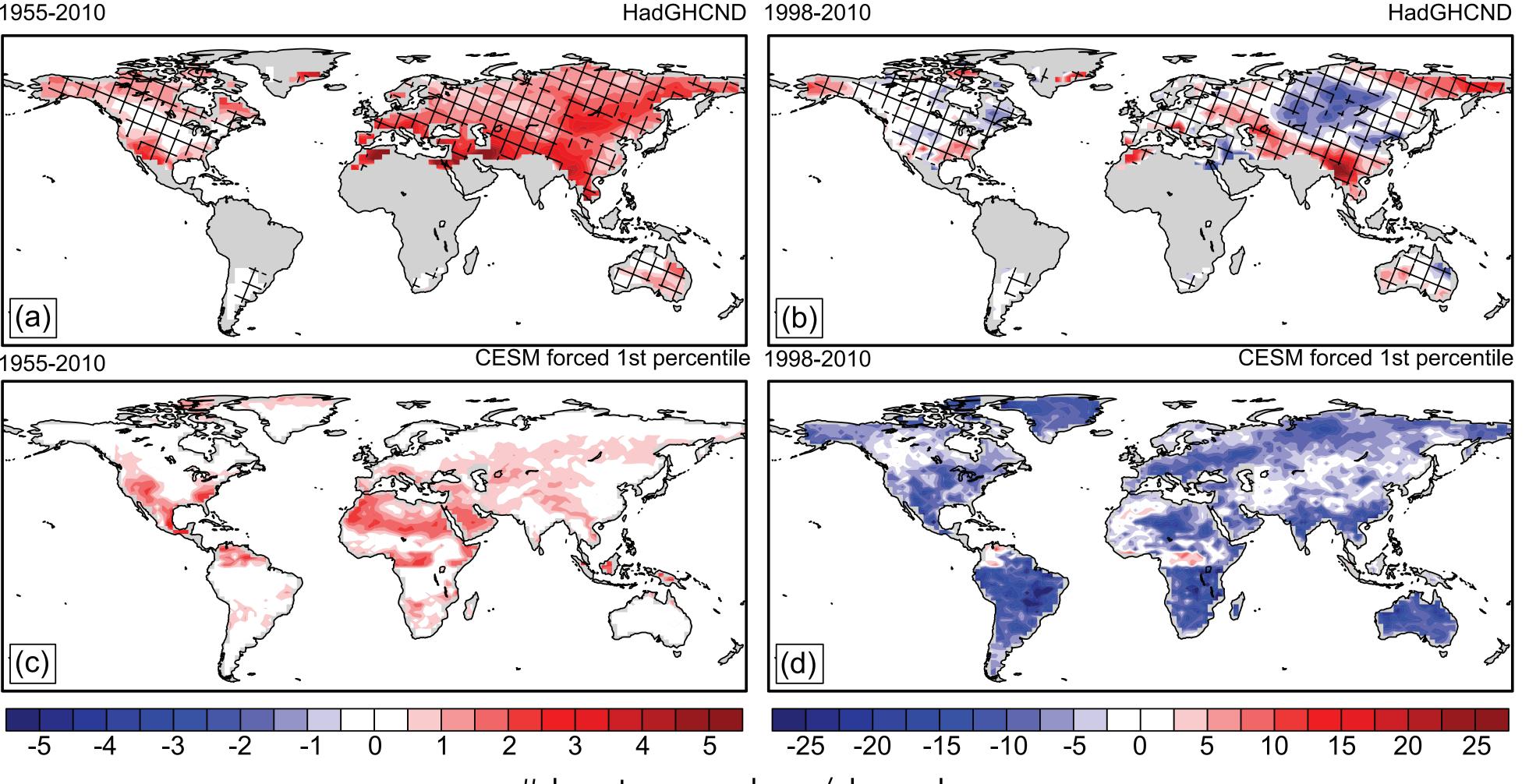
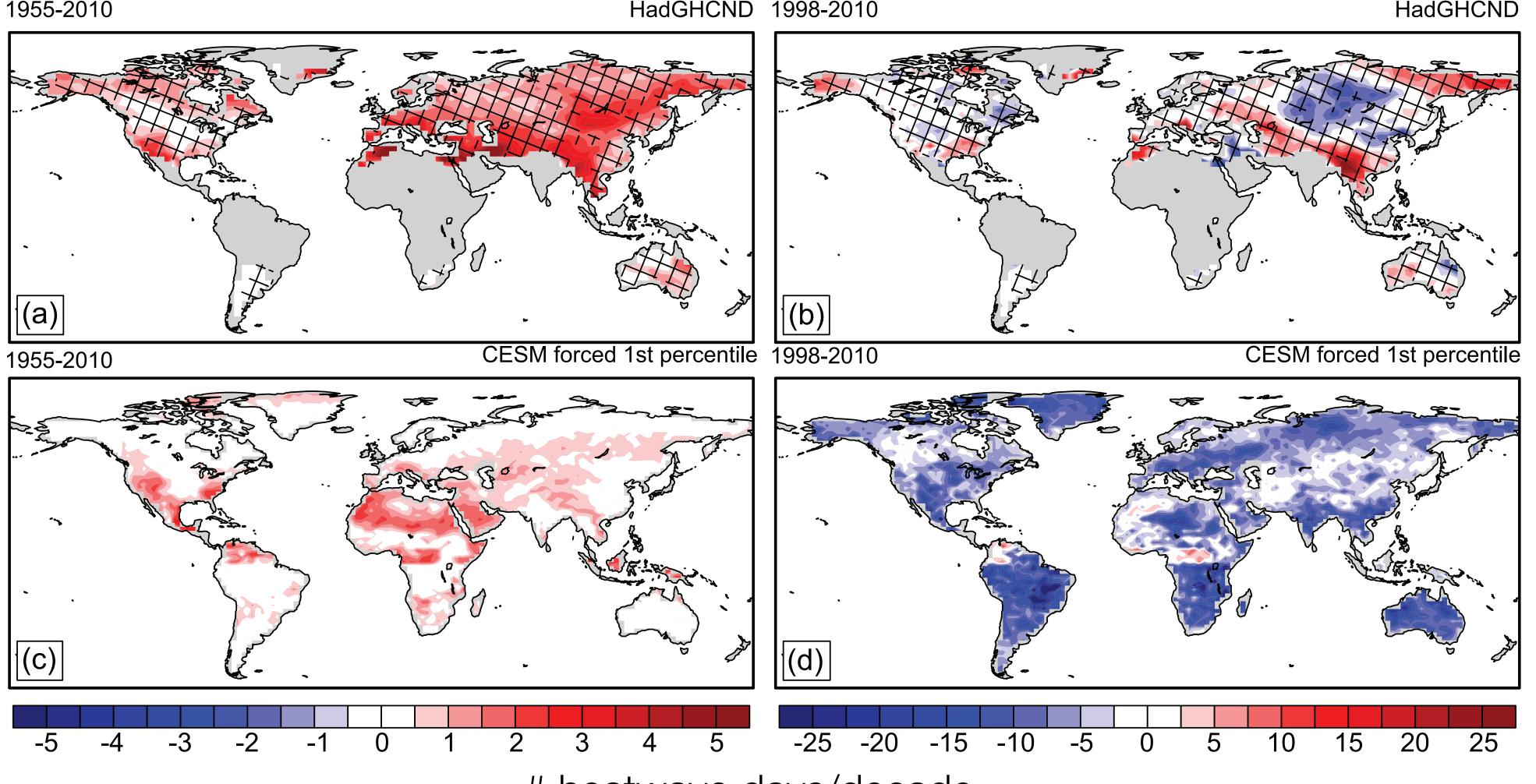


### Directly comparing historical trends in heat extremes with model simulations is difficult due to influence of internal variability

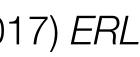
1955-2010



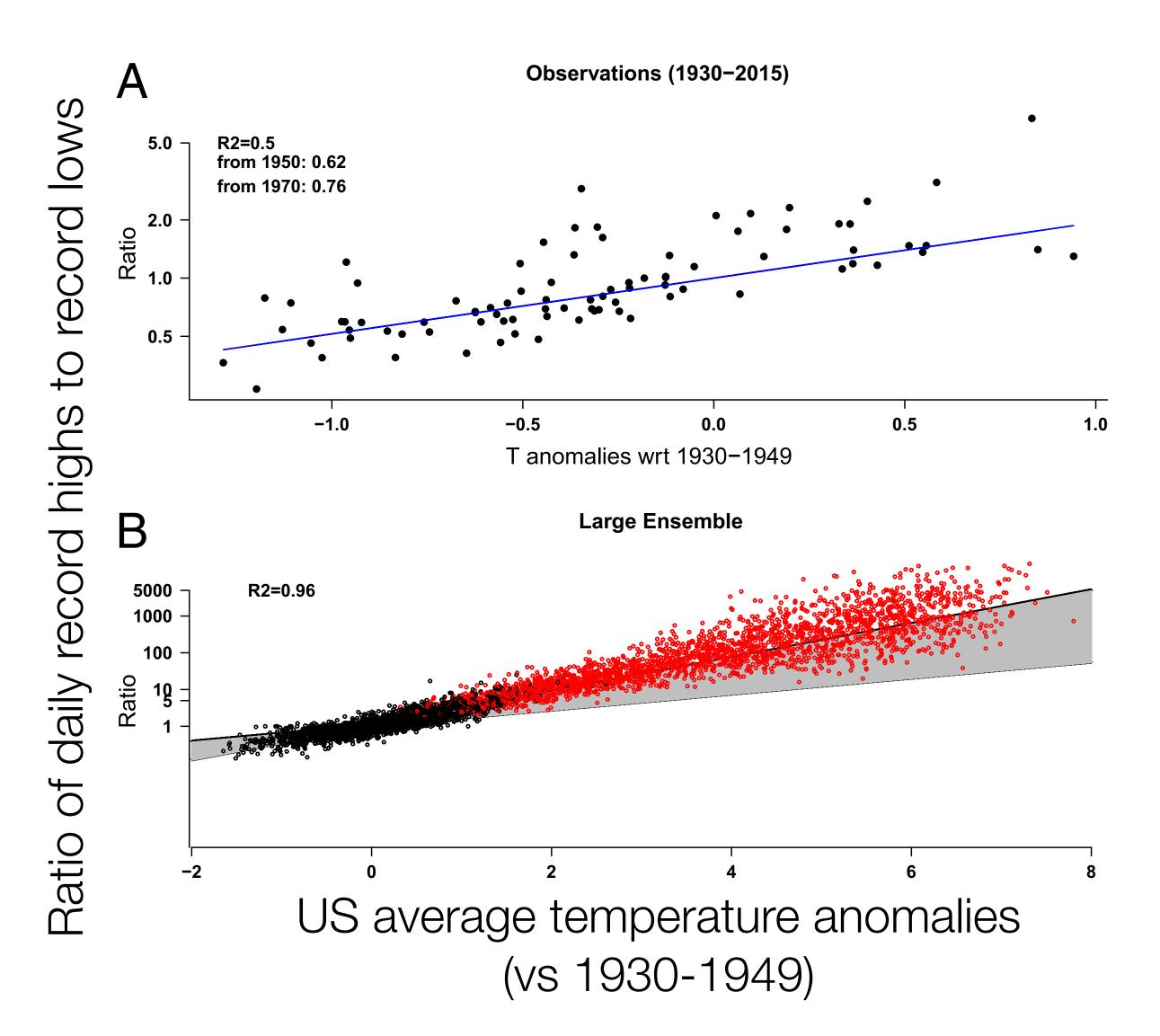


# heatwave days/decade

Perkins-Kirkpatrick et al (2017) ERL



### Signals in extremes get more clear through spatial aggregation. Hot extremes warm "too" fast in US in CCSM ensemble

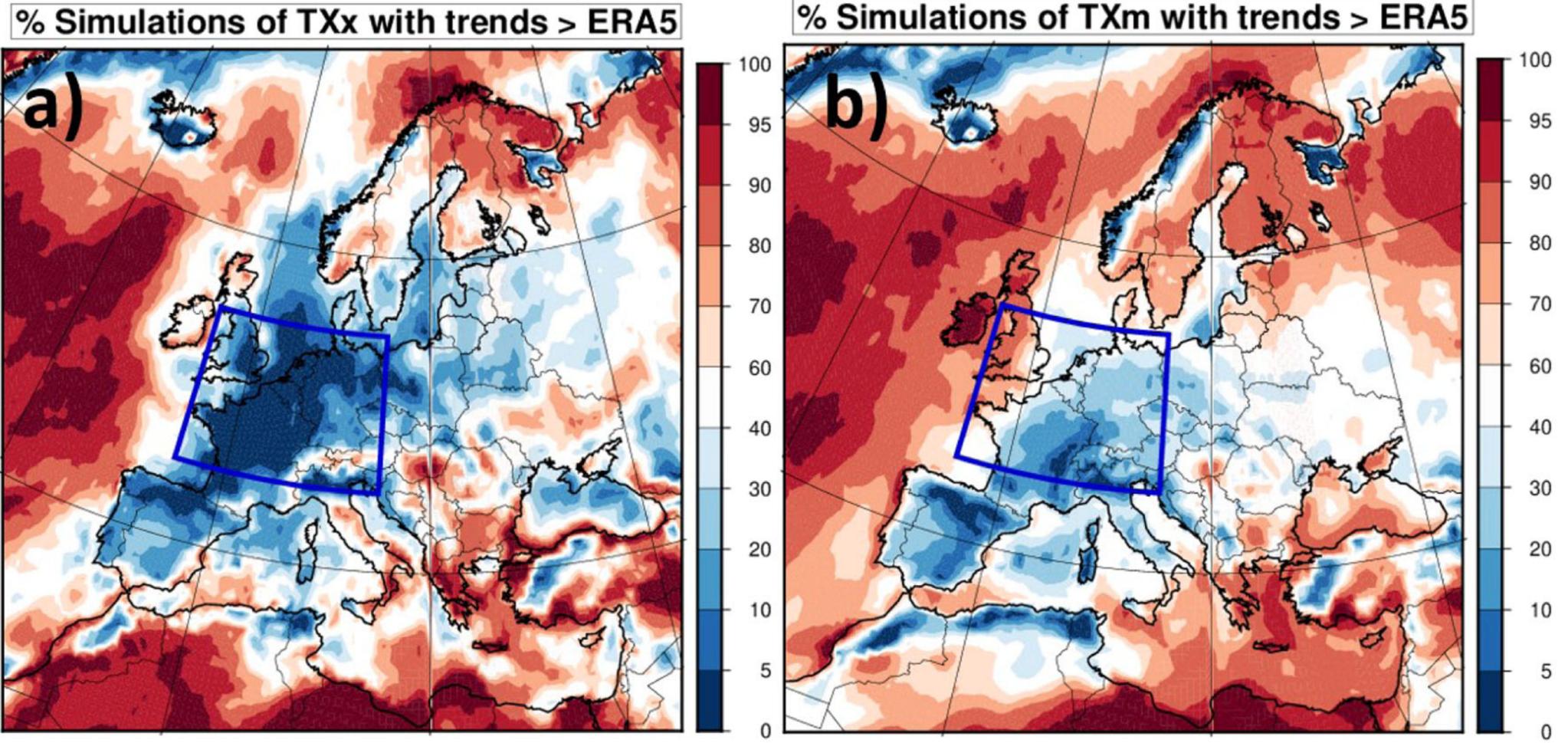


#### hypothesized cause: decrease in precipitation and ET

Meehl et al (2016), PNAS



### In contrast, western European heat extremes are warming faster than most models (1950-2022), difference greater than for mean



