

# **Isentropic analysis applied to hurricane circulation**

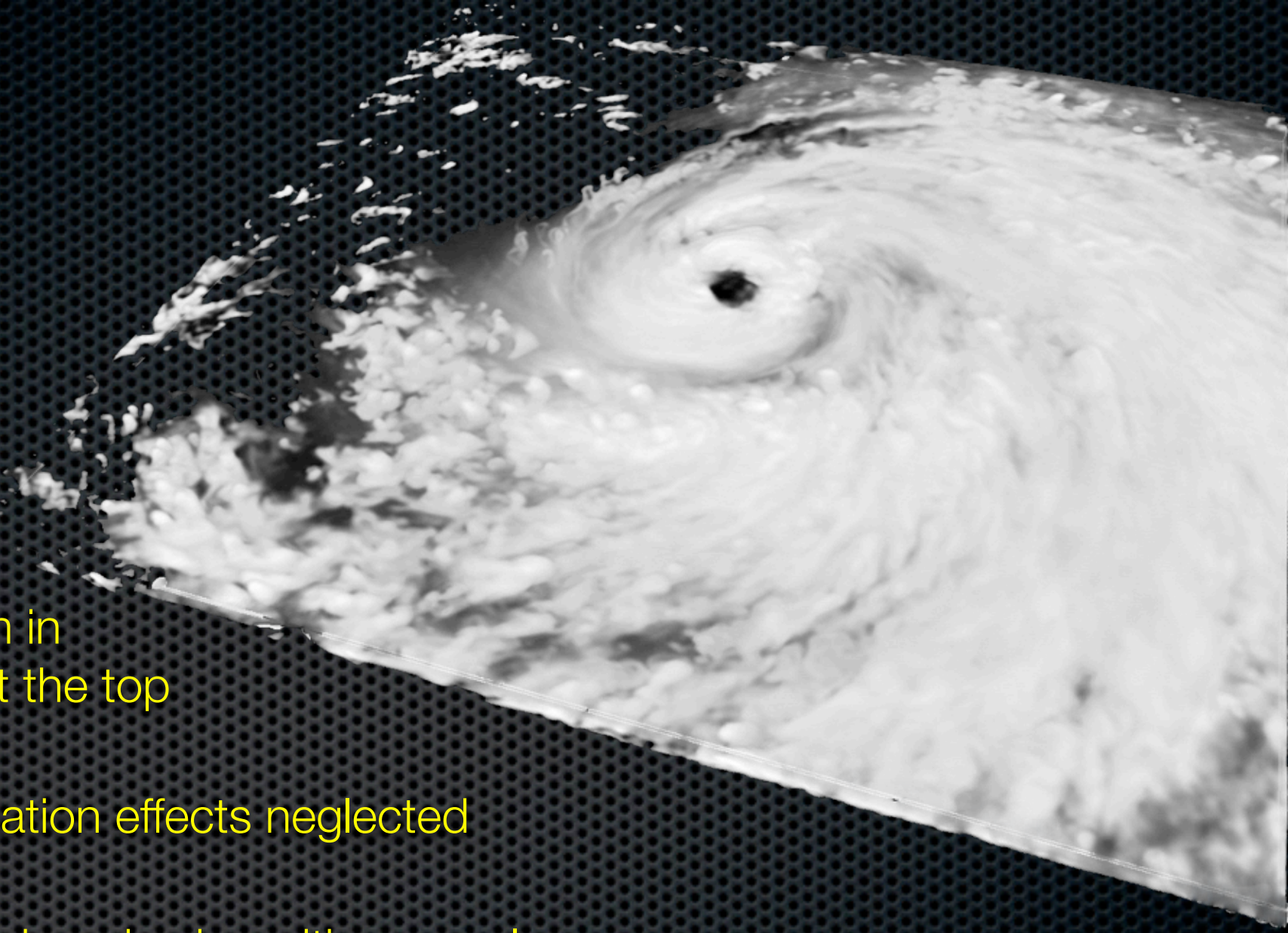
Agnieszka Mrowiec<sup>1</sup>, Olivier Pauluis<sup>2</sup>  
and Fuqing Zhang<sup>3</sup>

<sup>1</sup> Columbia University/NASA GISS, <sup>2</sup> NYU, <sup>3</sup> PSU



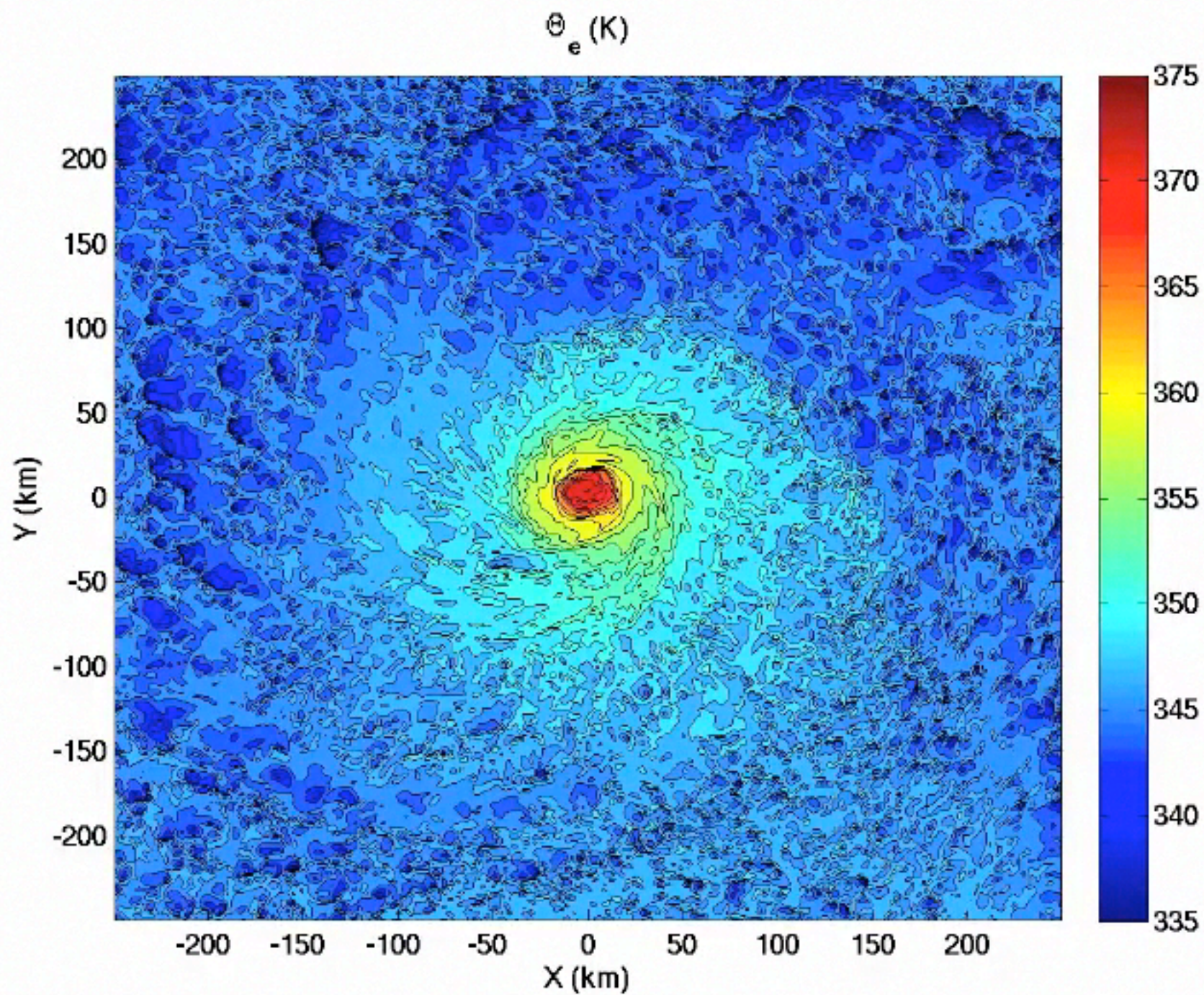
## WRF 2.2 Simulation:

- ✧ domain 1000 km x 1000 km
- ✧ horizontal resolution 1 km
- ✧ 35 levels stretched from 0.6 km in the boundary layer to 3.6 km at the top
- ✧ long-wave and short-wave radiation effects neglected
- ✧ WRF Single-Moment, 6-class microphysics with graupel
- ✧ Yonsei University turbulent fluxes scheme
- ✧ initialized with an axisymmetric vortex at 20°N with an initial radius of 102 km and tangential wind  $v_t = 16$  m/s
- ✧ the temperature and humidity profiles following Jordan(1958) soundings





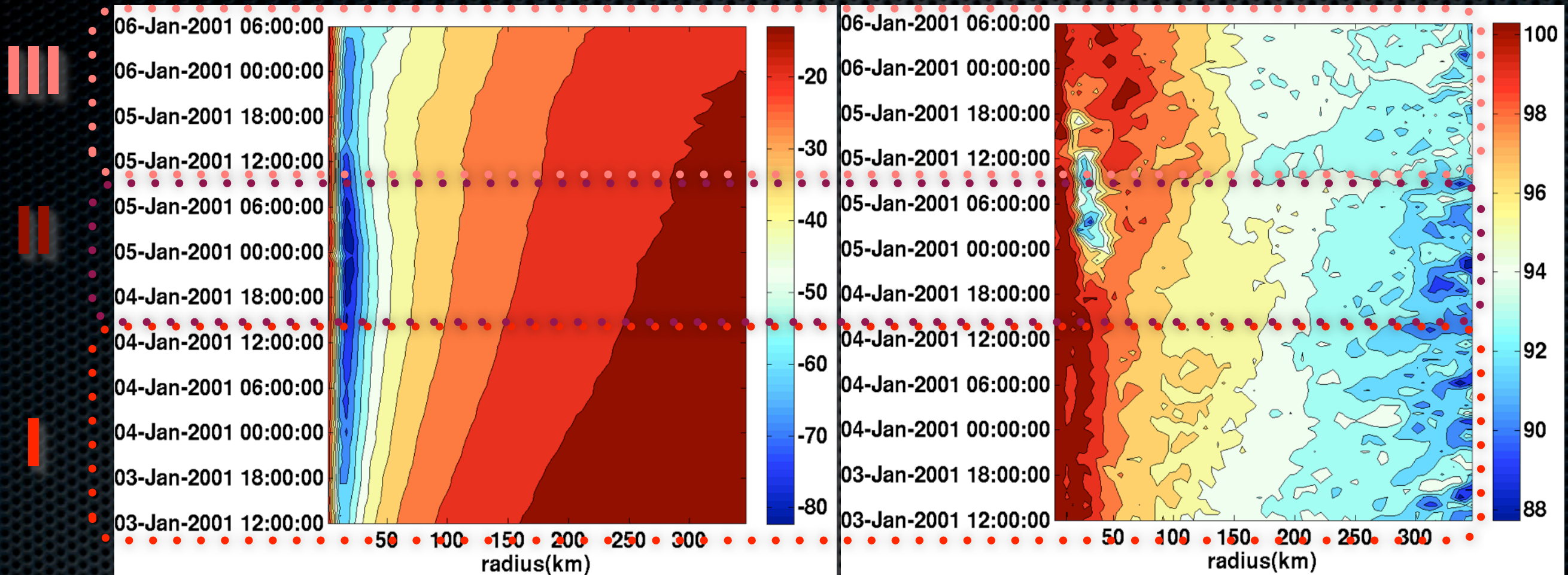
# surface equivalent potential temperature





