calculate air-sea CO<sub>2</sub> exchange

Air-sea CO<sub>2</sub> flux

(relative to atmosphere)

Ice fraction

$$F_{CO_2} = k_w S_{CO_2} (1 - f_{ice}) (pCO_2^{ocn} - pCO_2^{atm})$$

Gas-transfer velocity and solubility

Ocean and atmosphere pCO<sub>2</sub>

- ERA-interim 6-hourly global atmospheric reanalysis used to estimate monthly varying wind-speed covariance
- Calculated air-sea CO<sub>2</sub> exchange following Landschützer et al. 2014

Weiss 1974, Wanninkhof 1992, Sweeney et al. 2007