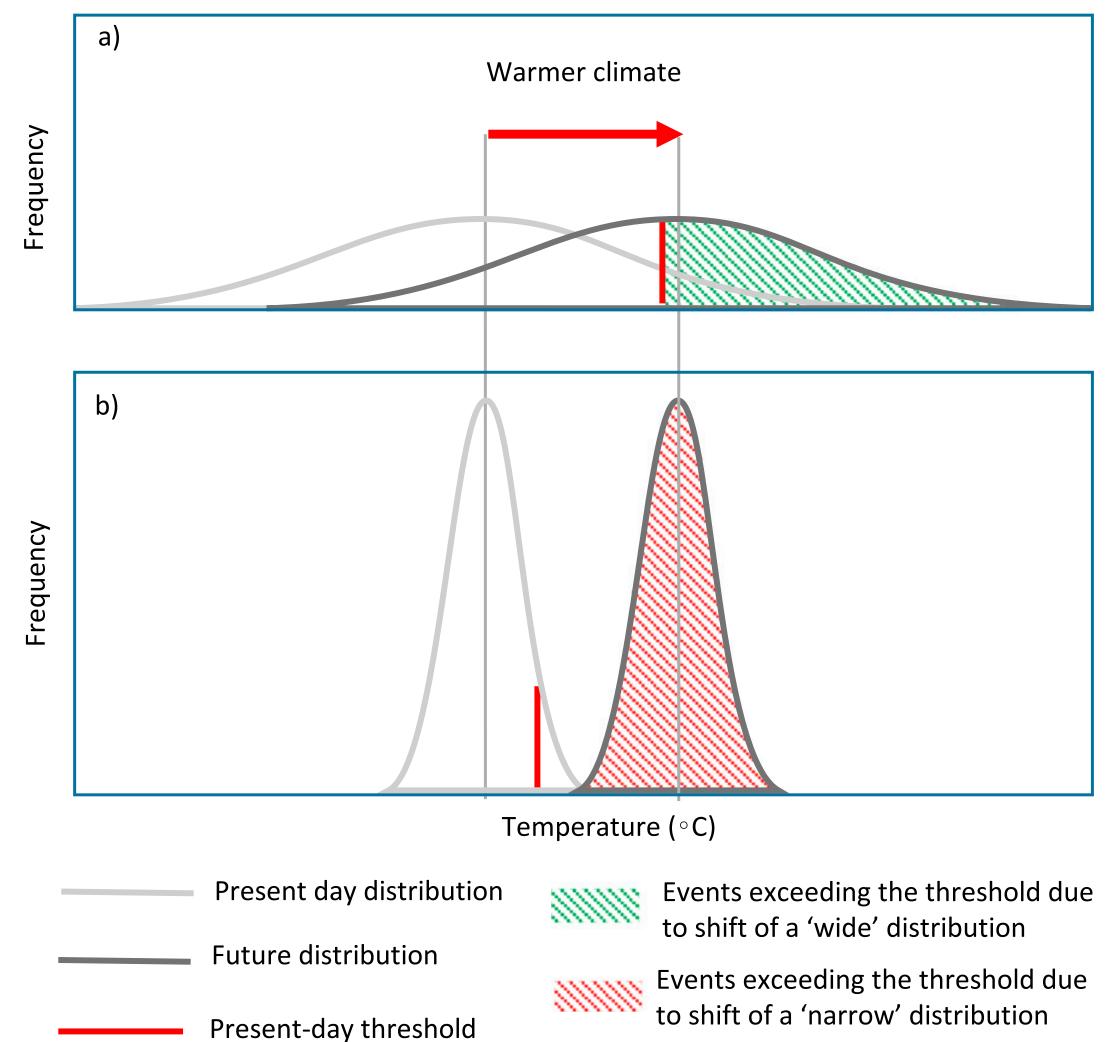
Vautard et al (2023) Nature Communications

Many metrics of changes in extremes are a strong function of the mean state.

Three examples.

In all cases, the true climate change signal is a uniform warming across summertime temperatures.

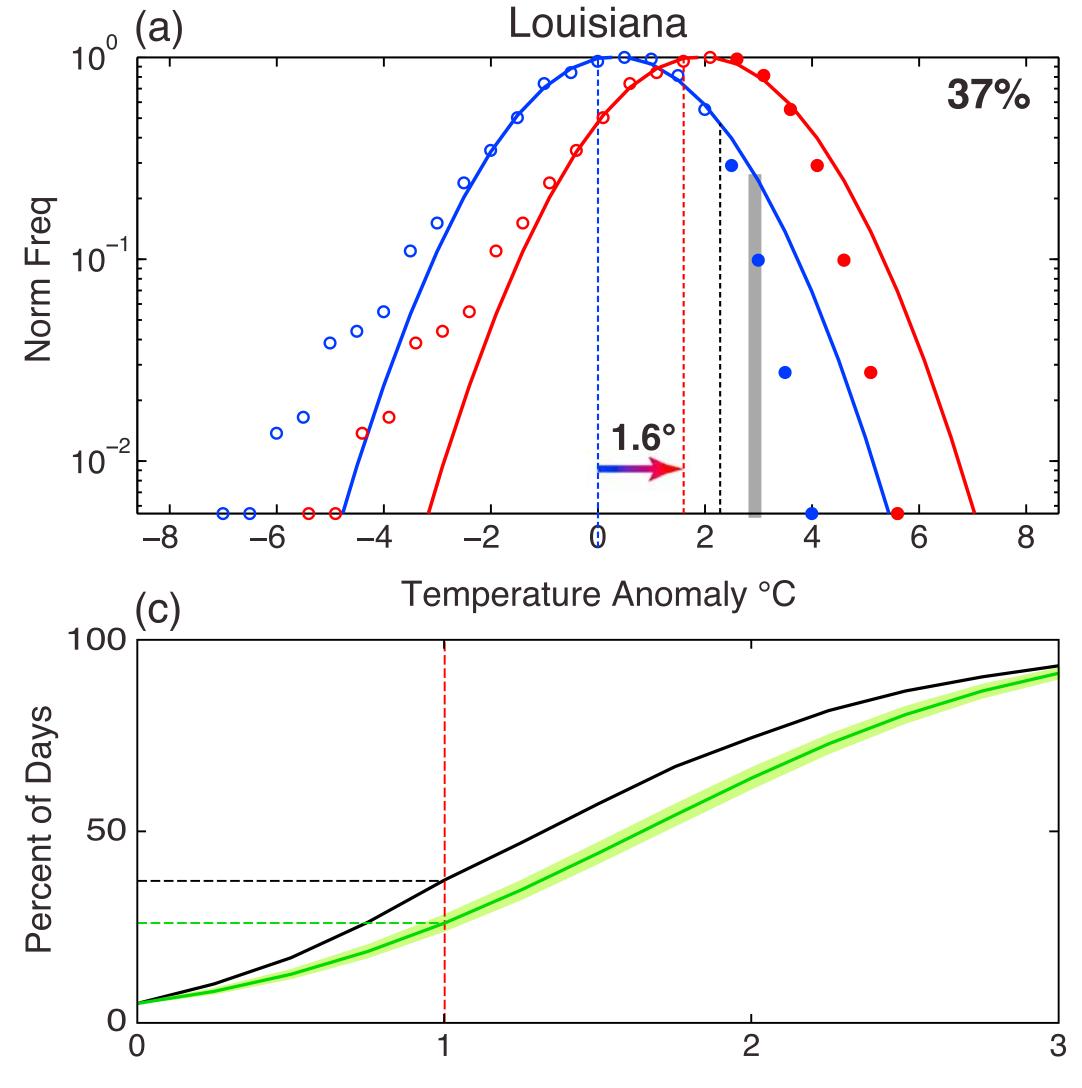
### The change of the number of days beyond a threshold depends on the width of the distribution: greater increases for narrow distributions





### The change of the number of days beyond a threshold depends on the symmetry of the distribution: greater increases for short upper tails

### actual distribution normal distribution



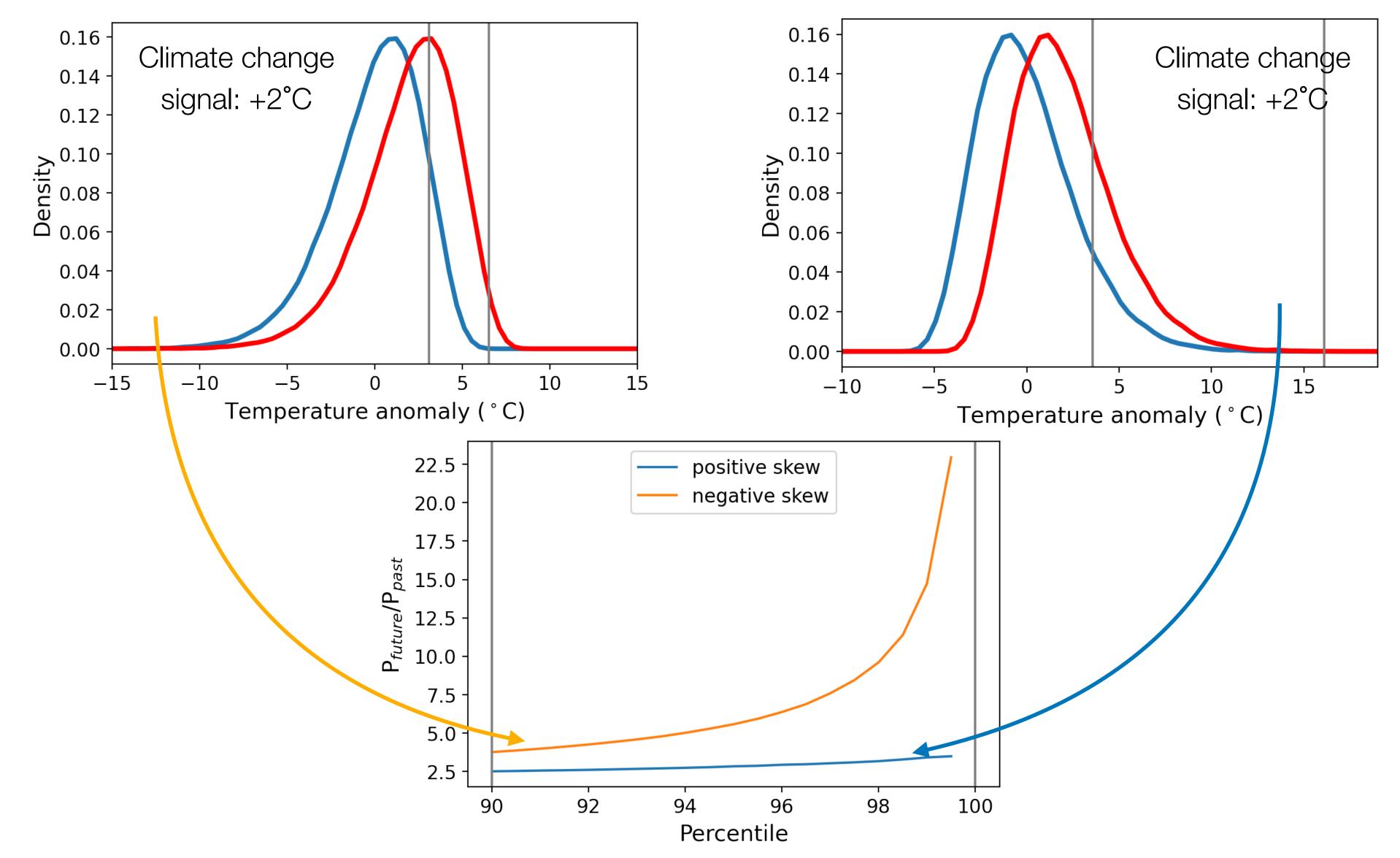
**Distribution Shift in Standard Deviations** 

Loikith and Neelin (2015) GRL





### The change in the probability of an event depends non-linearly on the threshold and the underlying distribution





A modest proposal: measure change in extremes as the change in temperature for a given percentile (max = 100th percentile)

A hierarchy of controls on the change in extremes (across models, or comparing models and observations)