tangential wind

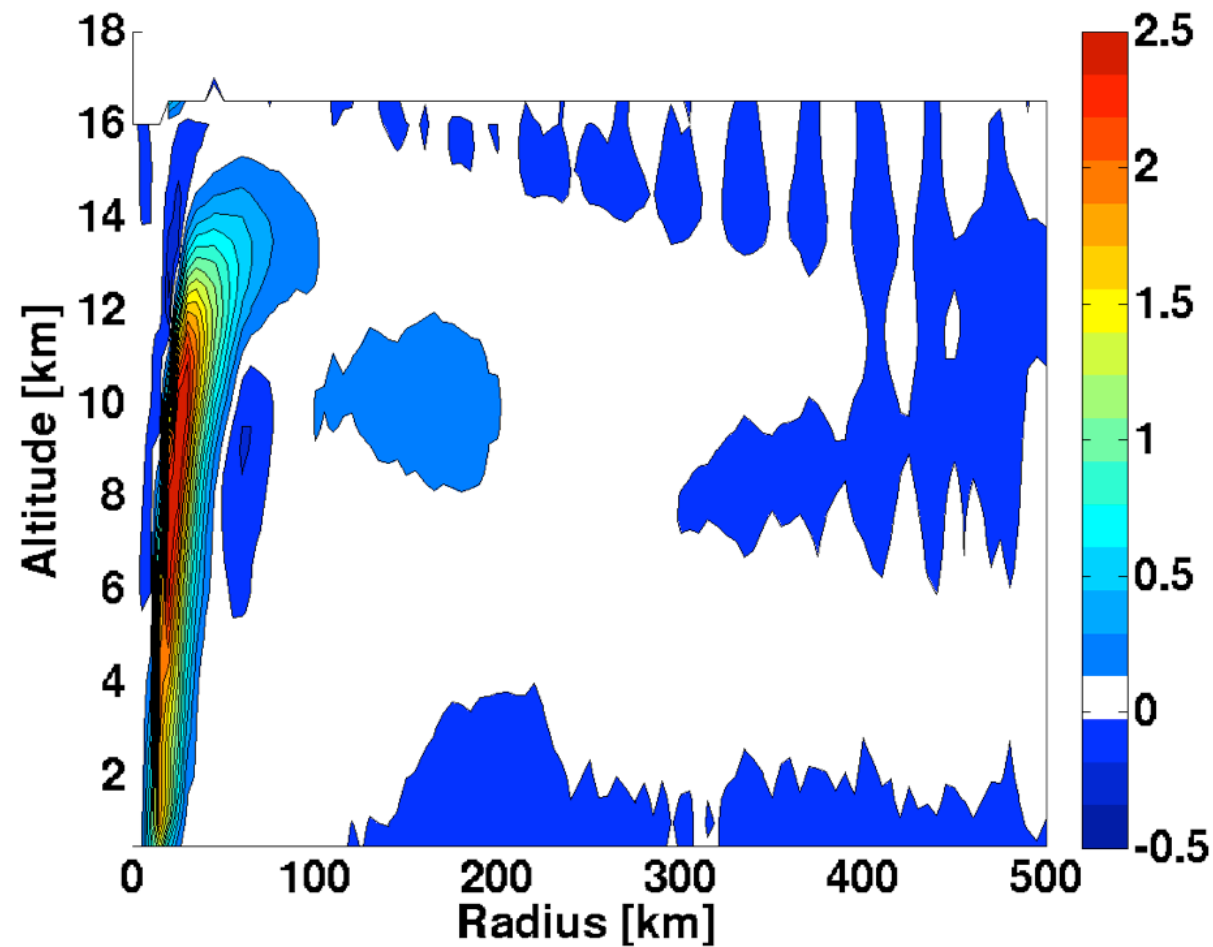
relative humidity



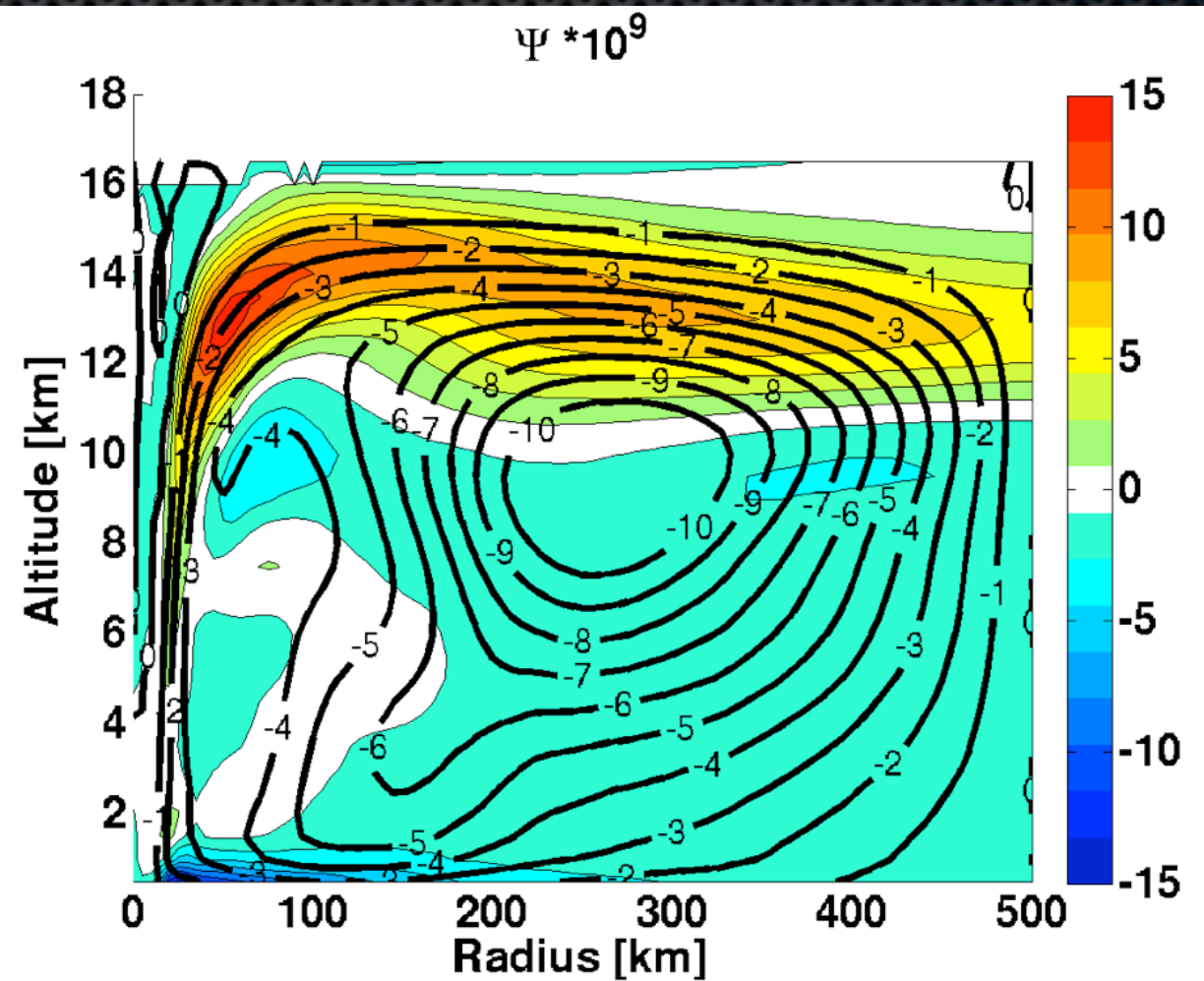


# secondary circulation

vertical velocity



radial velocity  
&  
eulerian streamfunction



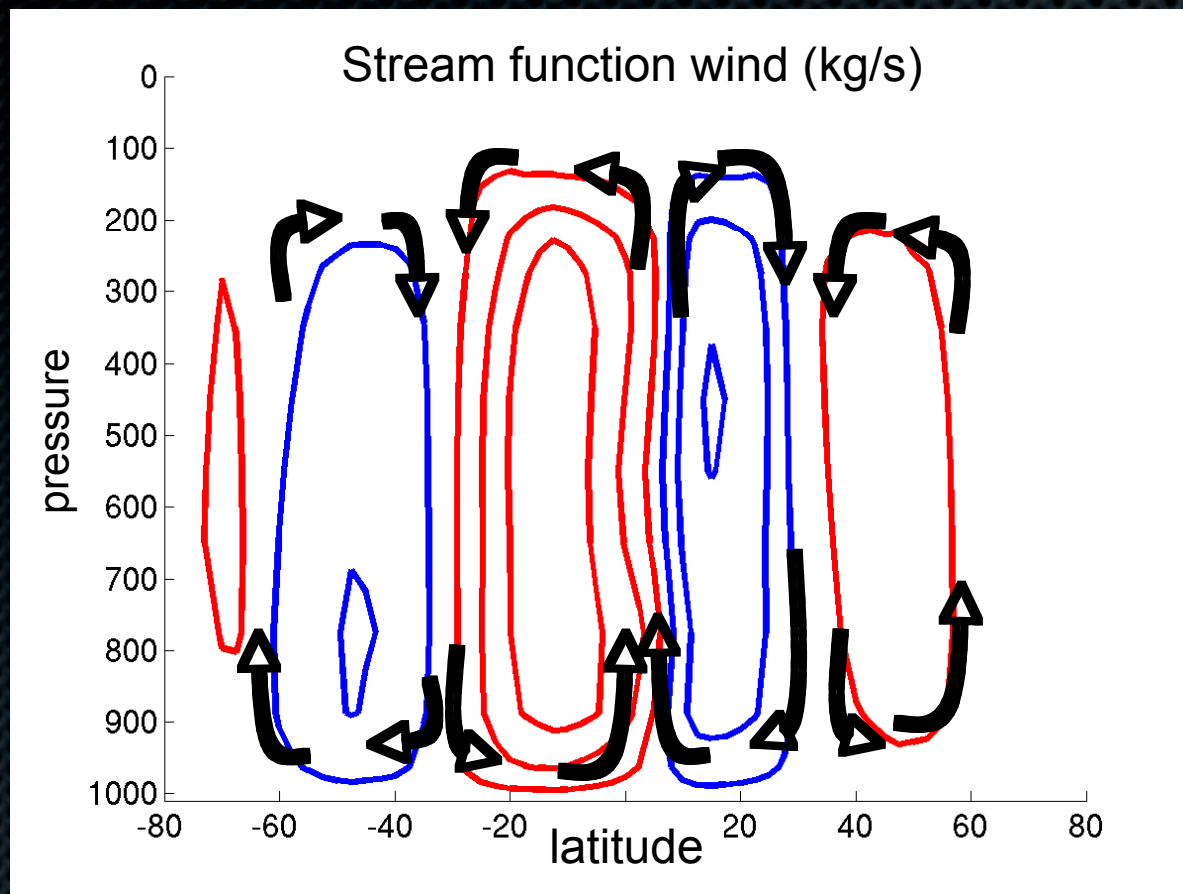


# isentropic circulation

- ✧ the concept of analyzing motions on surfaces of constant entropy dates back to the early days of dynamical meteorology (Rossby 1937)
- ✧ entropy (or equivalent potential temperature) is conserved for reversible adiabatic processes and allows to track parcels even if they experience significant vertical displacement



