



# Dynamical Decomposition of Multiscale Oceanic Motions

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## INTRODUCTION

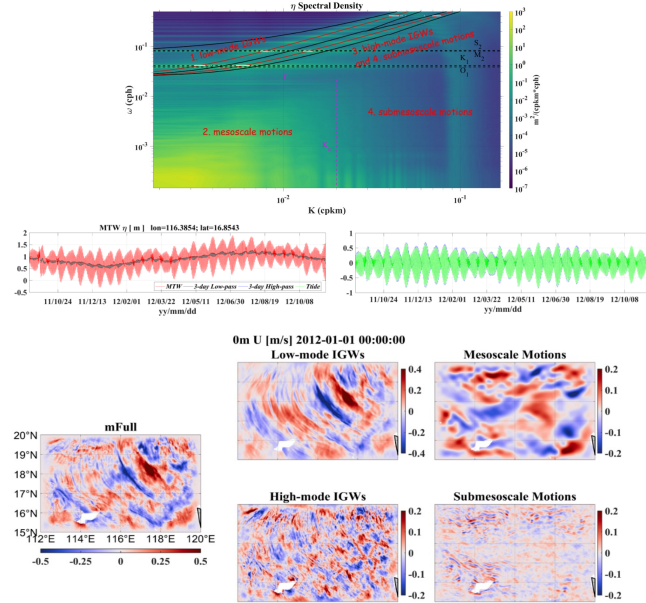
- A long-standing challenge in dynamical oceanography is to distinguish various dynamical regimes of multiscale oceanic motions
- Conventional approaches of the multi-regime disentanglement focus on time-scale or space-scale decompositions
- This study has established two *dynamical approaches* to disentangle vortical (PV-bearing) and wavy (PV-less) motions

## DYNAMICAL DECOMPOSITION #1

*decomposing physical variables into six regimes*

### Dynamical properties

- Large-scale currents and barotropic tides have the largest horizontal scales but contrasting frequencies
- Low-mode IGWs are constrained by dispersion relations
- Mesoscale flows are of relatively low frequency and with horizontal scales above the first baroclinic deformation radius
- The intrinsic frequency of high-mode IGWs (submesoscale flows) is above (well below) the inertial frequency



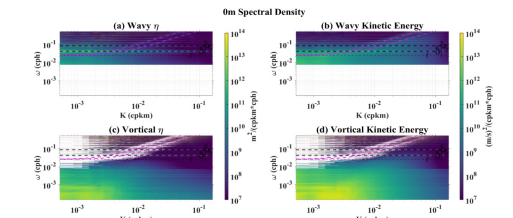
## DYNAMICAL DECOMPOSITION #2

*decomposing variables & equations into vortical & wavy motions*

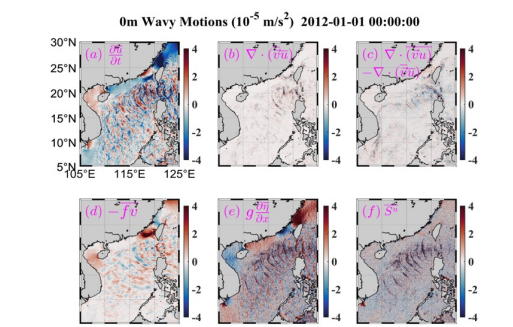
$$\frac{\partial \zeta}{\partial t} + U \frac{\partial \zeta}{\partial x} + V \frac{\partial \zeta}{\partial y} + f_{min} \frac{f \zeta}{f_{min}} = 0$$

$$i\omega \zeta + iUk\zeta + iVl\zeta + f_{min} \frac{f \zeta}{f_{min}} = i\Omega \zeta + f_{min} \frac{f \zeta}{f_{min}} = 0$$

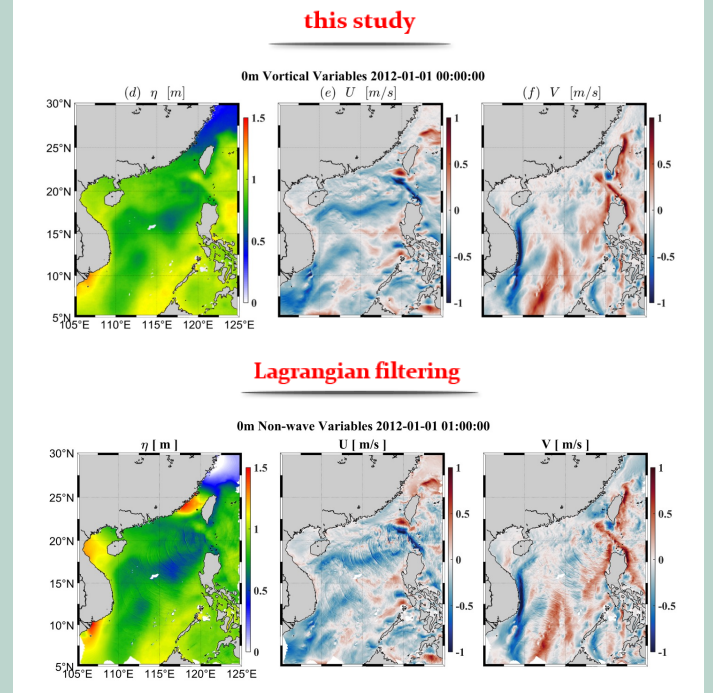
$$\begin{cases} \Omega = 0 & \text{vortical mode} \\ \Omega = \pm \sqrt{f_0^2 + c^2 K^2} & \text{wavy mode} \end{cases} \quad \widehat{M}_\omega(k,l,\omega) = \begin{cases} 1, & \text{when } |\zeta| < \frac{f \zeta}{f_{min}} \text{ at } (k,l,\omega) \\ 0, & \text{when } |\zeta| > \frac{f \zeta}{f_{min}} \text{ at } (k,l,\omega) \end{cases} \quad \begin{cases} A_\omega = M_\omega * A \\ A_\omega = M_\omega * A \end{cases}$$



$$\frac{\partial \bar{u}}{\partial t} + \frac{\partial \bar{u}\bar{u}}{\partial x} + \frac{\partial \bar{v}\bar{u}}{\partial y} + \frac{\partial \bar{w}\bar{u}}{\partial z} - \bar{f}v = -g \frac{\partial \bar{\eta}}{\partial x} + \bar{res}_x$$



## COMPARISON WITH LAGRANGIAN FILTERING



## REFERENCE FOR DETAILS (& CODES)

- Wang C., Liu Z.\*, and Lin H. (2023), On dynamical decomposition of multiscale oceanic motions, *Journal of Advances in Modeling Earth Systems*, 15(3), e2022MS003556.
- Wang C., Liu Z.\*, and Lin H. (2023), A simple approach for disentangling vortical and wavy motions of oceanic flows, *Journal of Physical Oceanography*, 53(5), 1237–1249.

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