Global mean temperature

Global land temperature

Global land temperature

Summer versus annual-mean temperatures

Global land temperature

Summer versus annual-mean temperatures

Local summer average temperature

Global land temperature

Summer versus annual-mean temperatures

Local summer average temperature

Local summer extreme temperature

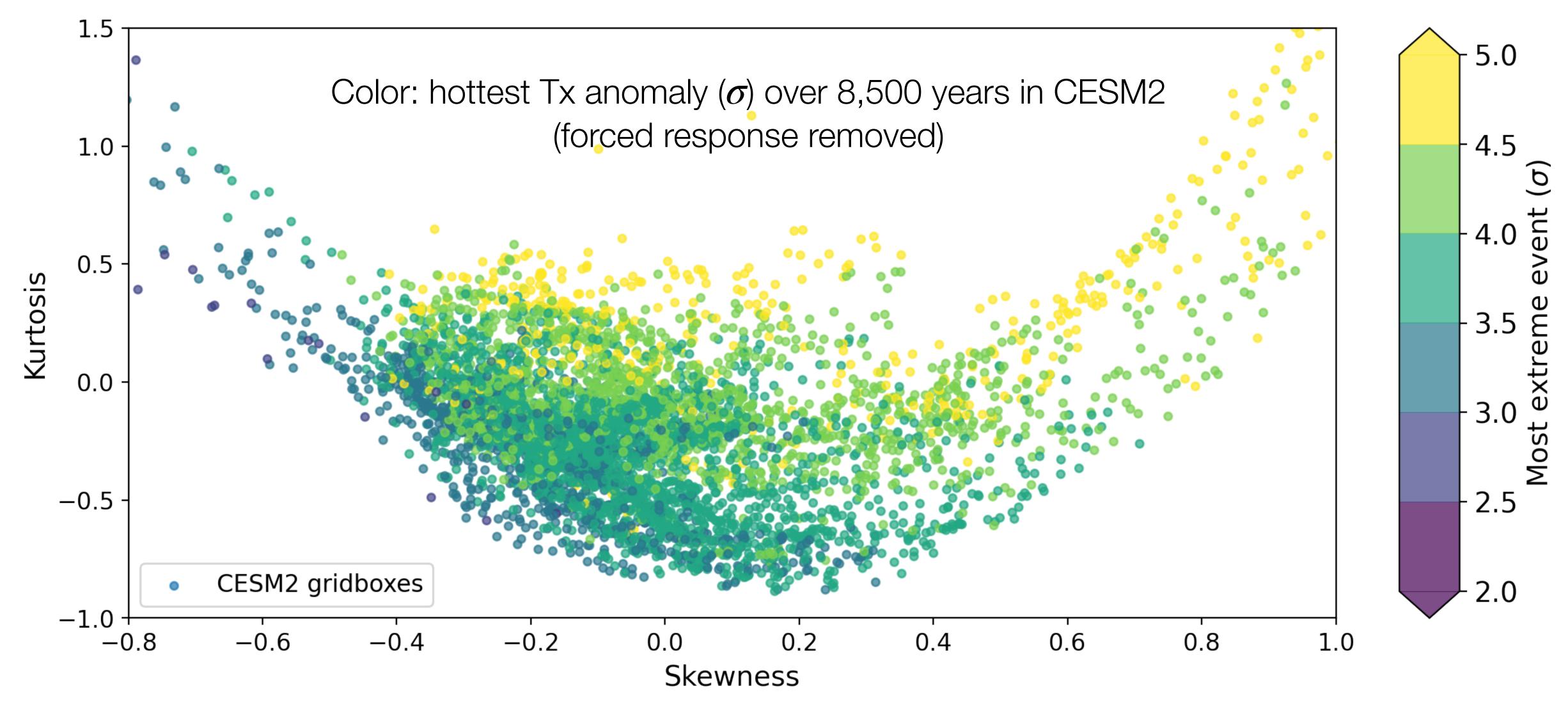
Global land temperature

Summer versus annual-mean temperatures

Local summer average temperature

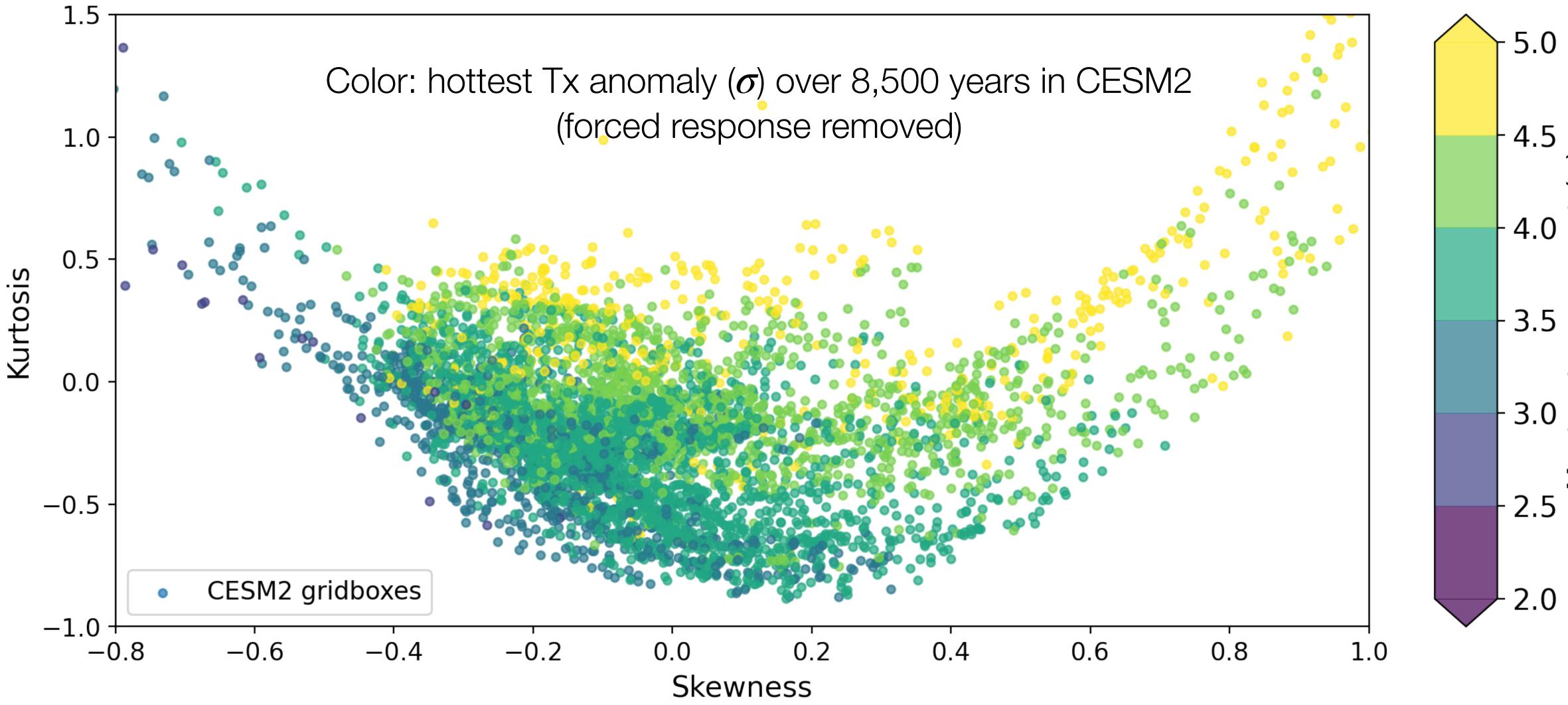
Local summer extreme temperature

### The probability of very extreme events compared to the mean is higher for locations with positive skewness and/or kurtosis



McKinnon and Simpson (2022), GRL; see also Van Loon and Thompson (2023), GRL

### This can lead to apparent trends in extremes from sampling alone



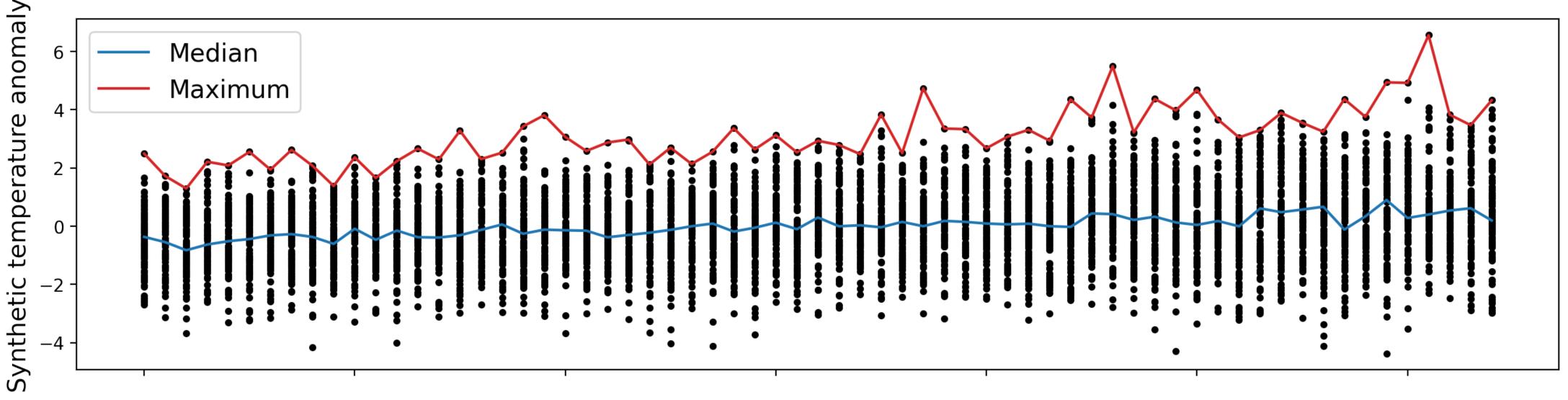
McKinnon and Simpson (2022), GRL; see also Van Loon and Thompson (2023), GRL

ω ent (0 4.0 3.5 E Most

#### Two challenges:

- 1. The contribution of internal variability to trends in extremes is very large
- 2. The probability of a given extreme (e.g. a 3-sigma across space

event) is spatially-variable due to non-normality in temperature distributions, so unclear how to average

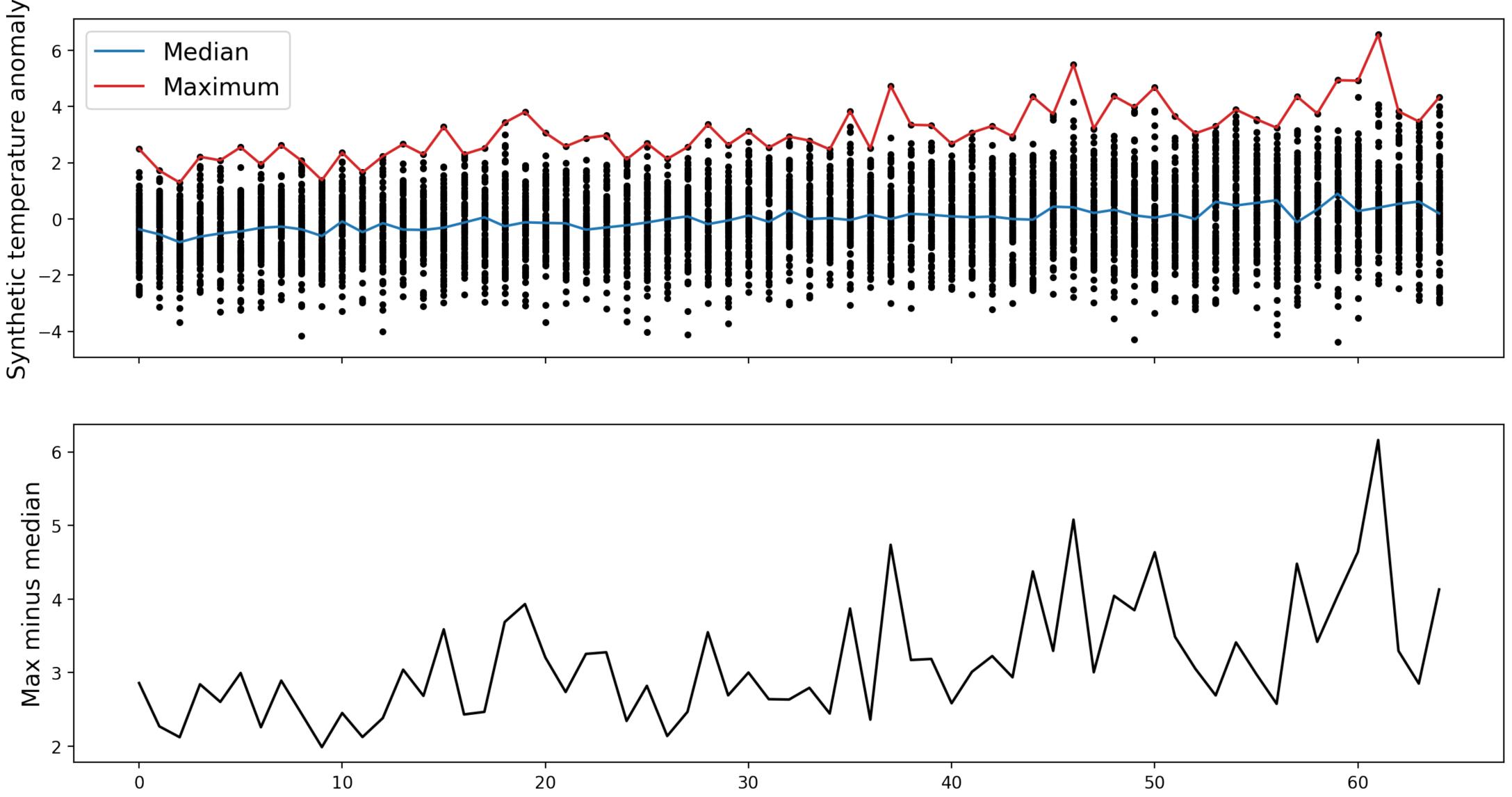


Synthetic years

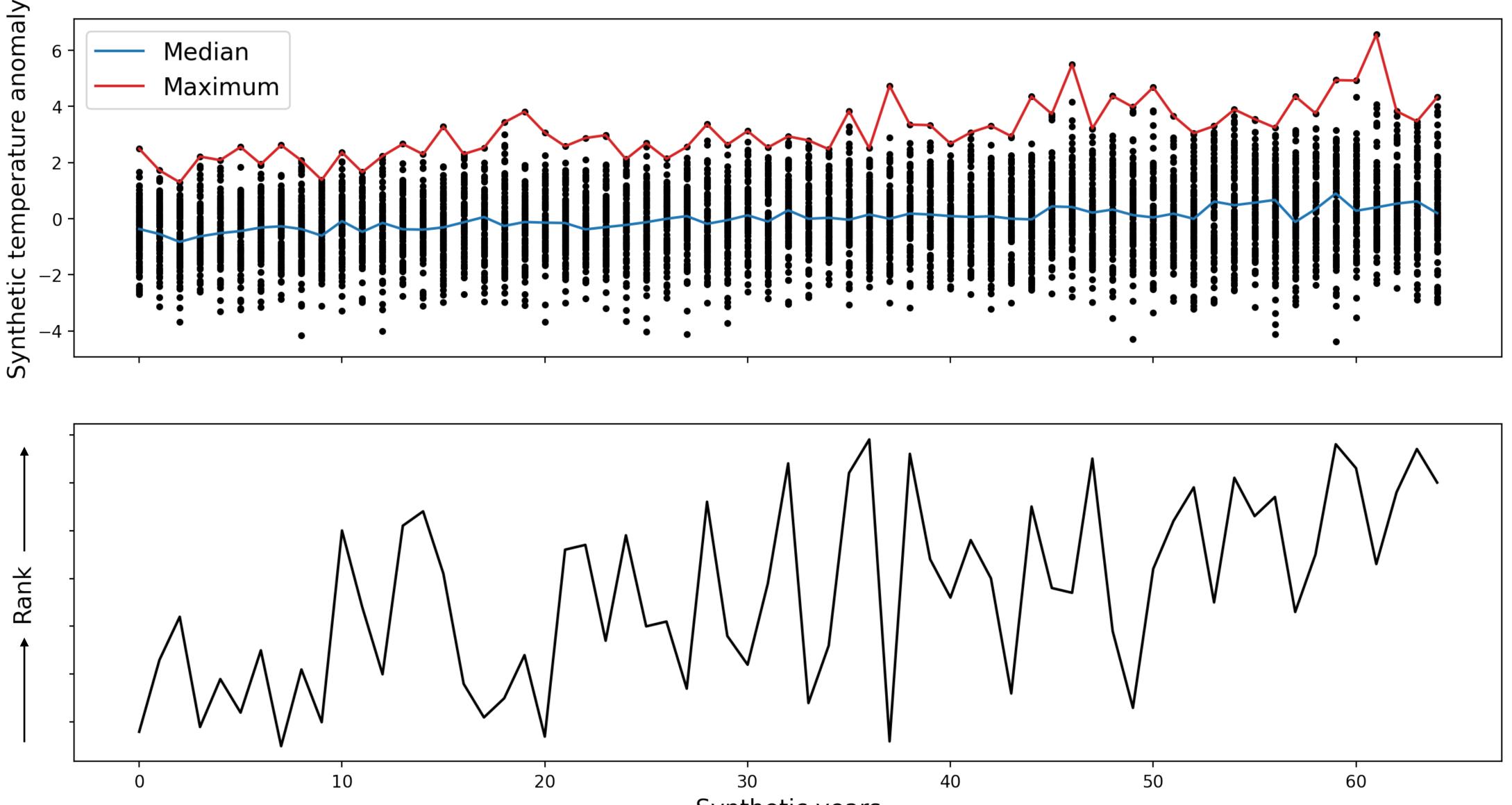
#### Synthetic data: normal distribution with an increasing variance

McKinnon, Simpson, and Williams (in prep)