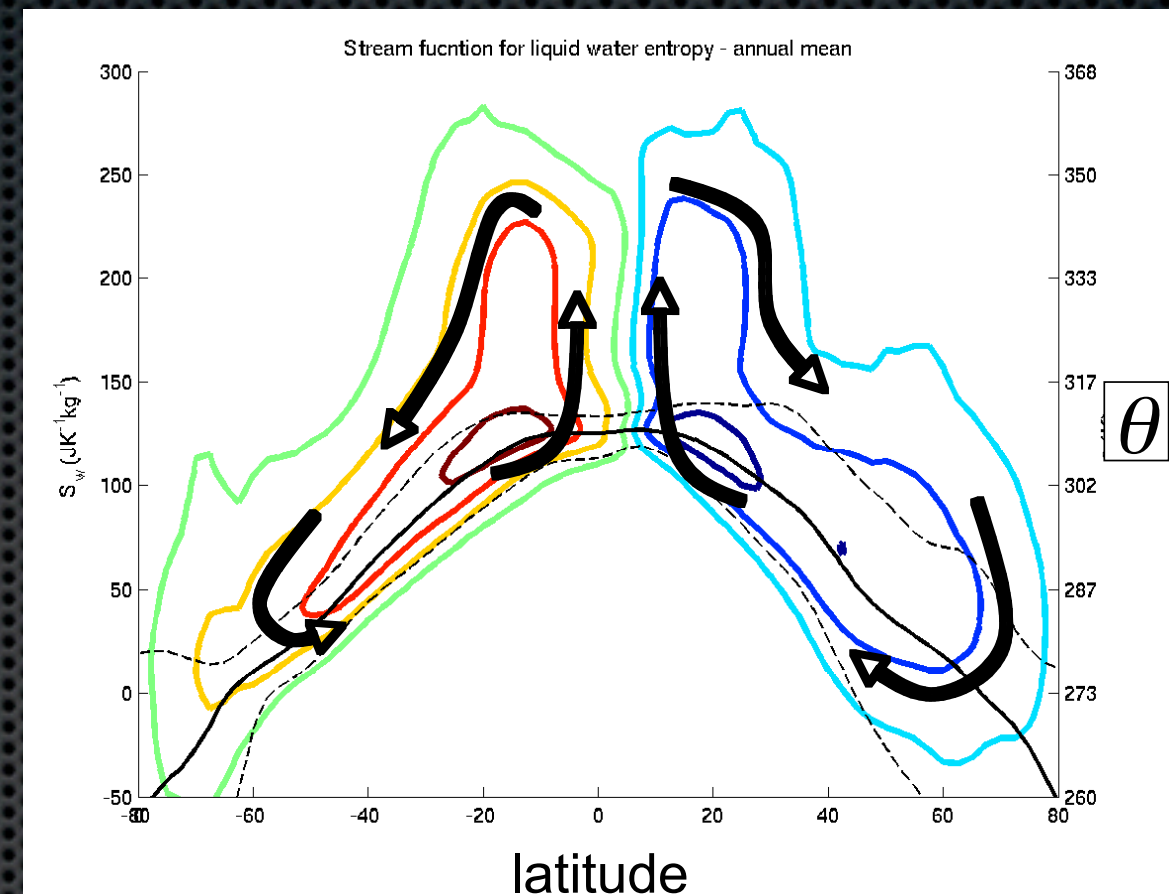
## eulerian-mean circulation



for the meridional circulation a streamfunction may be defined by averaging the velocity at constant pressure, resulting in the well-known three-cell structure

this averages out the 'weather'...

## isentropic circulation



the differences between the eulerian and isentropic circulations show how the choice of the coordinate system for a turbulent flow can make it possible to include or exclude different aspects of the eddy transport into the circulation



# isentropic surfaces

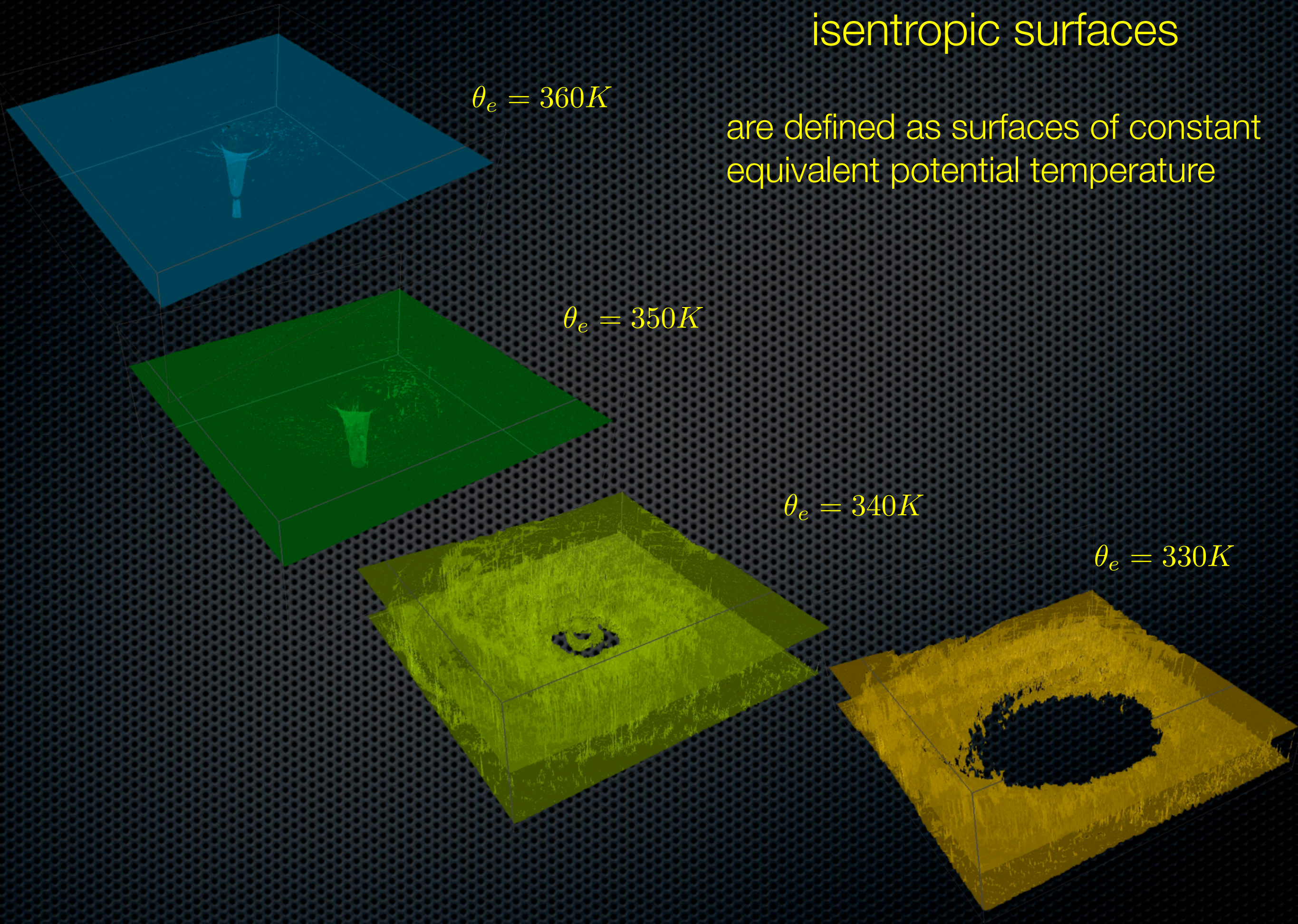
are defined as surfaces of constant equivalent potential temperature

$$\theta_e = 360K$$

$$\theta_e = 350K$$

$$\theta_e = 340K$$

$$\theta_e = 330K$$





# isentropic analysis

we introduce **isentropic averaging**, where we replace both horizontal coordinates  $(x, y)$  by  $\Theta_e$ . In practice the properties of air parcels are averaged over finite size bins of equivalent potential temperature.

$$\langle f(\theta_e, z, t) \rangle = \frac{1}{L^2} \iint f(x, y, z, t) \delta(\theta_{e0} - \theta_e(x, y, z, t)) dx dy$$

the time mean isentropic **mass flux** may be defined as:

$$M(\theta_e, z) = \langle \rho w \rangle (z, \theta_e)$$

the isentropic **streamfunction**:

$$\overline{\Psi}(z, \theta_e) = \int_{\theta_{e,min}}^{\theta_e} M(\theta'_e, z) d\theta'_e.$$



mass conservation:

$$\frac{\partial \langle \rho \rangle}{\partial t} + \frac{\partial \langle \rho w \rangle}{\partial z} + \frac{\partial \langle \rho \theta_e \rangle}{\partial \theta_e} = 0$$

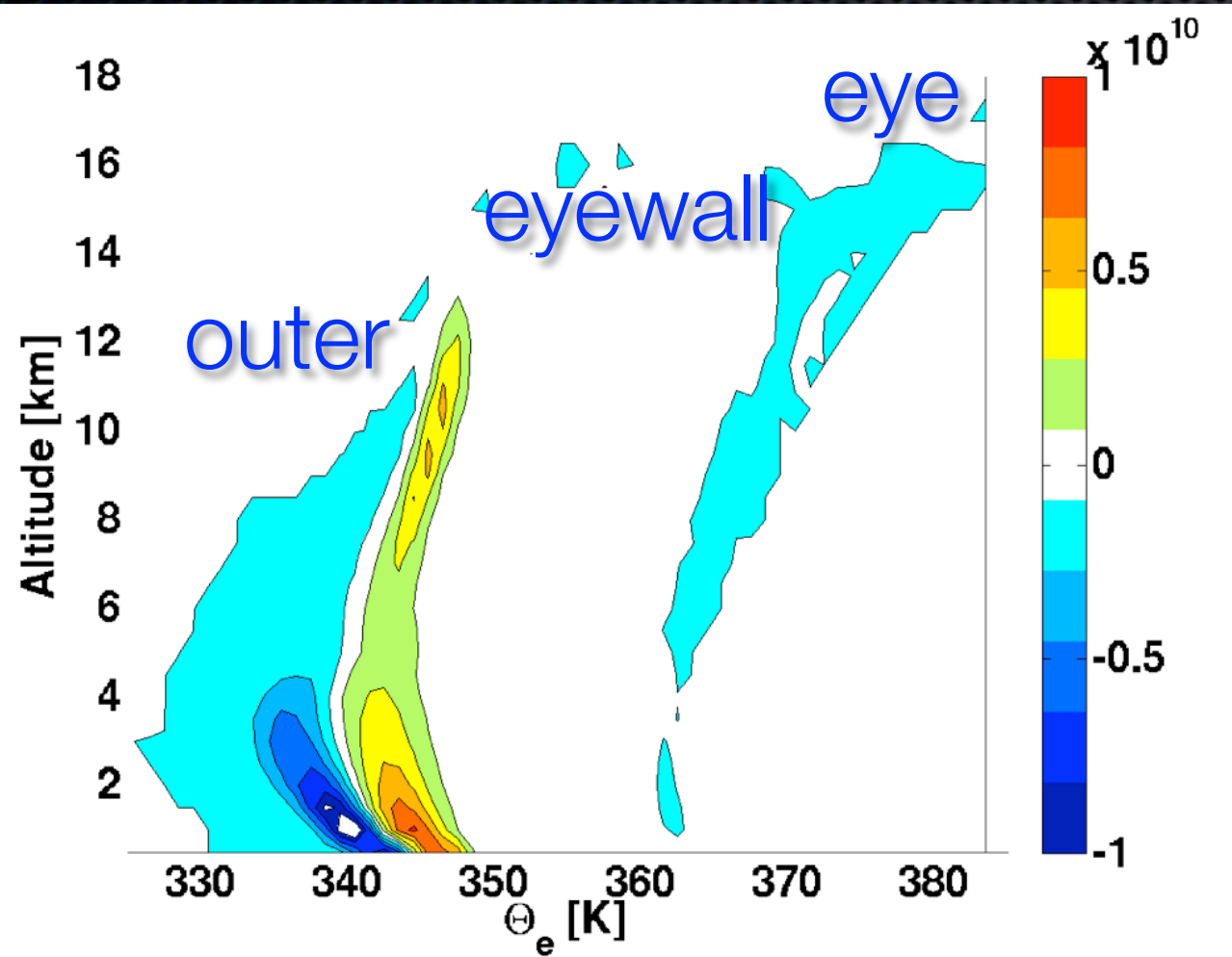
for a statistically steady case, this means that the mean trajectories are parallel to the streamlines

$$\begin{aligned} \langle \rho w \rangle &= \frac{\partial \Psi}{\partial \theta_e} \\ \langle \rho \theta_e \rangle &= -\frac{\partial \Psi}{\partial z} \end{aligned}$$

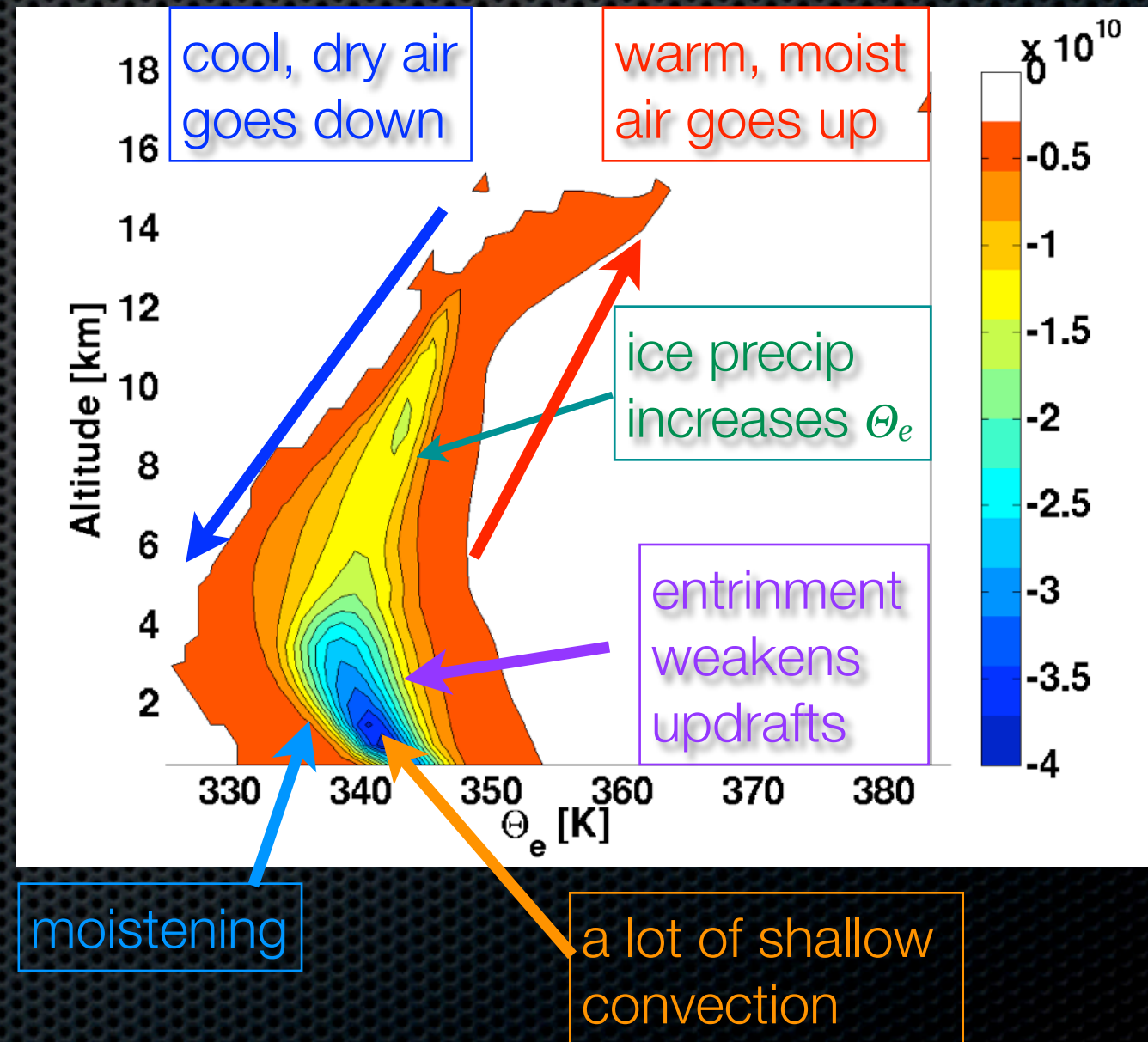
and the diabatic tendency can be directly computed from the streamfunction.



## isentropic mass flux



## isentropic streamfunction

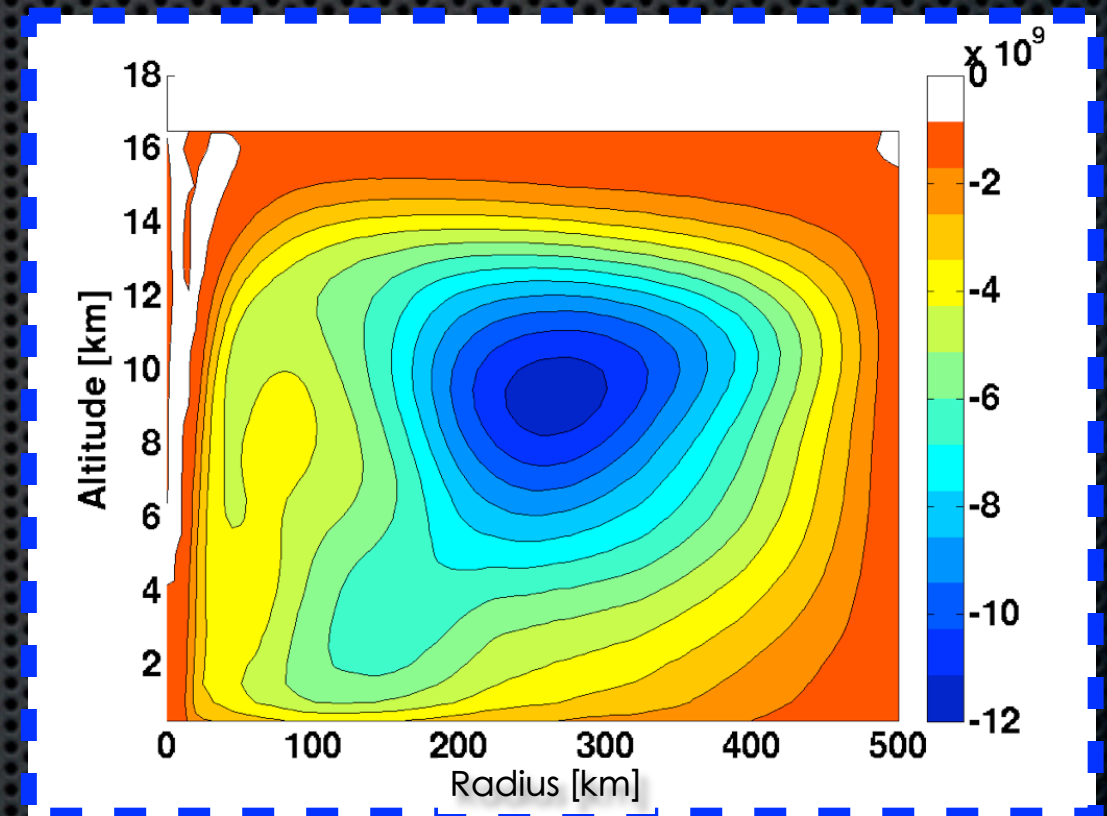
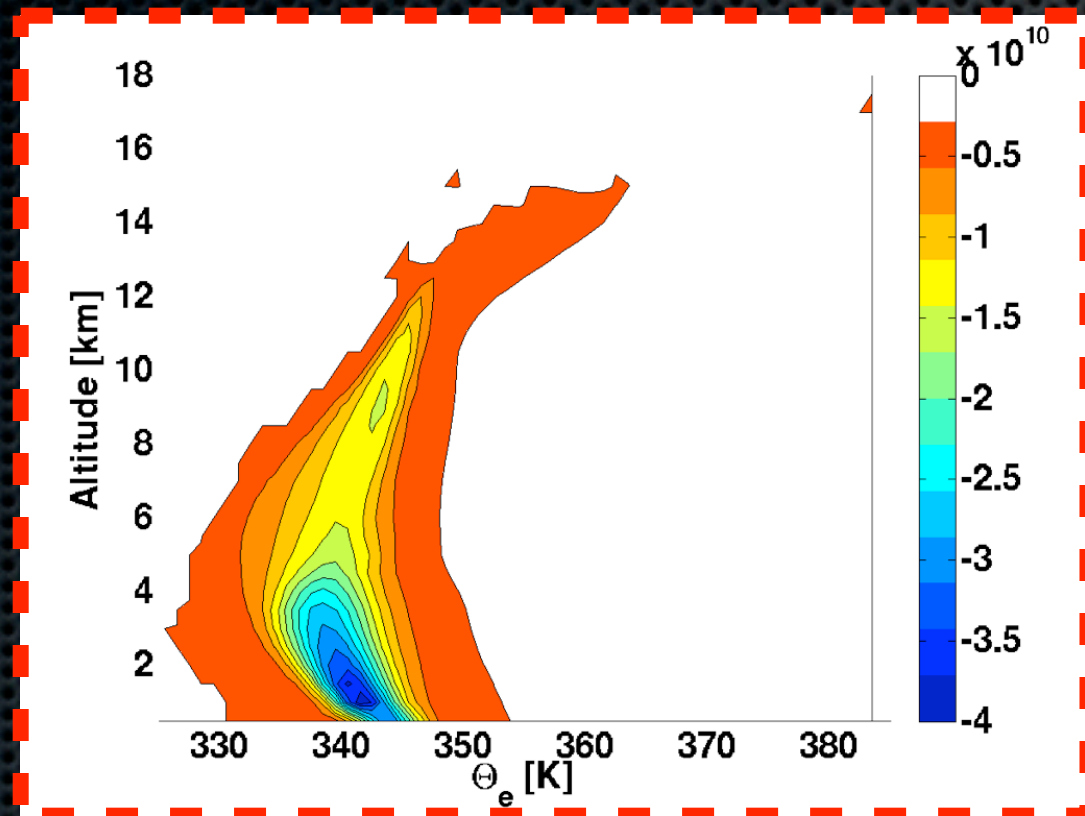




isentropic streamfunction

eulerian streamfunction

$$\Psi_{\theta_e}(\theta_{e0}, z, t) = \int_0^{L_x} \int_0^{L_y} \rho w H(\theta_{e0} - \theta_e(x, y, z, t)) dx dy.$$