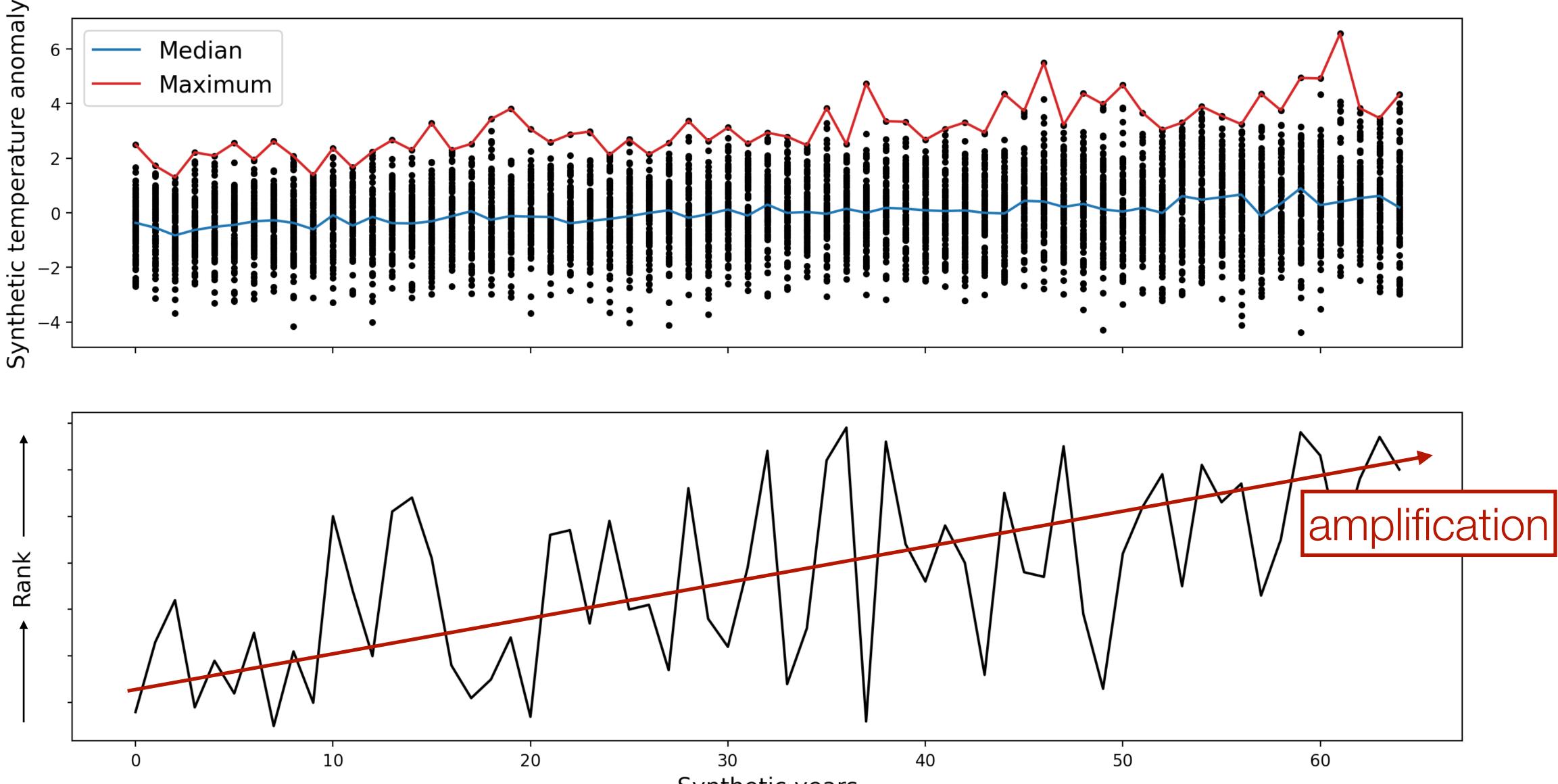




Synthetic years



Synthetic years



Synthetic years



#### Advantages of a rank-based approach

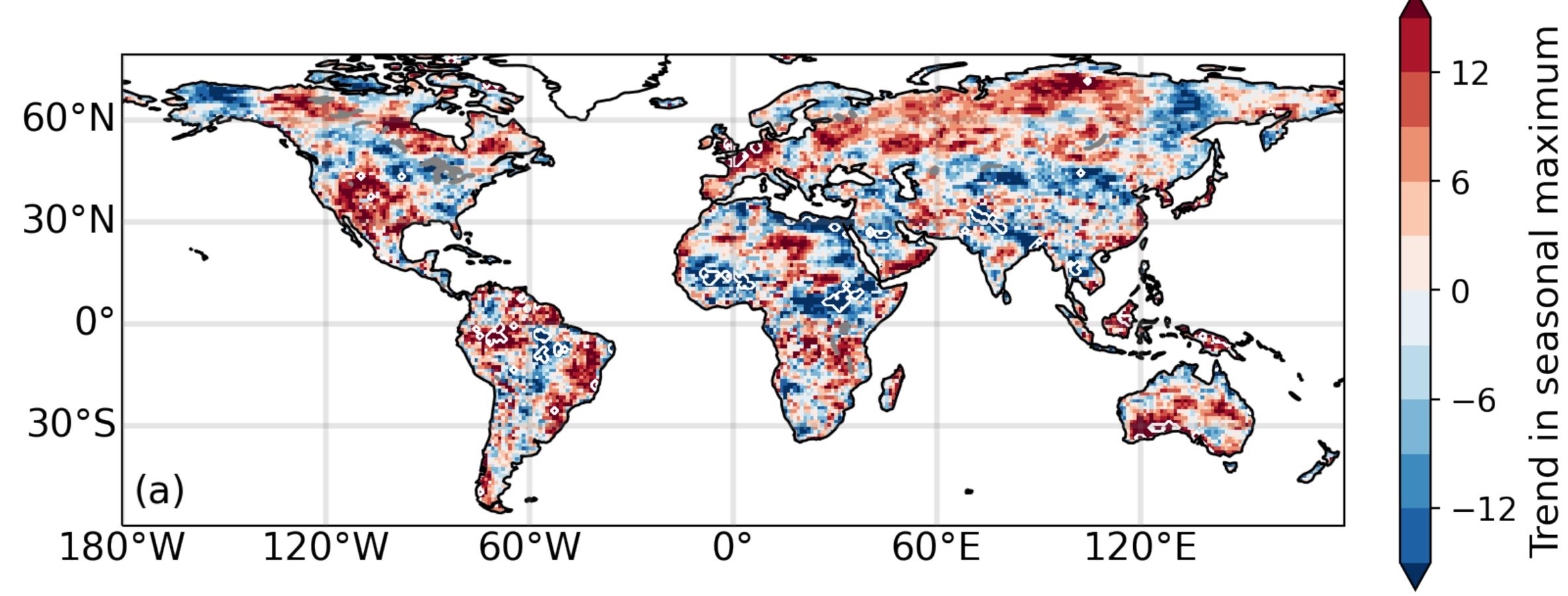
- No dependence on the underlying distribution
- The expected rank across locations and time is known (33 for 65 years of data)
- Can combine information or inter-compare across different definitions of heatwaves

#### Advantages of a rank-based approach

- No dependence on the underlying distribution
- (33 for 65 years of data)
- Can combine information or inter-compare across different definitions of heatwaves

The expected rank across locations and time is known

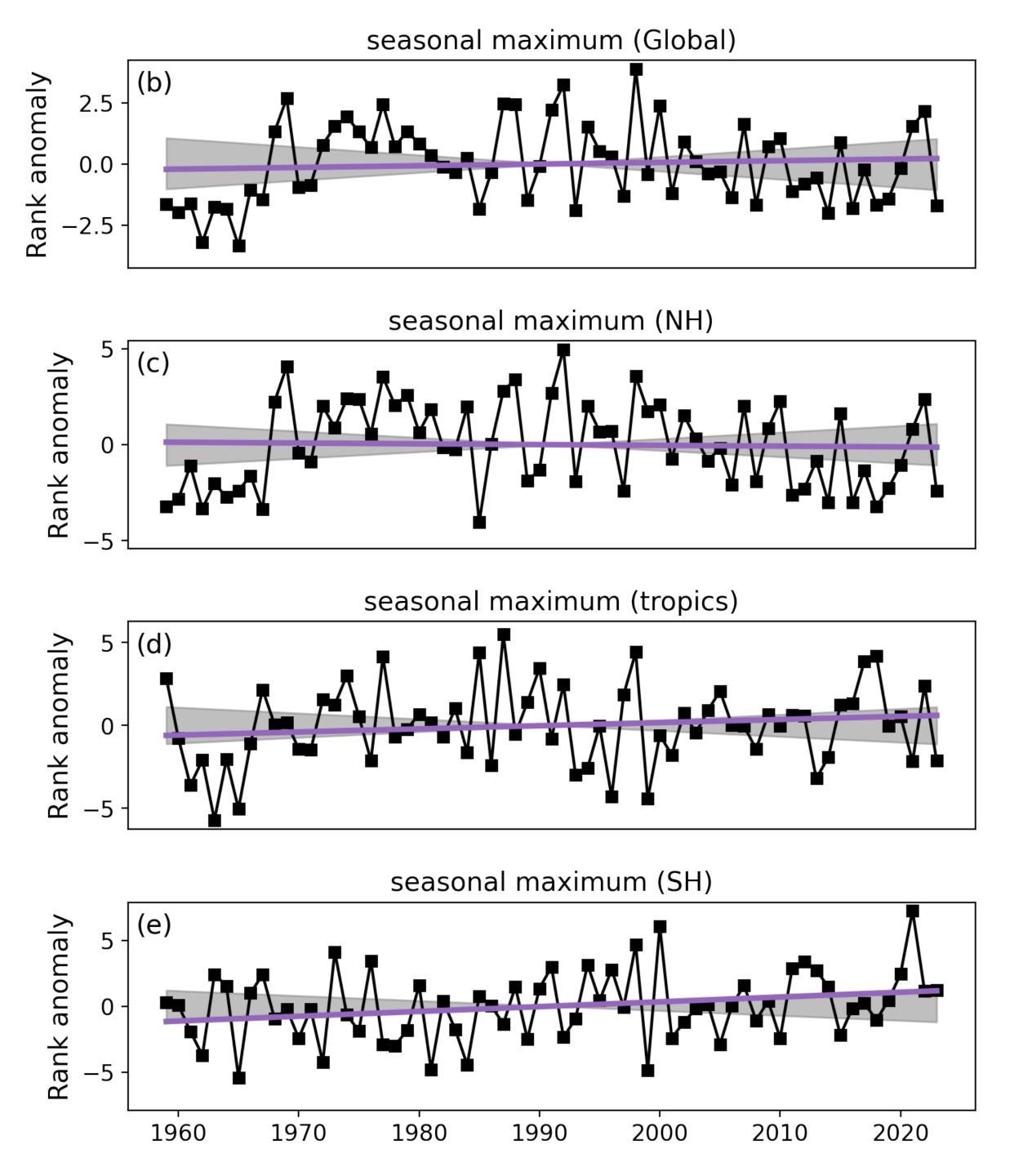
Data: ERA5, daily maximum (Tx), 1959-2023



## Spatial heterogeneity in trends of amplification in ERA5, very few trends are locally significant ( $\alpha_{FDR} = 0.05$ )

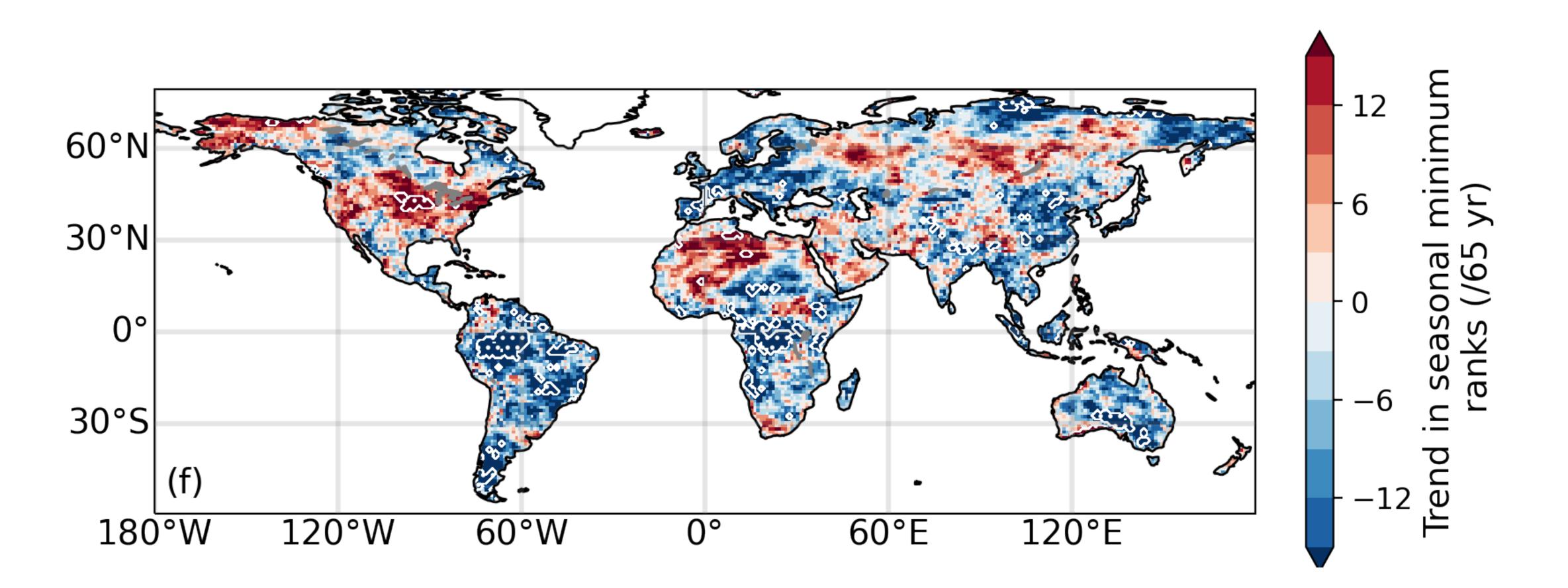
#### significance indicated by white contours / stippling