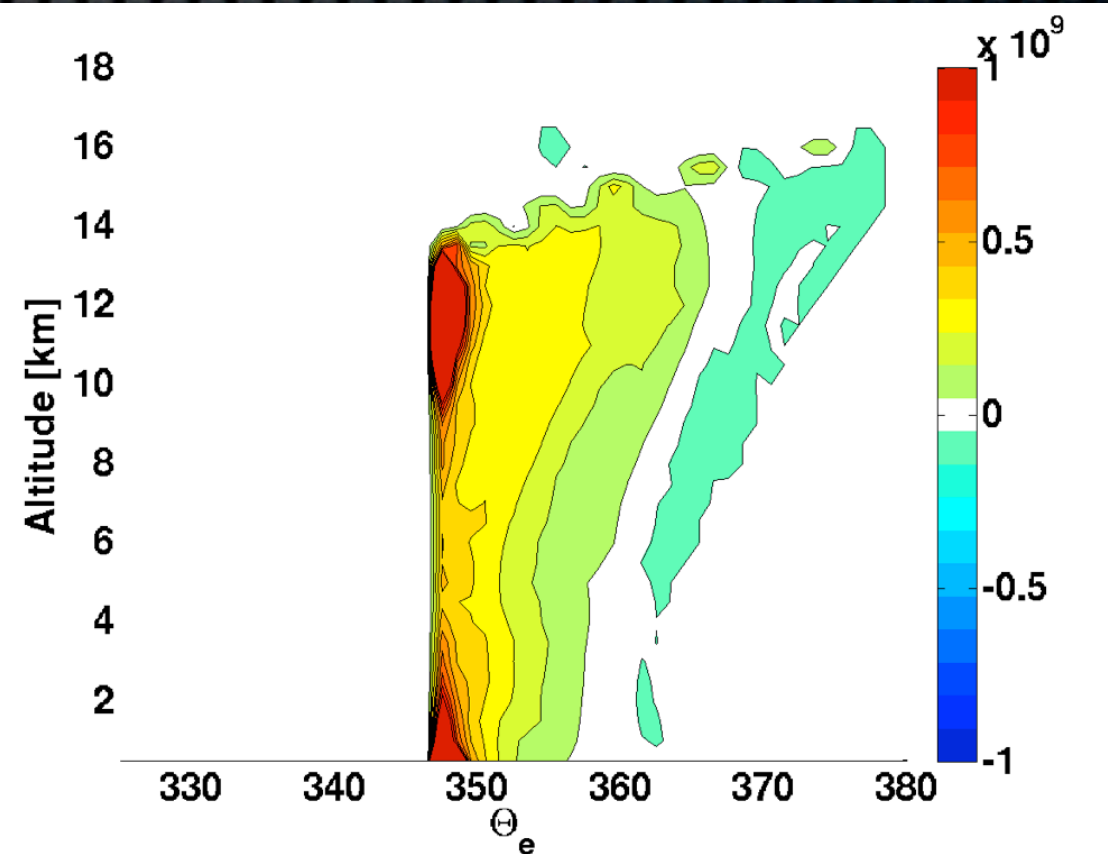
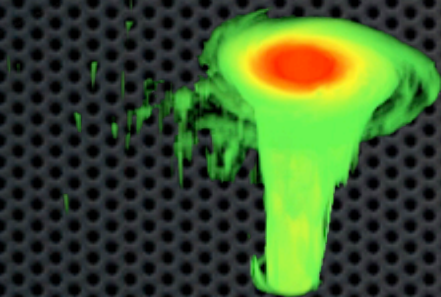
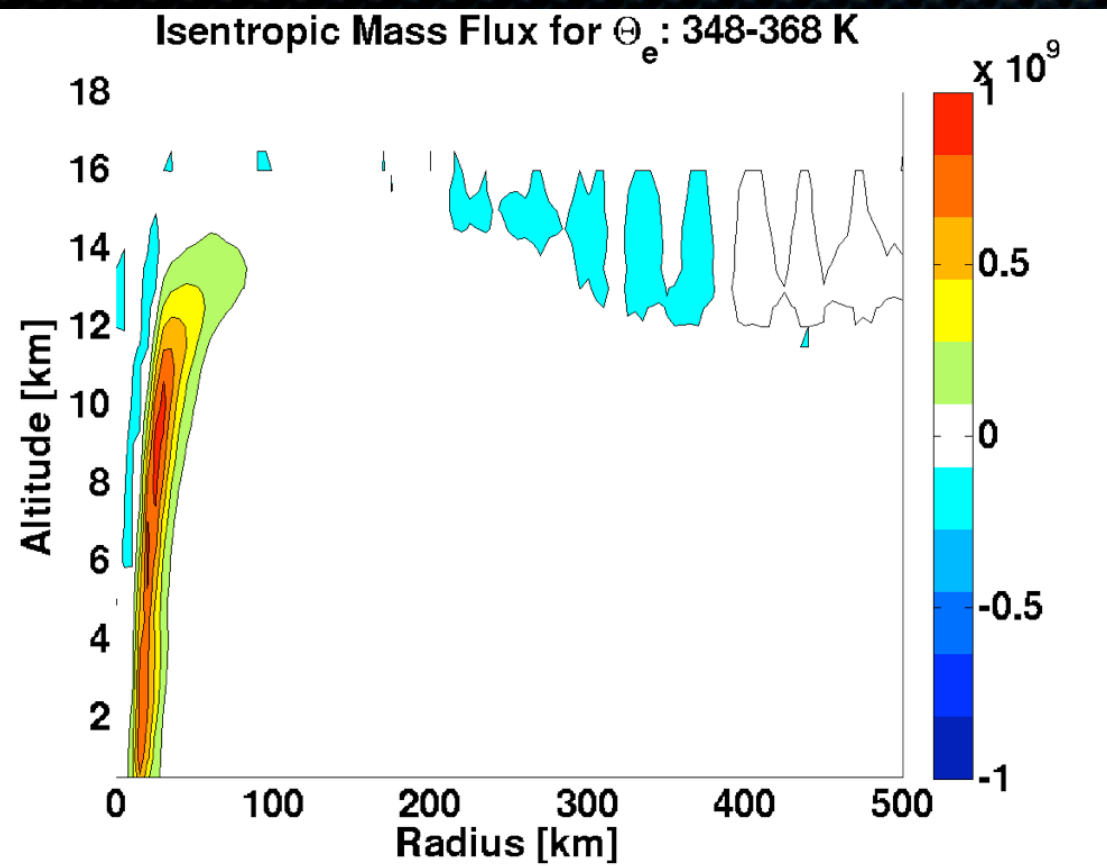


$$\Psi_R(r_0, z, t) = \int_0^{L_x} \int_0^{L_y} \rho w H(r_0 - r(x, y, z, t)) dx dy$$