No significant trends at the global or hemispheric/tropical scale



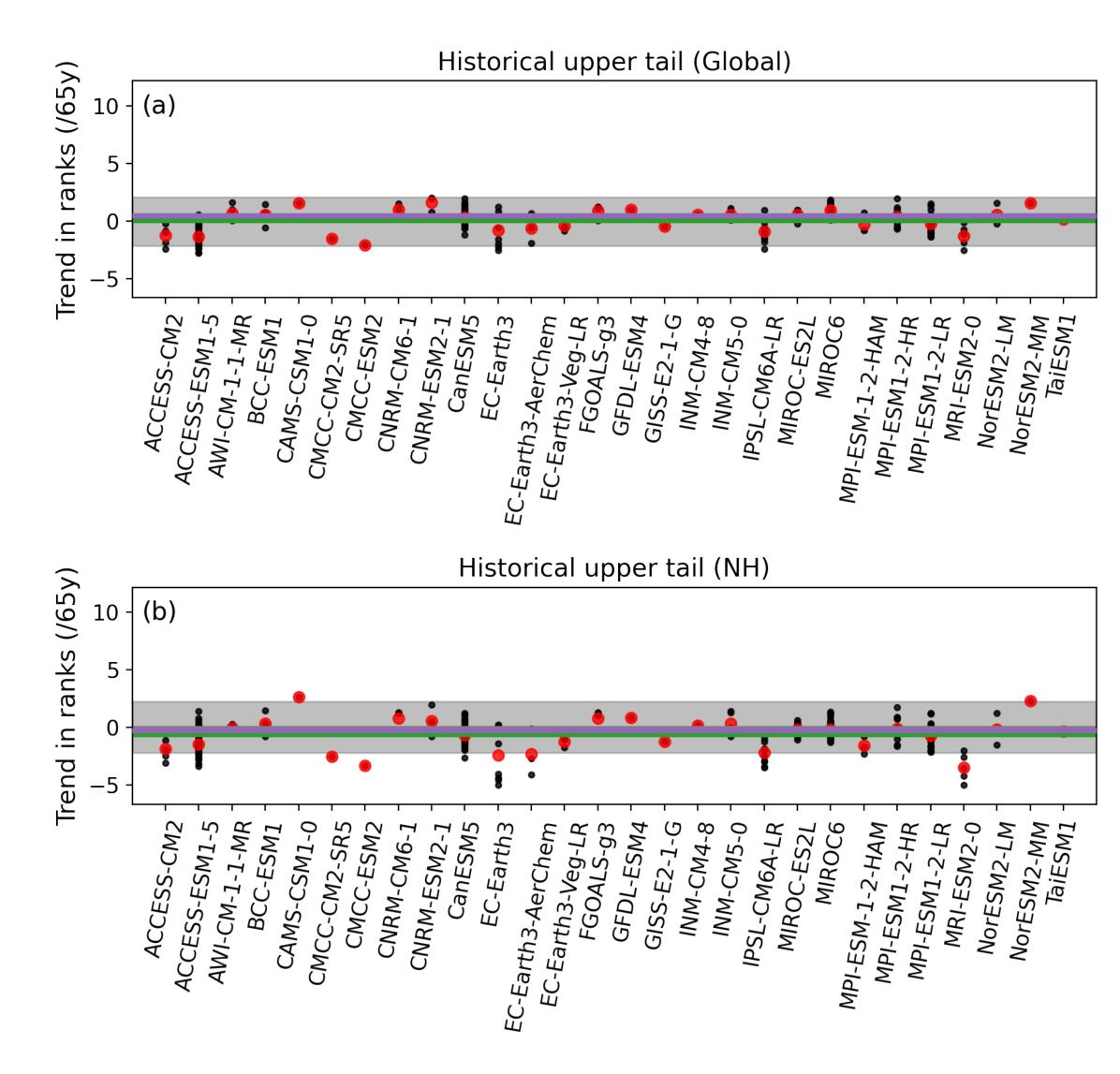


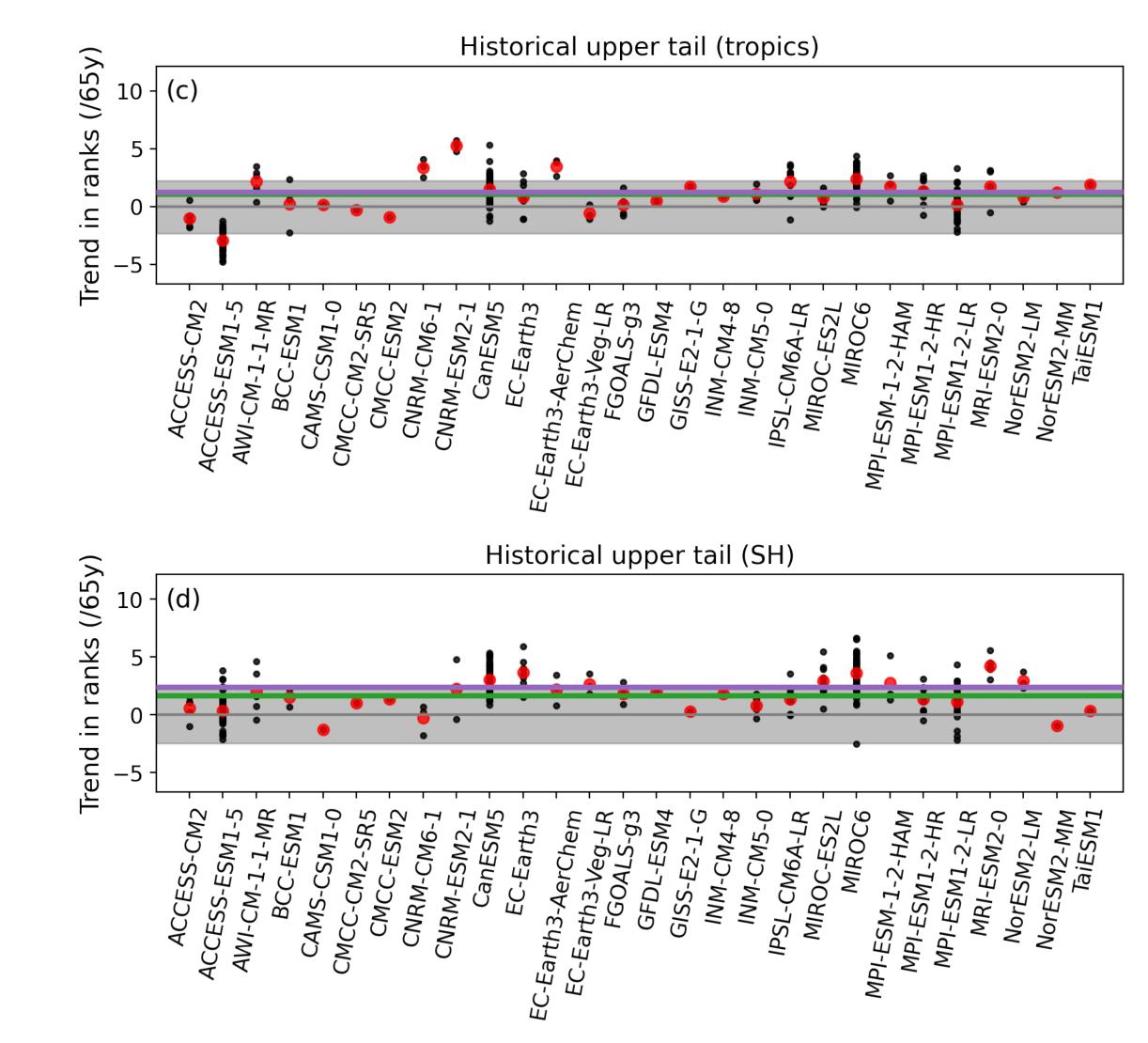
### What about cold summertime temperatures (still Tx though)? In most regions of the world, they are warming less than the median

seasonal minimum (Global) (g) Rank anomaly 5 -0 -5 seasonal minimum (NH) 5 (h) Rank anomaly ┶┺╍╸┍ 0 -5 seasonal minimum (tropics) 10 Rank anomaly 0 -10seasonal minimum (SH) 10 Rank anomaly  $\Lambda \wedge \Lambda$  $\Lambda$  , -102010 1970 1980 1990 2000 2020 1960

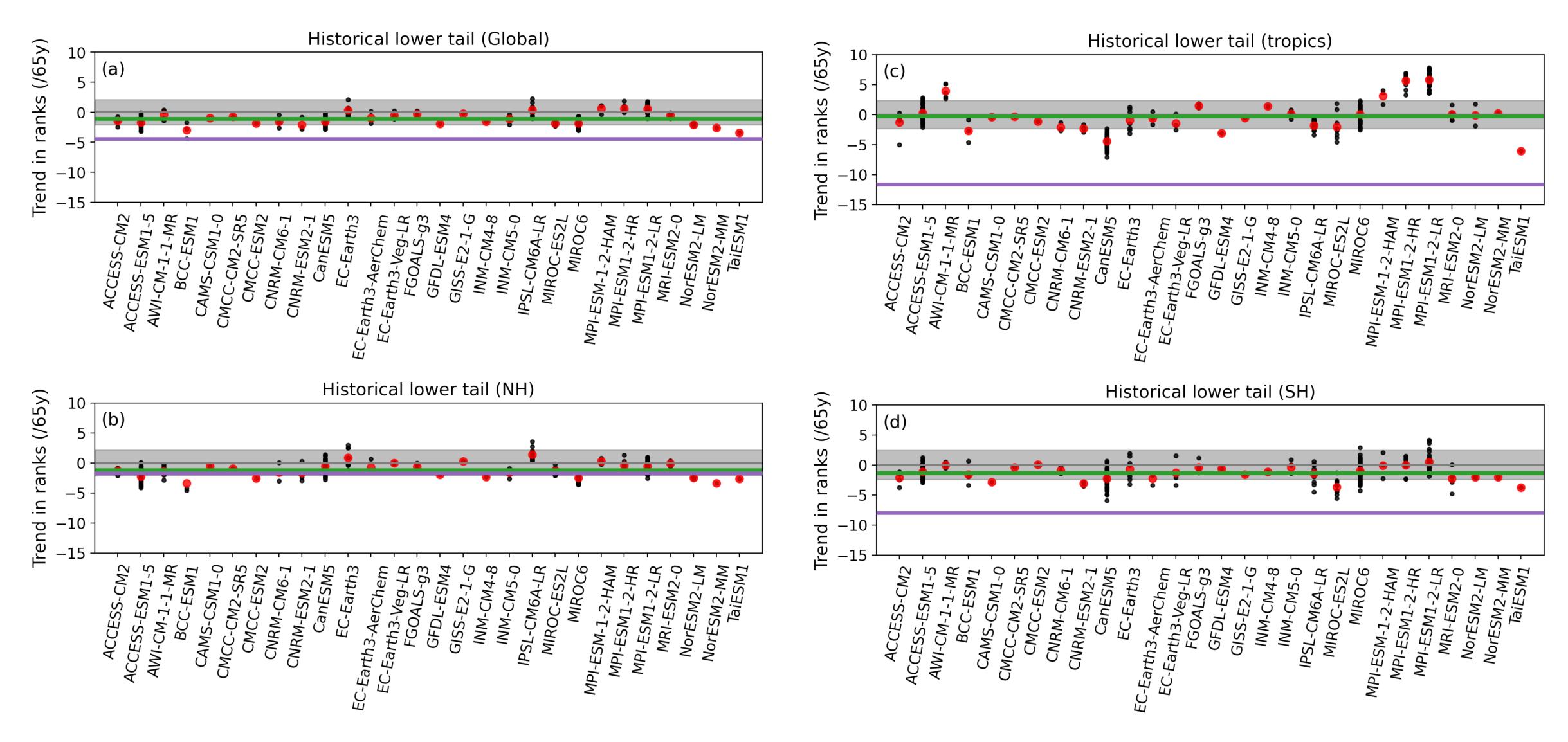
Significant trends (except in NH) towards *damped* warming of the lower tail

# CMIP6 simulations tend to agree with observations of no historical, significant amplification of heat extremes





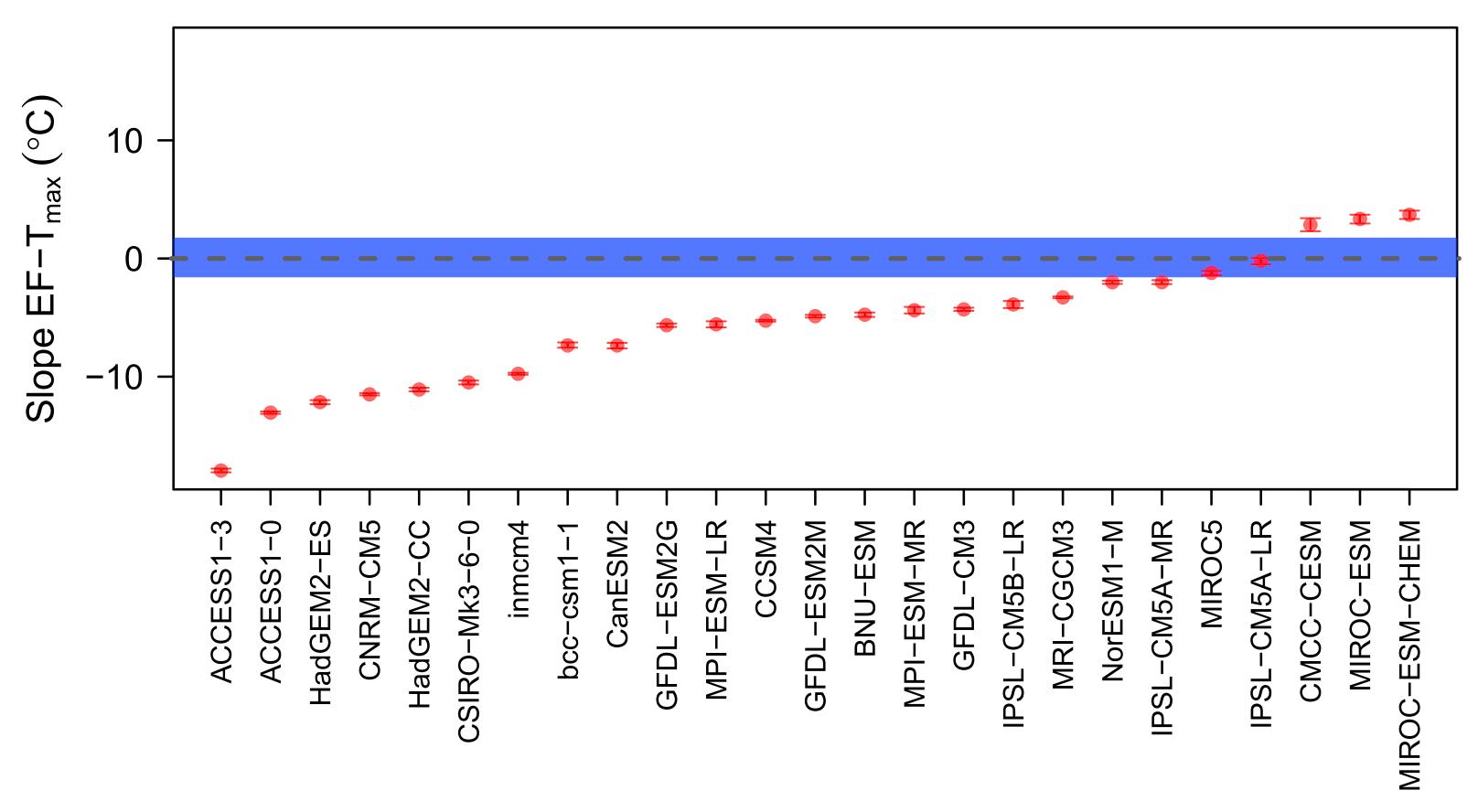
### But they miss the observed damping of the cold tail in the tropics and Southern Hemisphere, perhaps related to precipitation changes





### Consistency between models and observations in terms of lack of hot day amplification does not preclude model errors

a) Wet



How do mean state errors affect (or not) trends?

observations: Tmax in "wet" regions is insensitive to evaporative fraction -> lack of land/atmosphere coupling

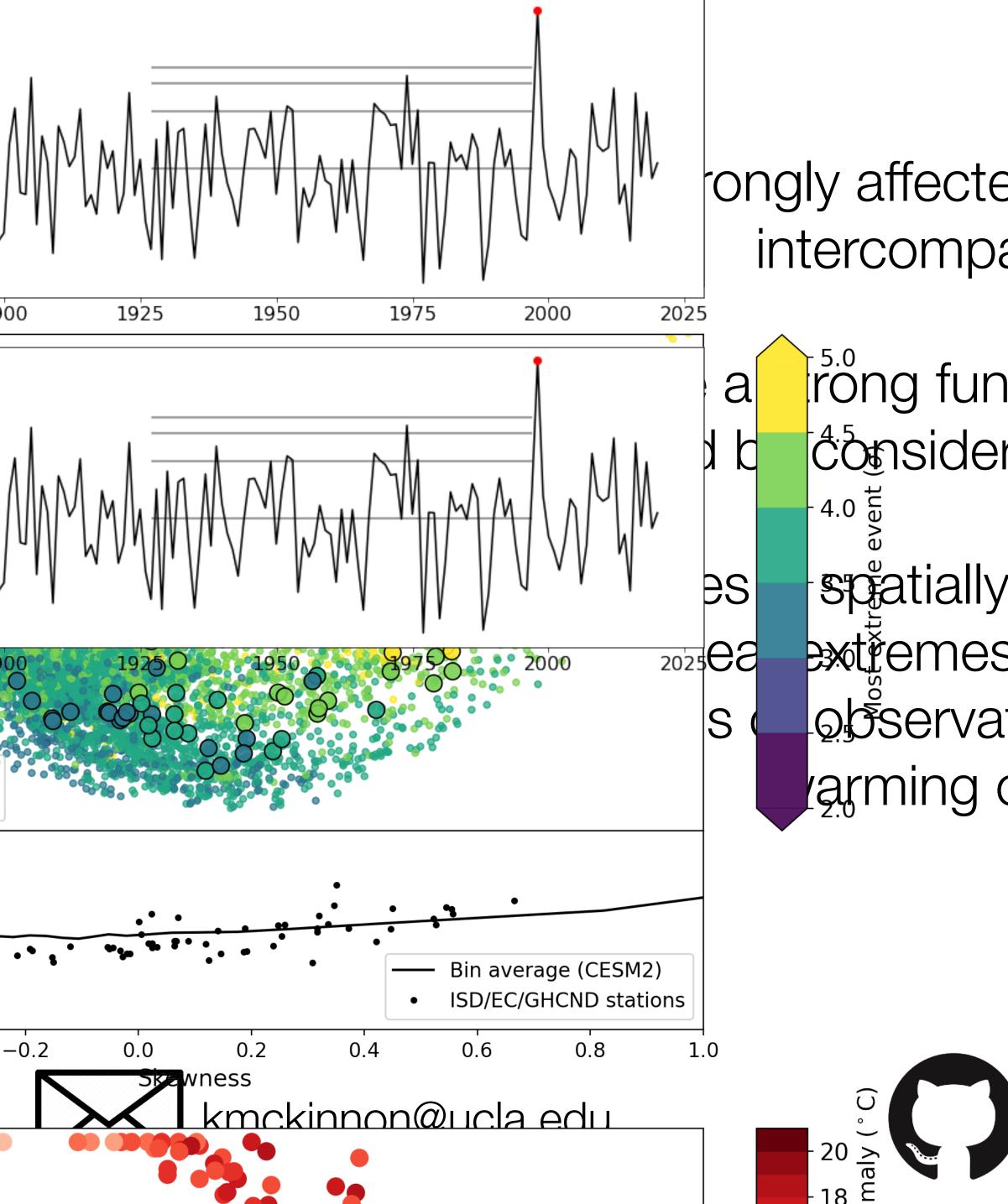
most models (CMIP5): Tmax is higher when the evaporative fraction is lower (drier conditions) -> existence of land/atmosphere coupling

Ukkola et al (2018) GRL









ongly affected by internal variability, so can be difficult to intercompare with models.

rong function of the underlying distribution, which tobasidered before interpretation.

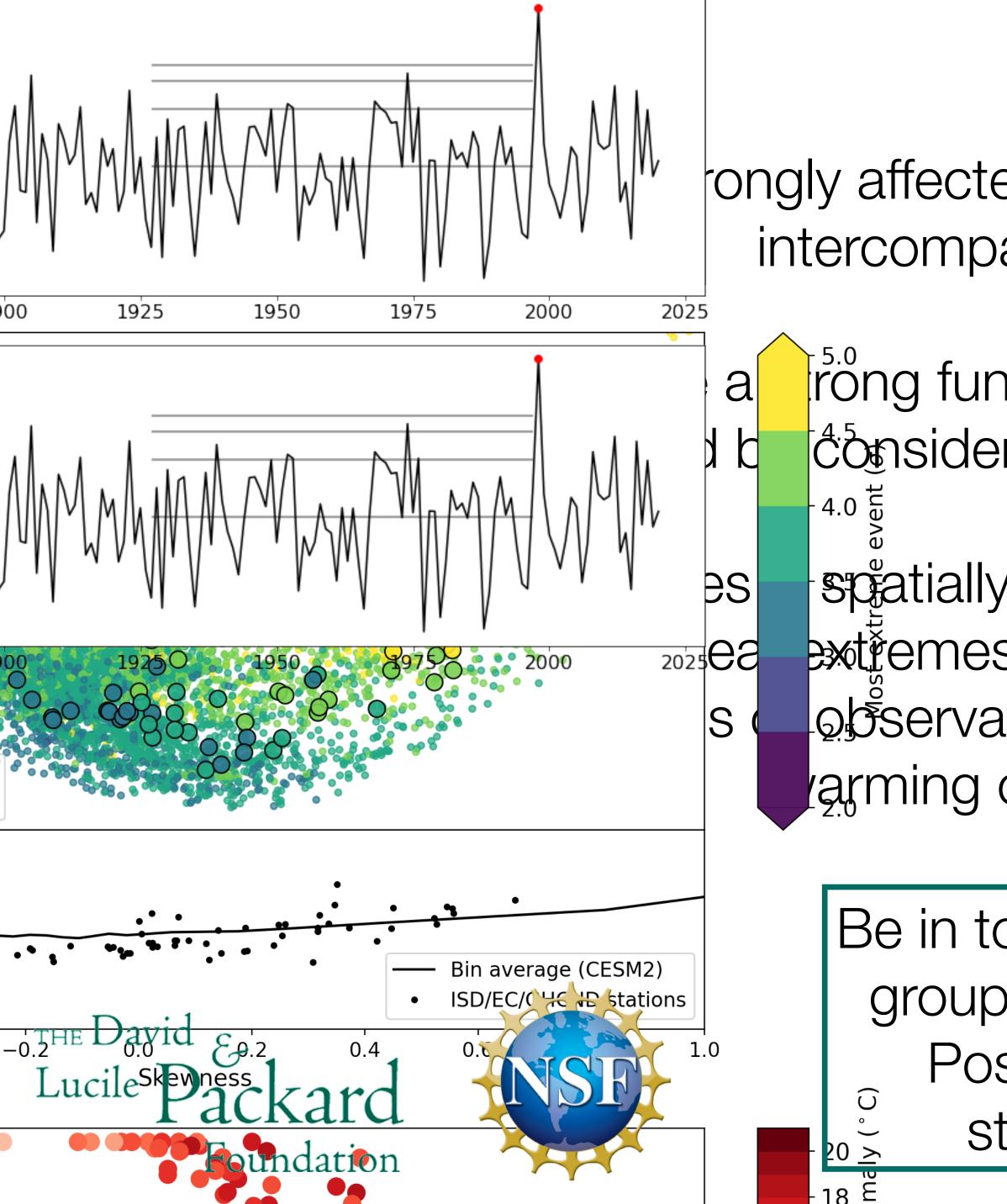
spatially-variable due to non-normality. We propose extremes are not warming faster than the median at observations, but the models miss the damped grming of the lower tail.





website





ongly affected by internal variability, so can be difficult to intercompare with models.

rong function of the underlying distribution, which tobasidered before interpretation.

spatially-variable due to non-normality. We propose extremes are not warming faster than the median at observations, but the models miss the damped grming of the lower tail.

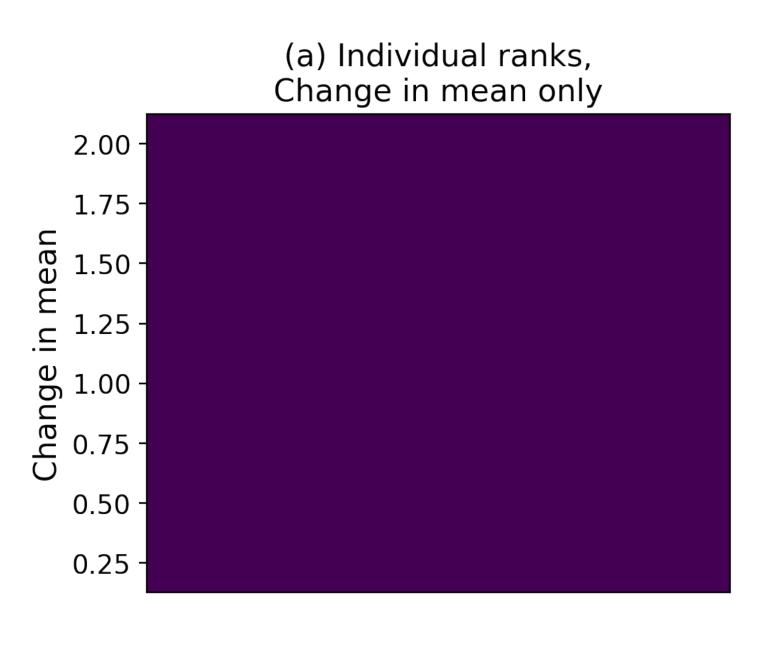
Be in touch if you want to join the group to work on these topics! Post-docs (now) and PhD students (next season)