scale separation: mass flux

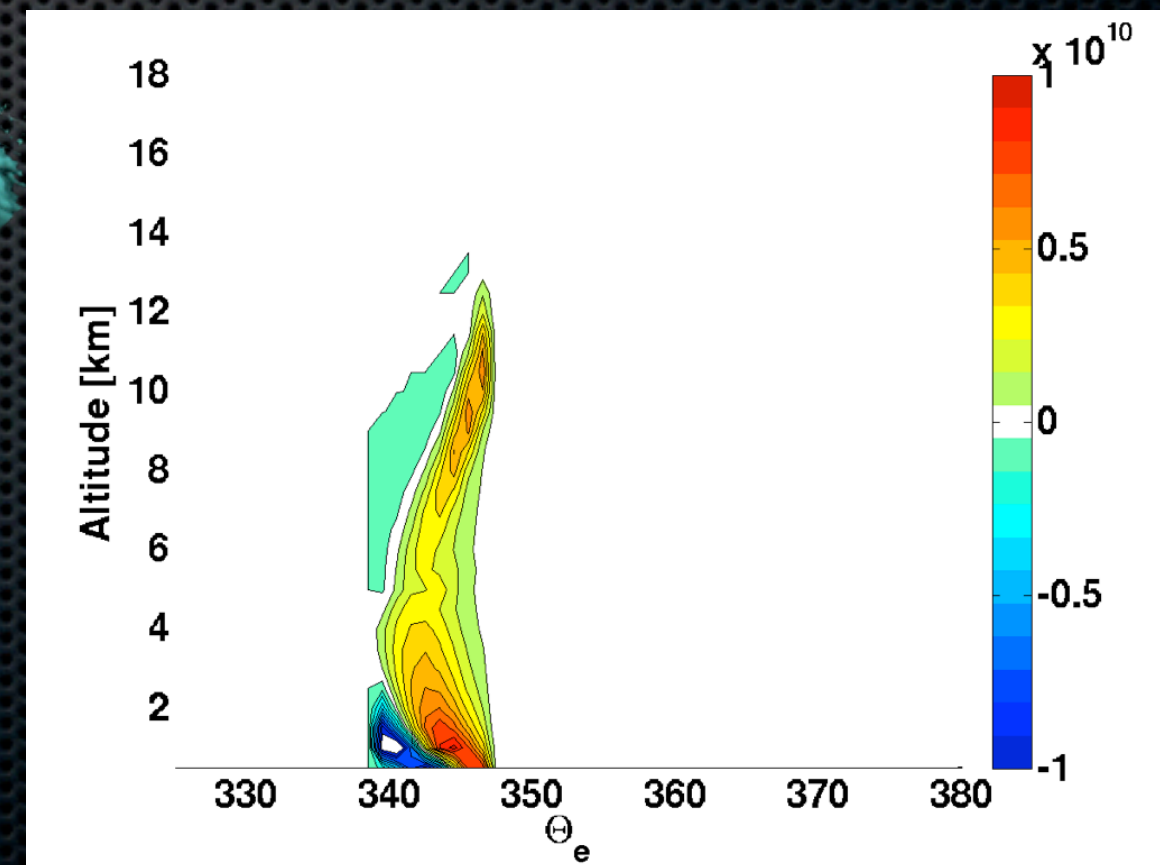
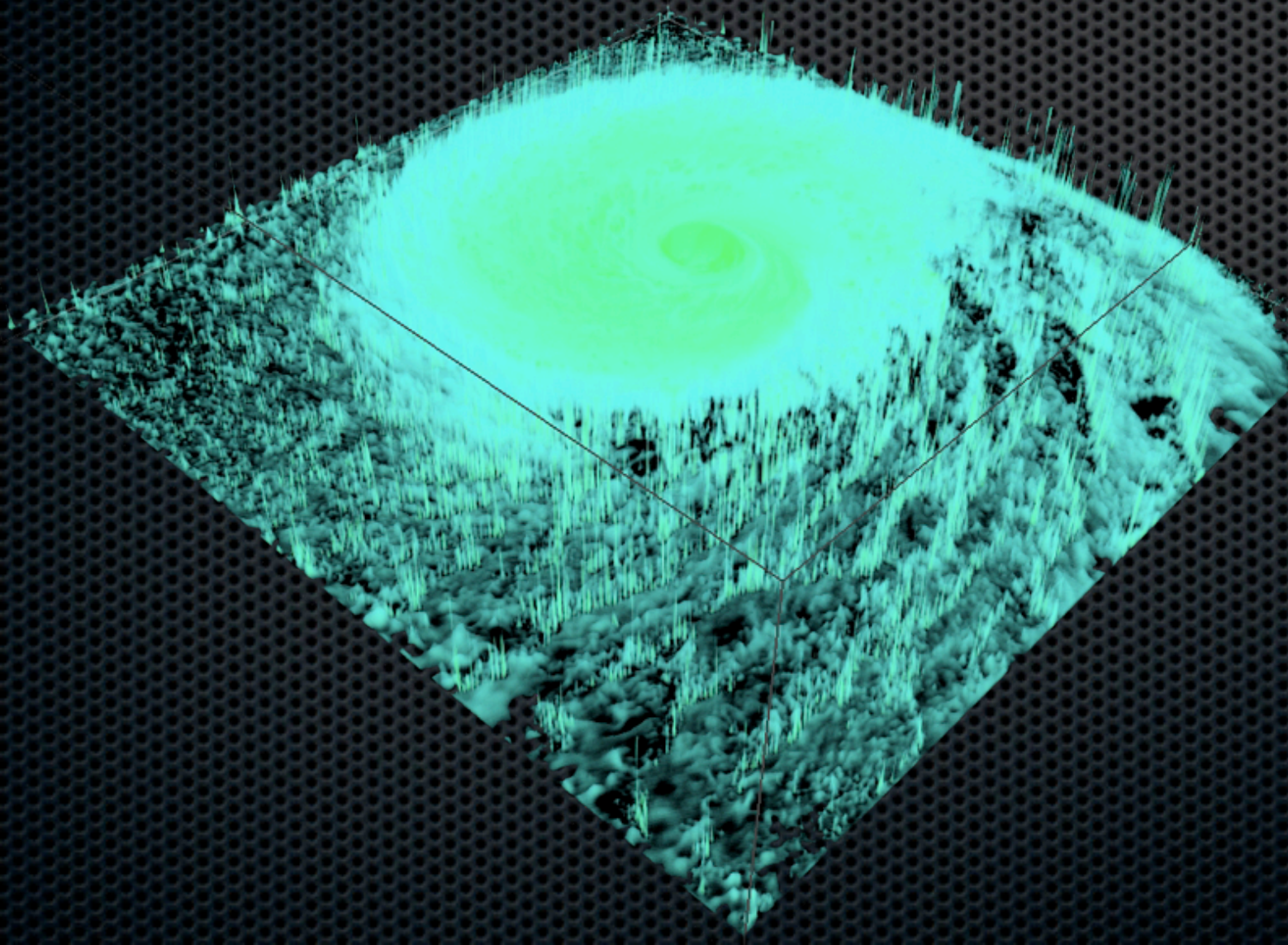
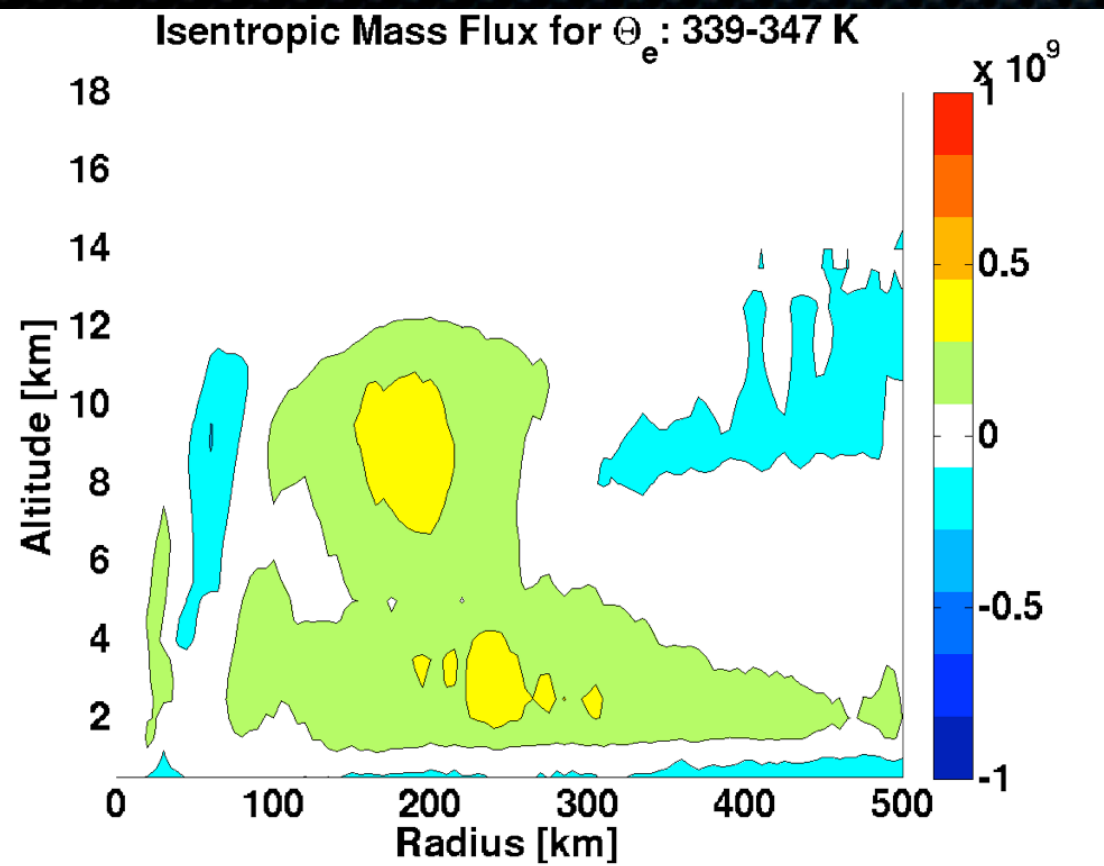
$$348K > \theta_e > 368K$$