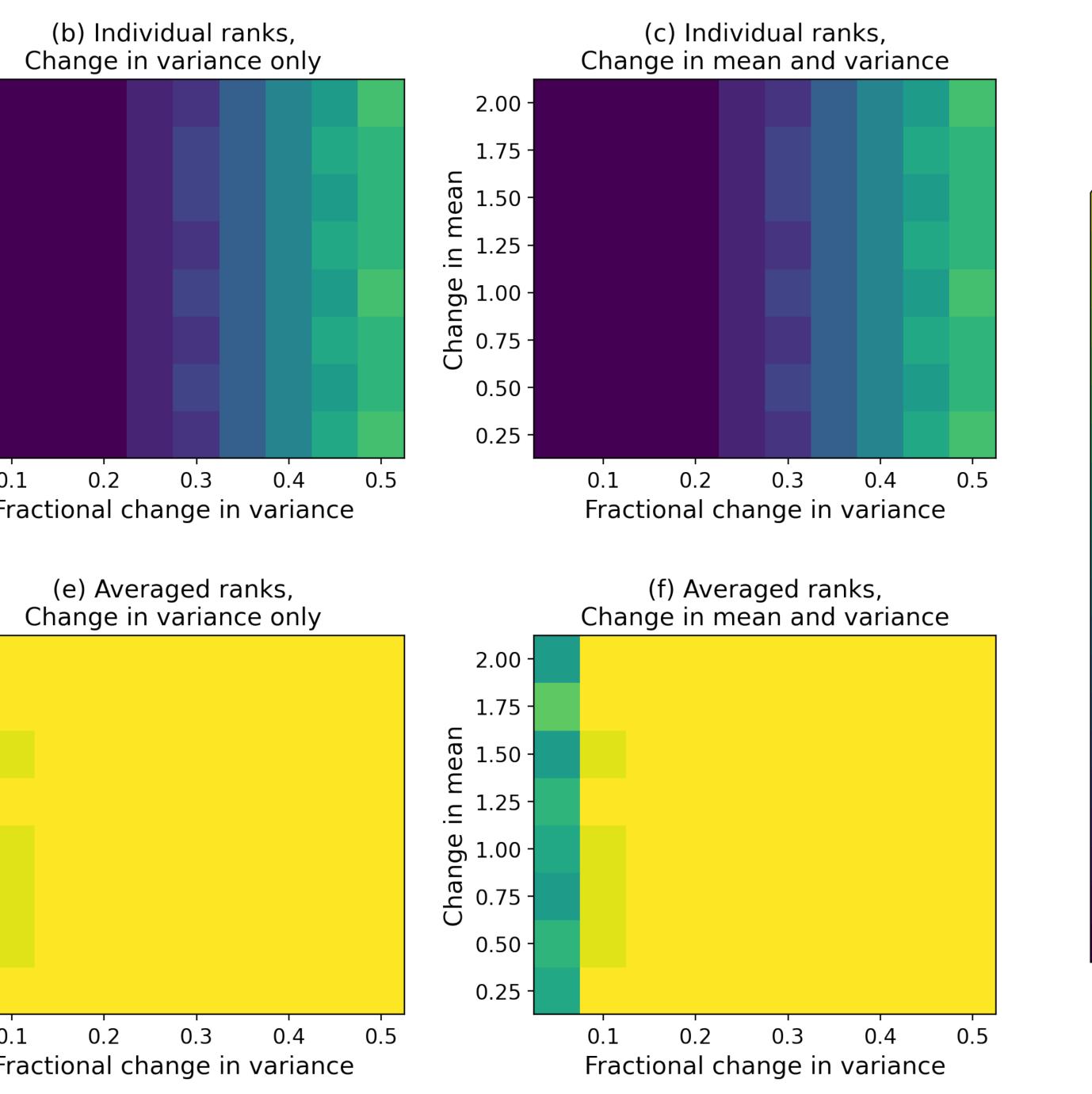


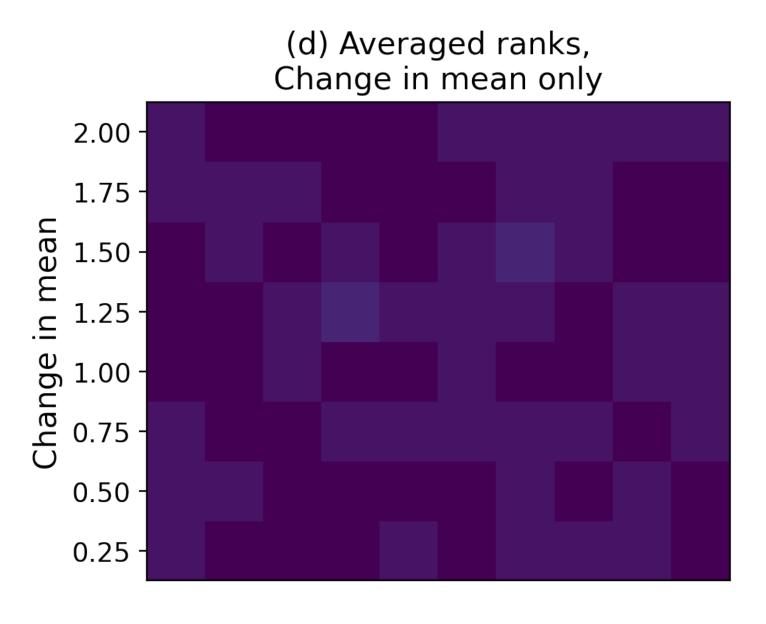
website

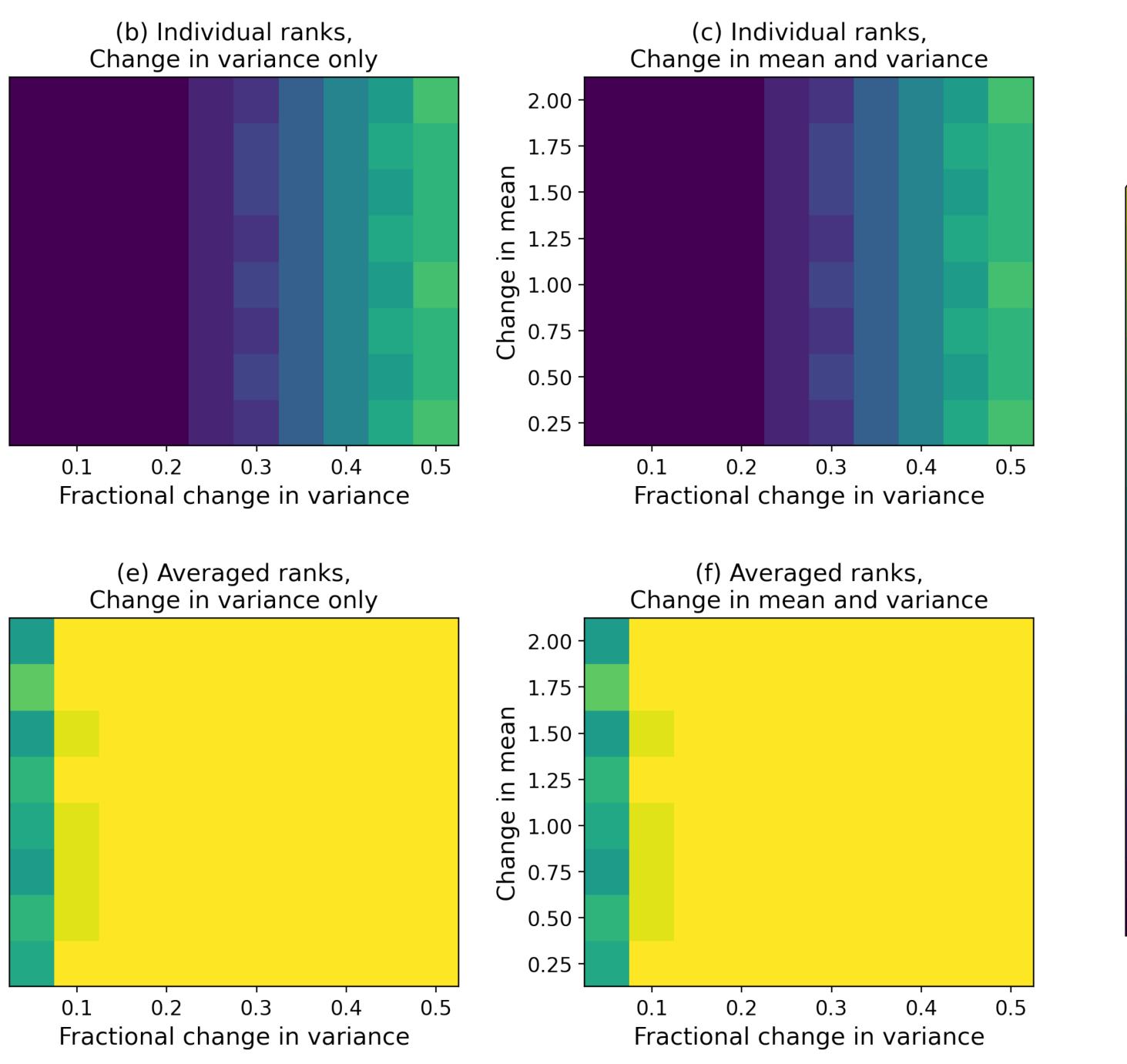


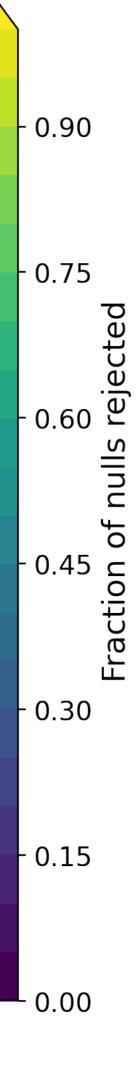


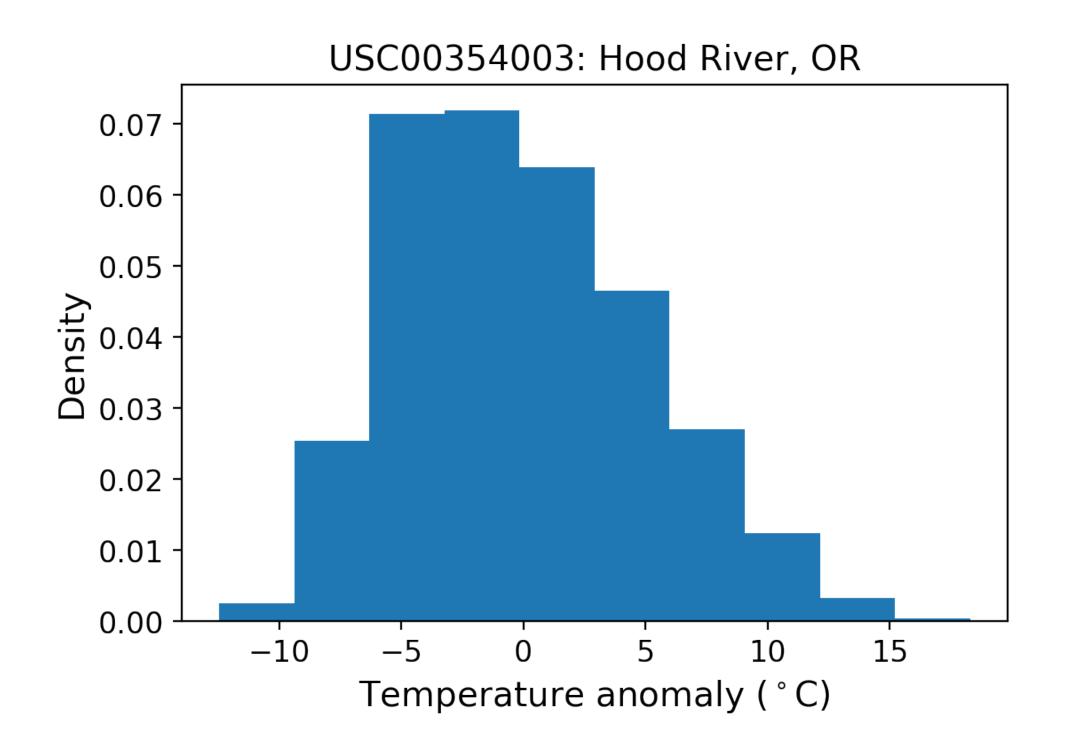


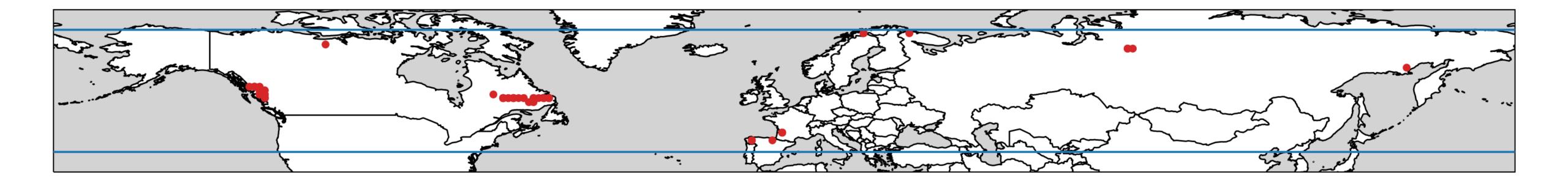


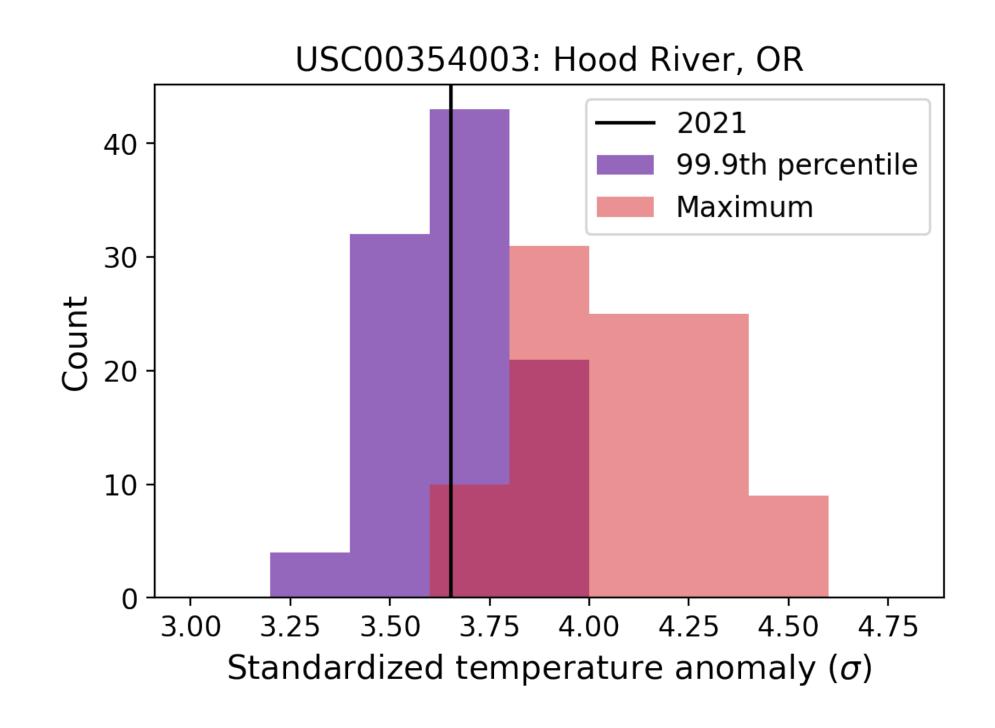




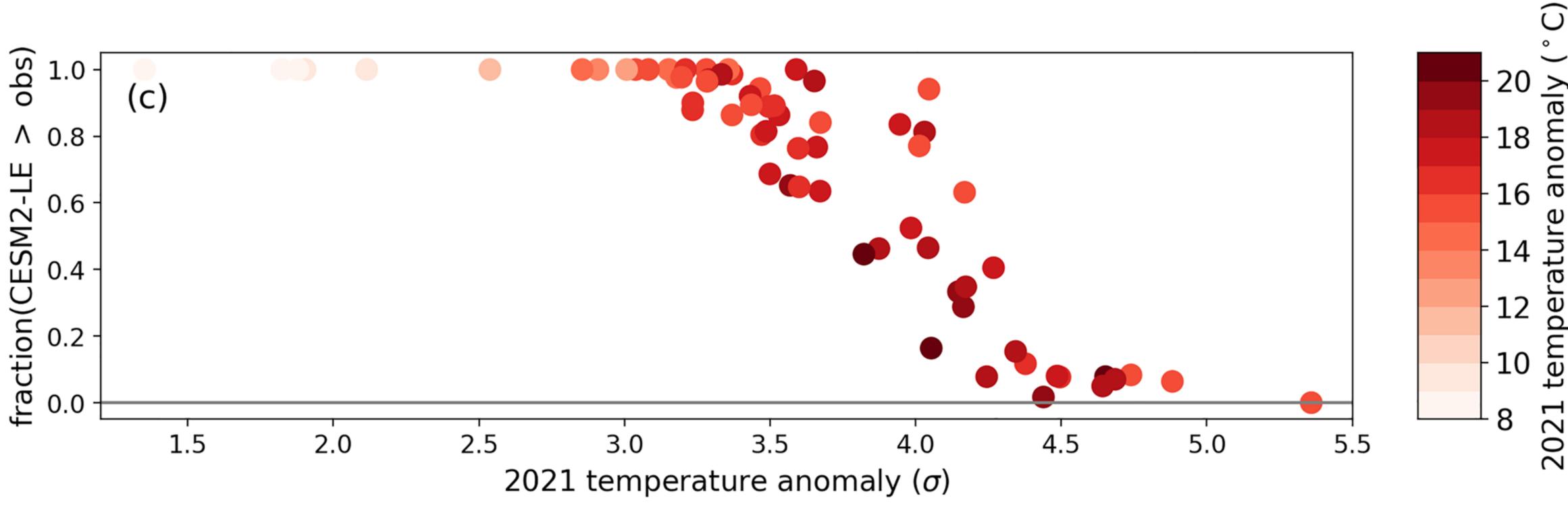




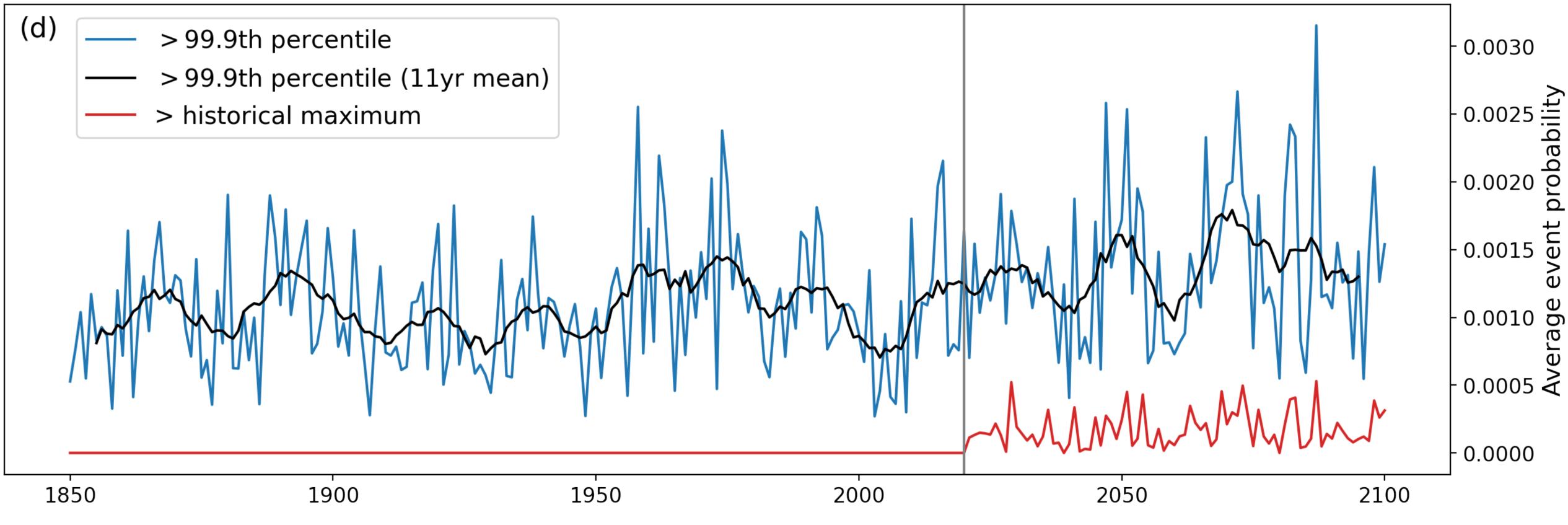




### "Analog locations" (similar skewness and kurtosis) in CESM2 produce heatwaves as large and larger than we saw in 2021