scale separation: mass flux

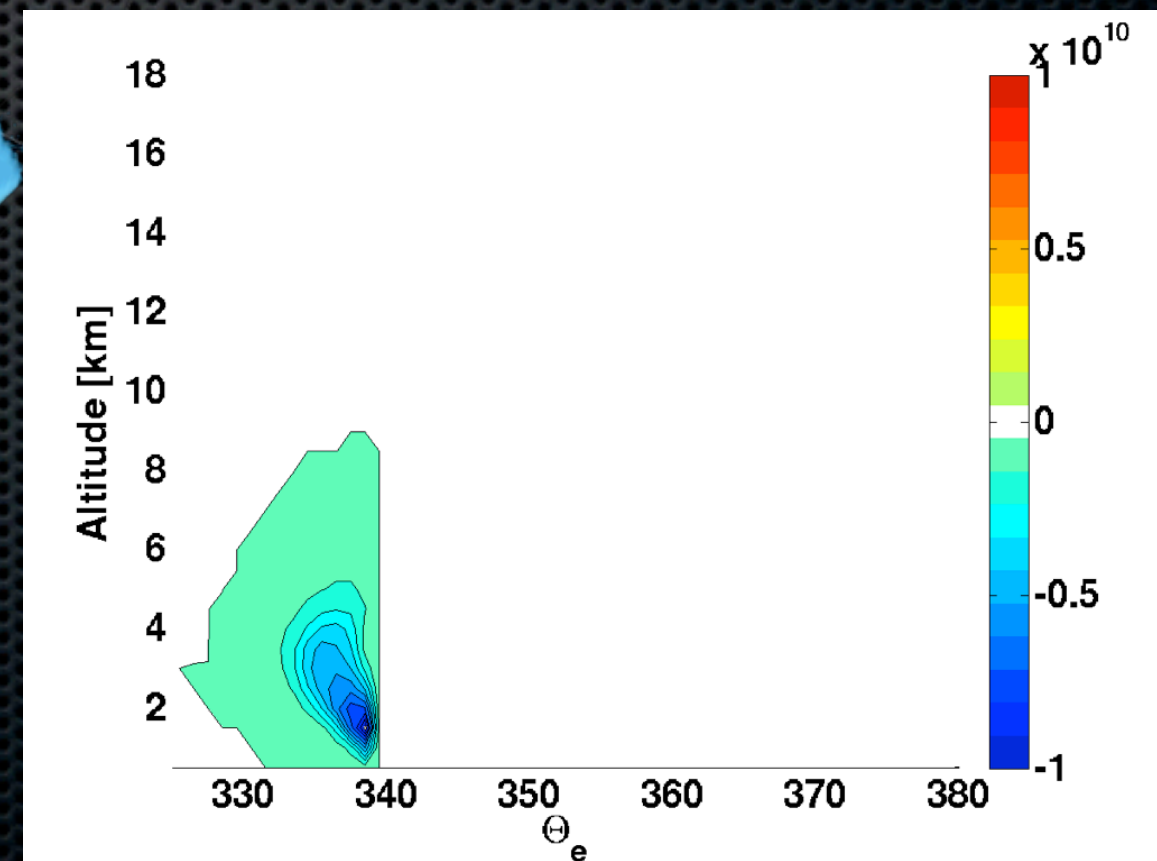
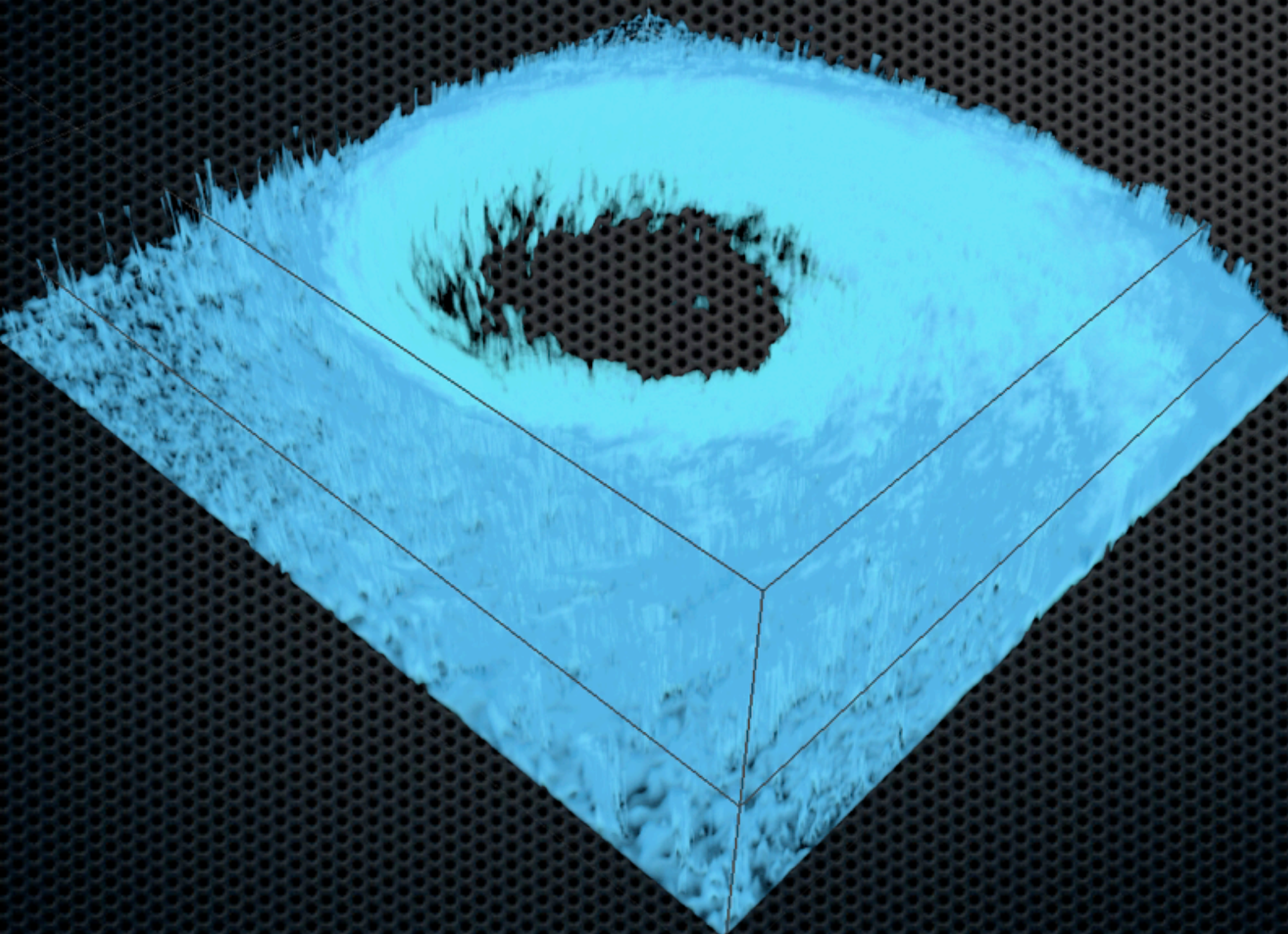
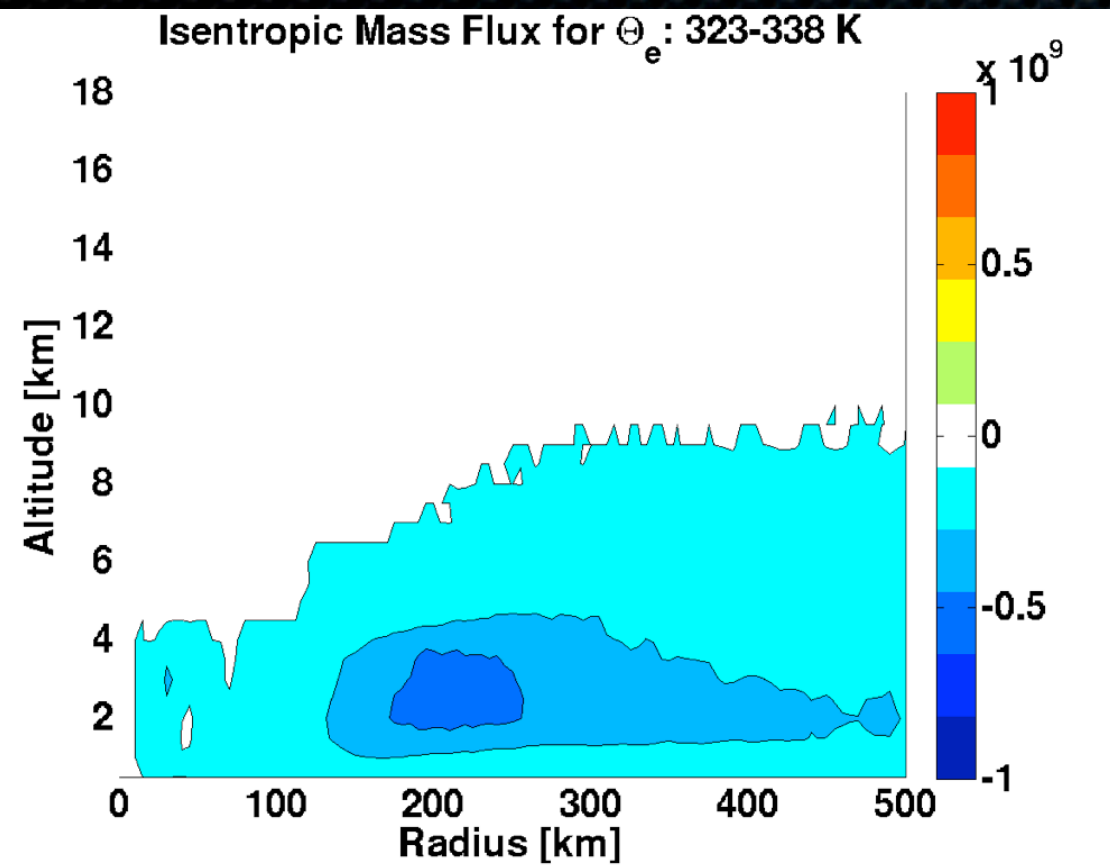
$$339K > \theta_e > 347K$$





scale separation: mass flux

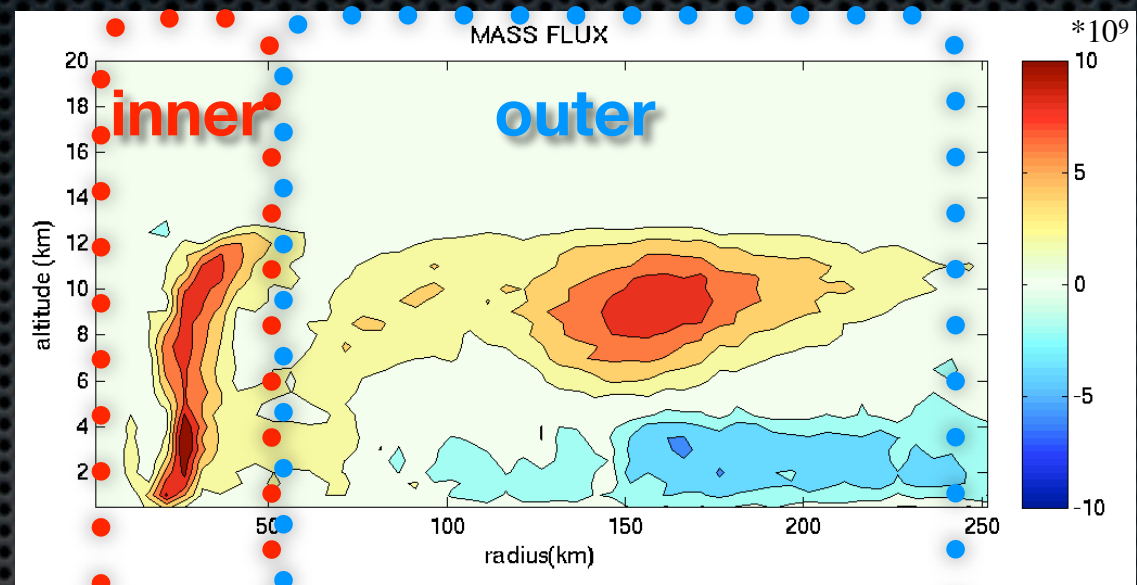
$$323K > \theta_e > 338K$$



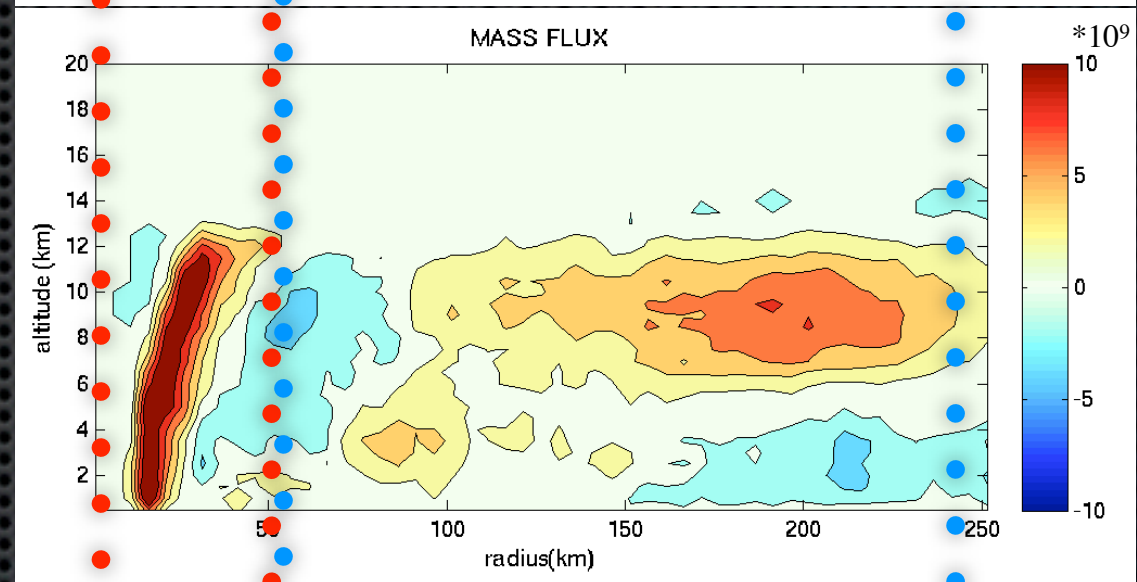


# transient structure: mass flux

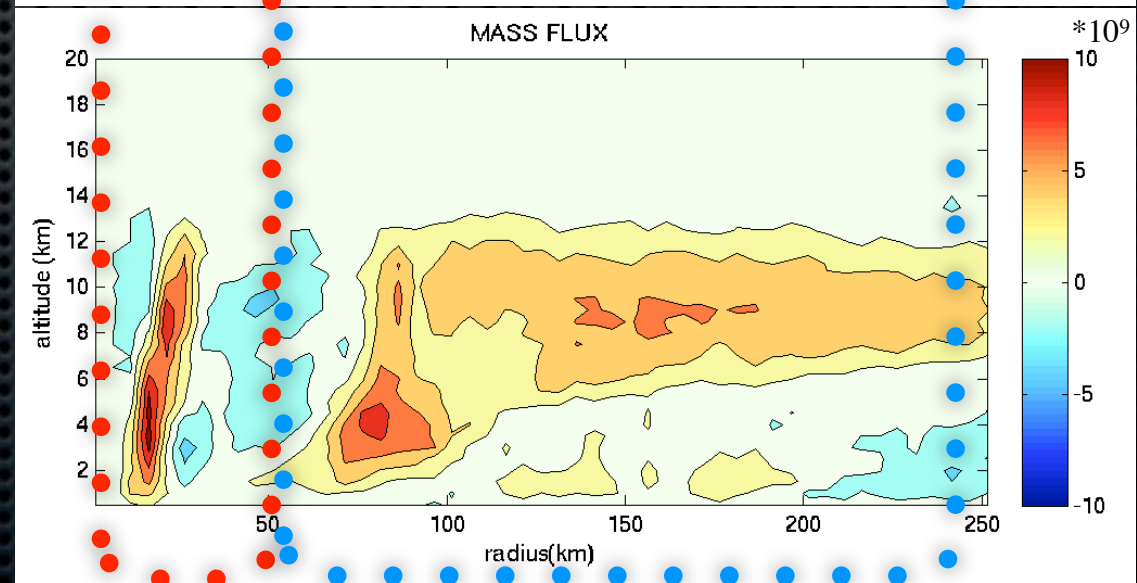
I - intensification



II - peak intensity



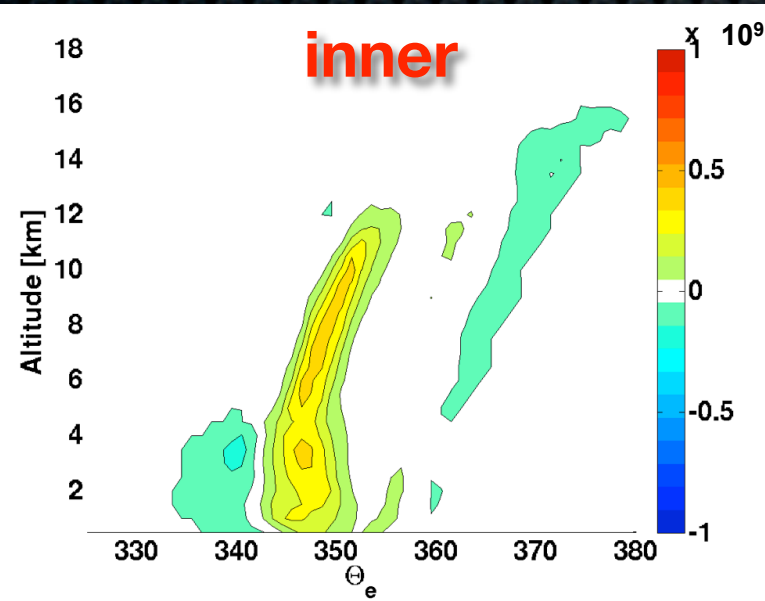
III - weakening



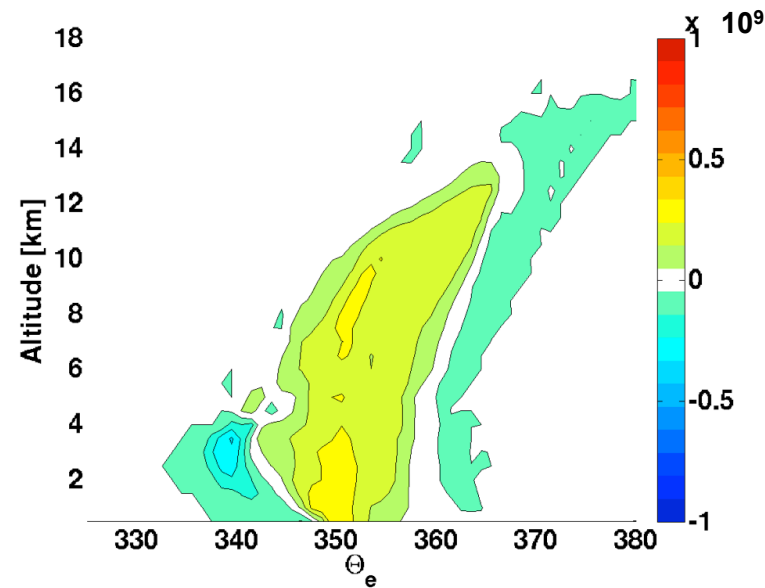


# transient structure: isentropic mass flux

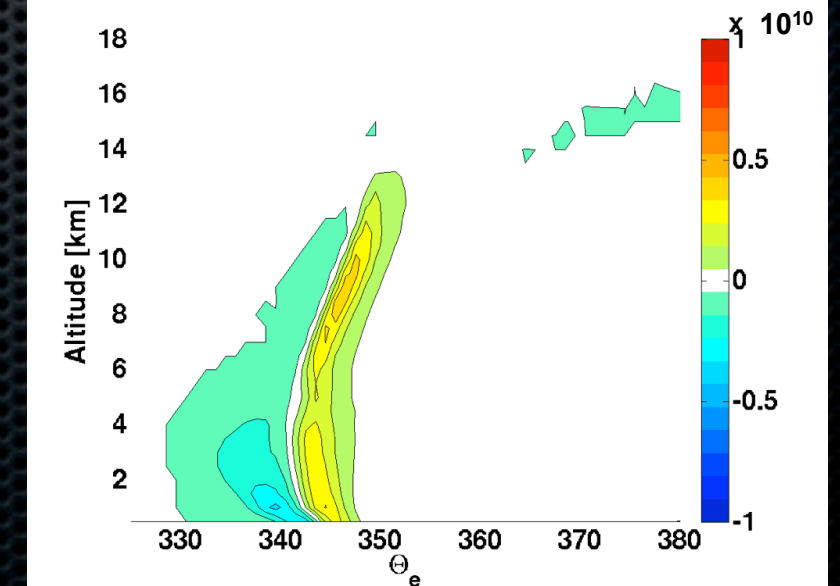
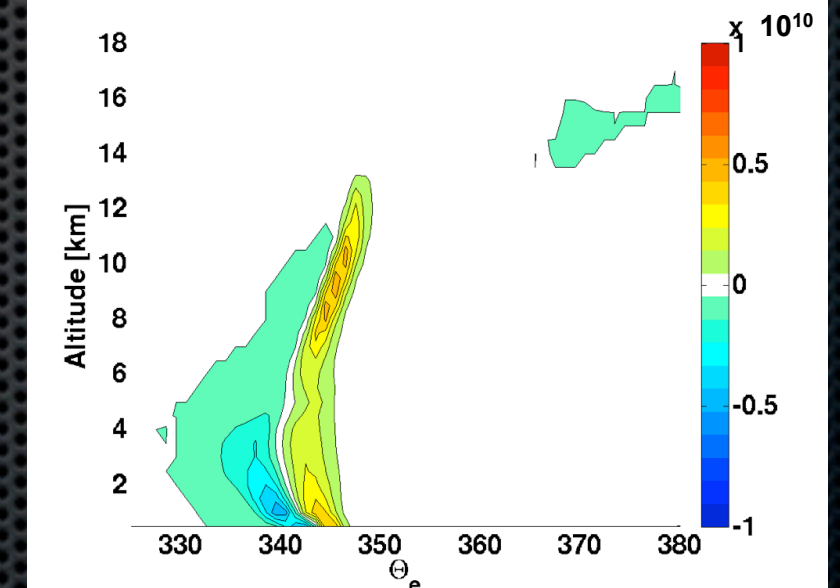
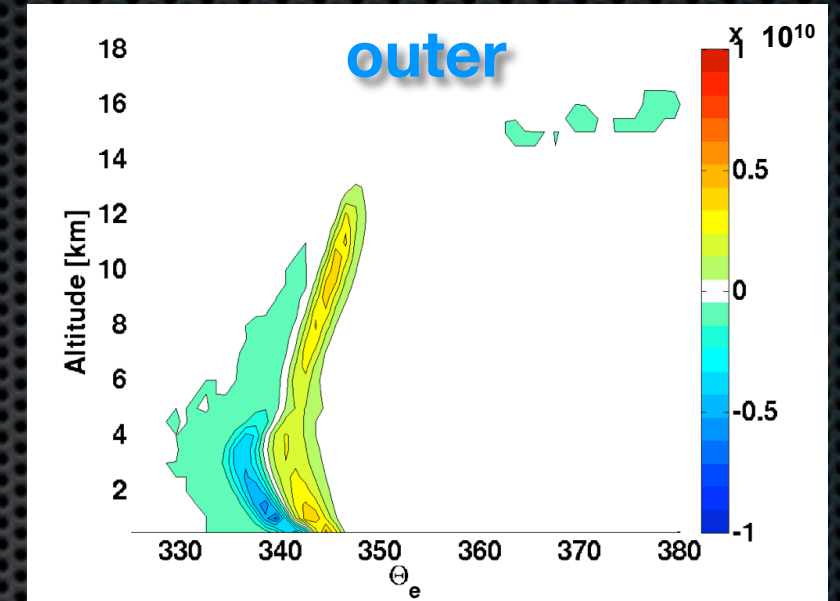
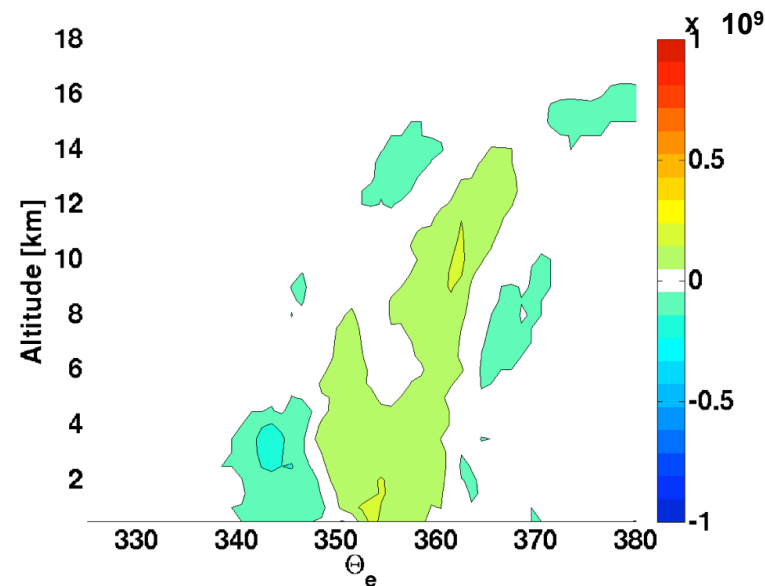
I - intensification



II - peak intensity



III - weakening





# summary

- ✦ the mass transported by the eye is much smaller than the mass transported by the outer region in the hurricane
- ✦ it is possible to separate the inner flow (eye + eyewall) from the outer flow based on equivalent potential temperature
- ✦ It can be used to diagnose many aspects of convection, such as diabatic heating, entrainment or downdrafts and to identify different convective regimes.
- ✦ we can study properties of thermodynamically similar air parcels and separate between warm, moist updrafts and cool drier downdrafts
- ✦ we can analyze dynamics and thermodynamics relationship in hurricanes and other convective systems
- ✦ isentropic analysis of convective motions can be used as a basis for comparison between cloud resolving models