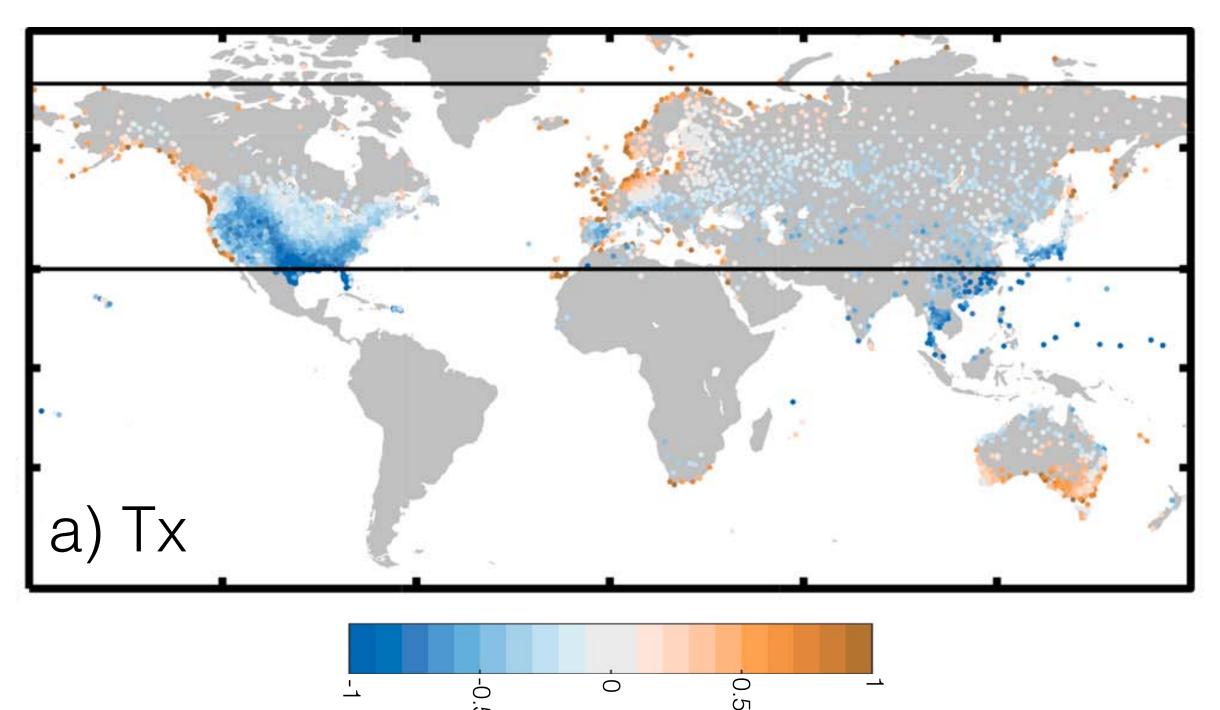
#### But comparable events are rare: the maxima across 171 years x 50 ensemble members



#### Data: CESM2 large ensemble

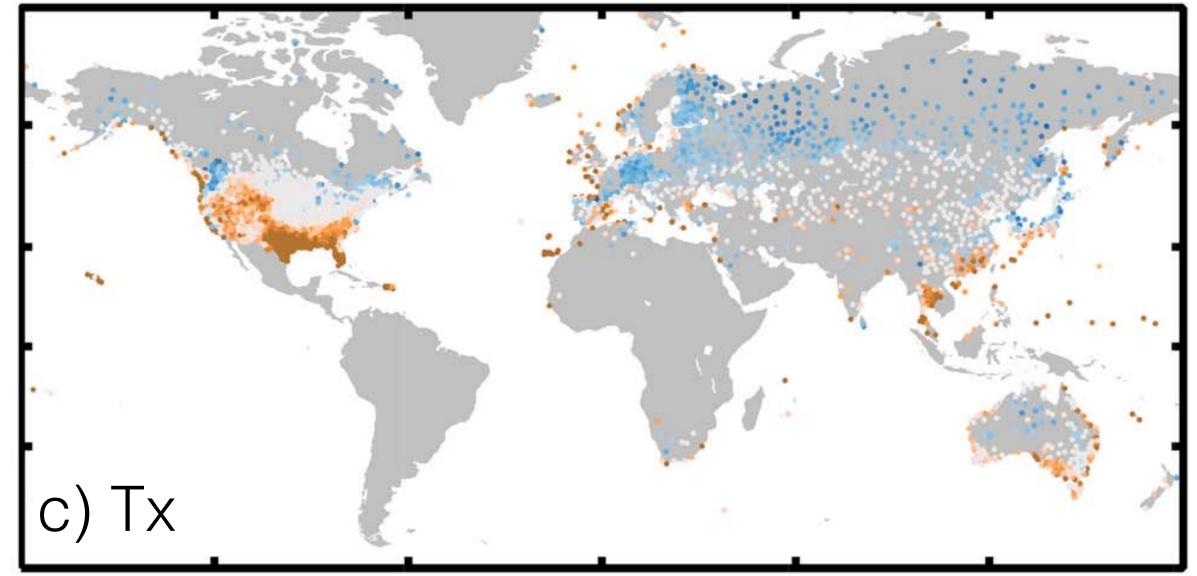
After accounting for warming of the mean, a large climate model ensemble detects significant trends of the most extreme events, although their probabilities remain small

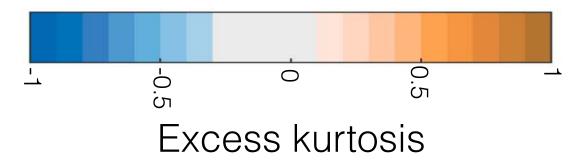
### Daily temperature data is typically non-Gaussian, so insufficient to only assess changes in the mean and variance



Skewness

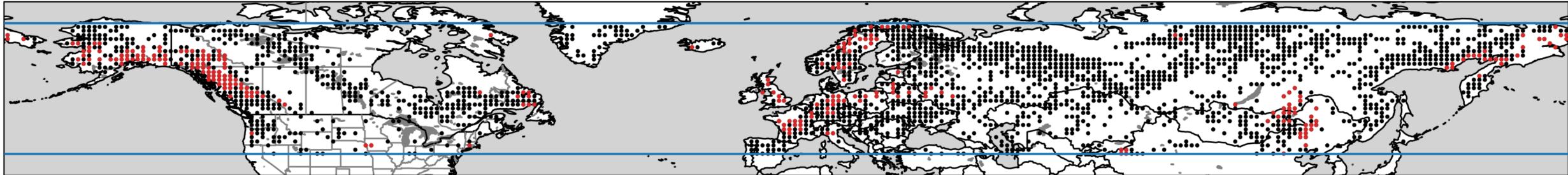
Data: GHCND (weather) stations





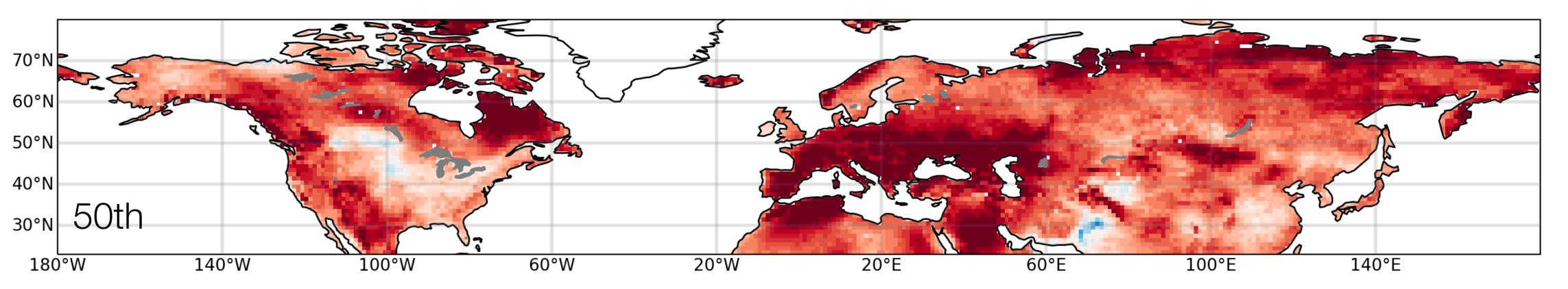


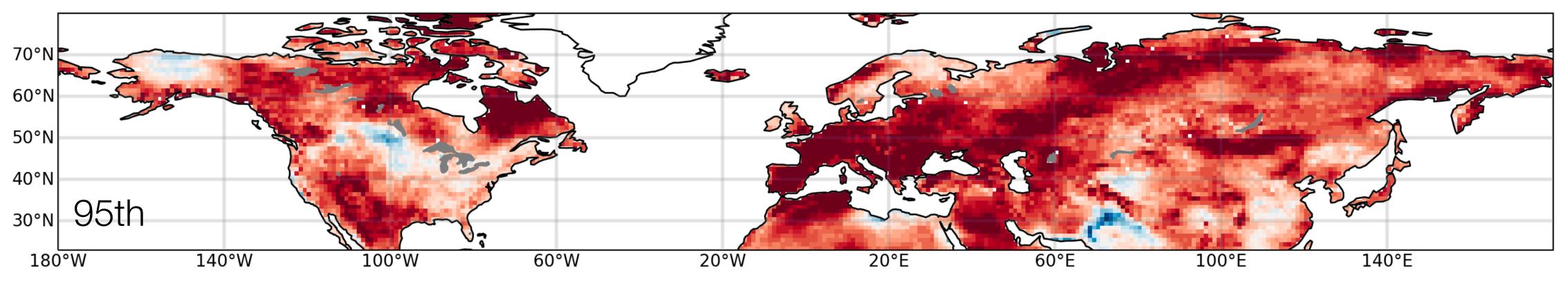
#### Black: all analog locations Red: both observations and CESM2 had greater than 4 sigma event

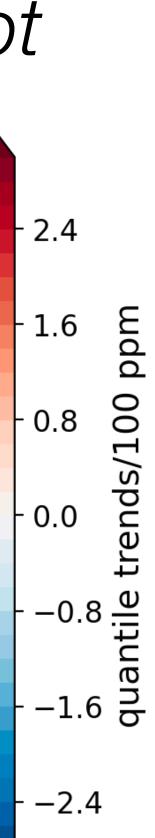




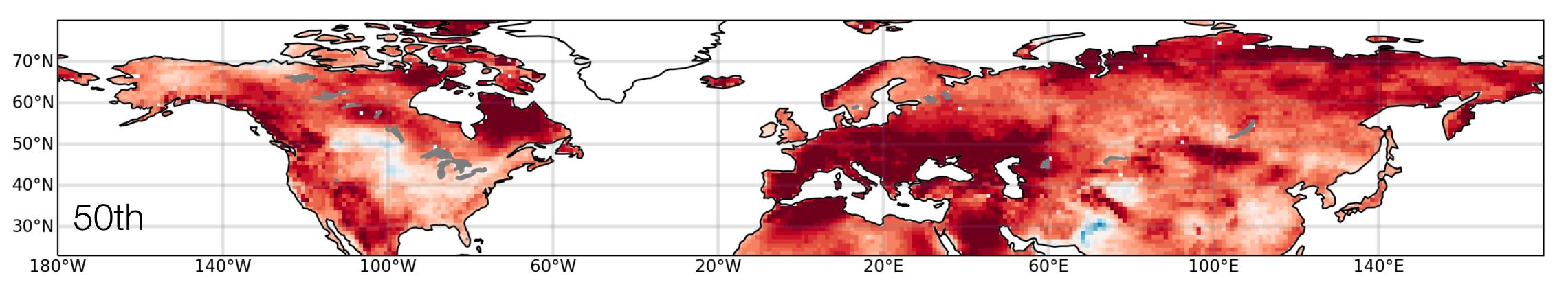
#### Hot days largely follow the median; some places have warmed a lot

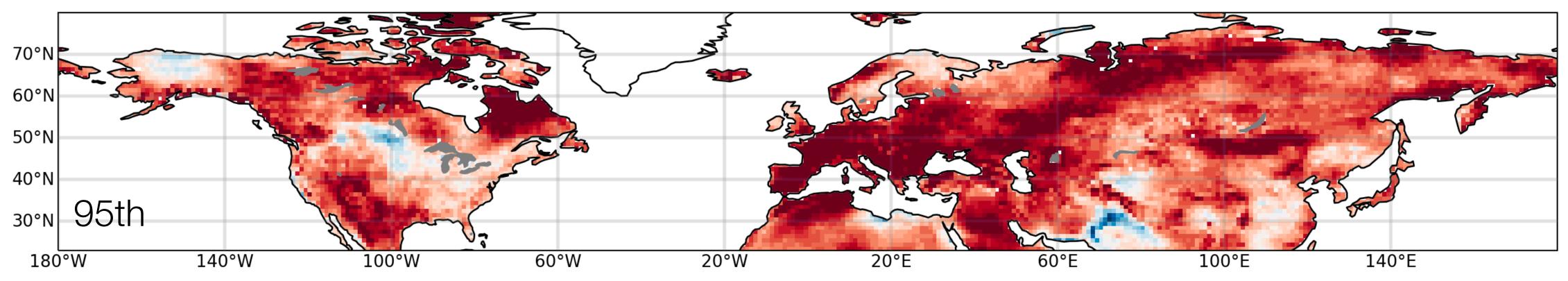


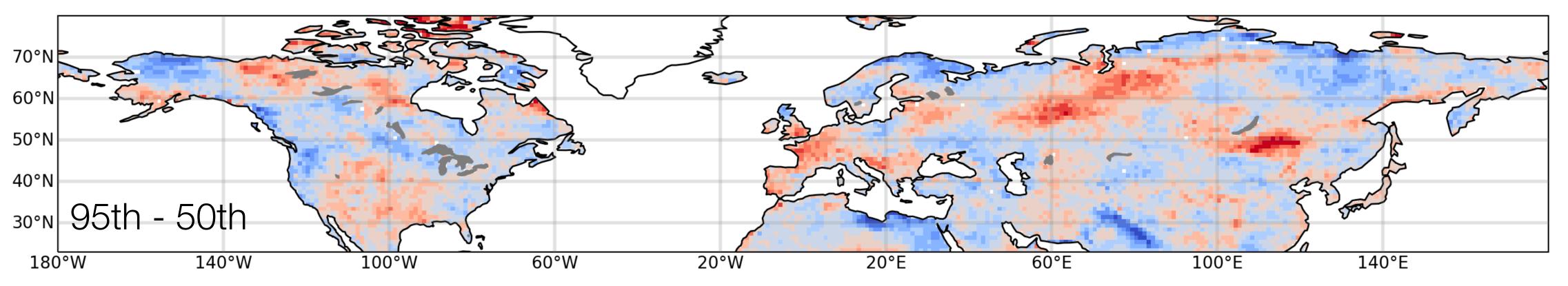


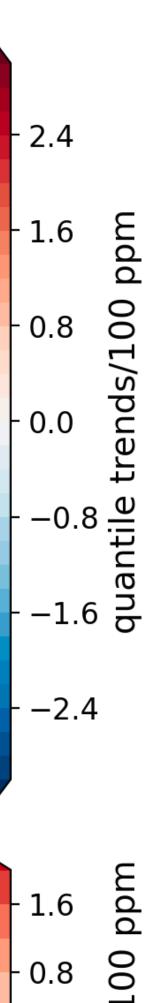


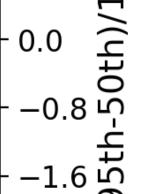
#### Relatively small differences between percentiles, limited significance





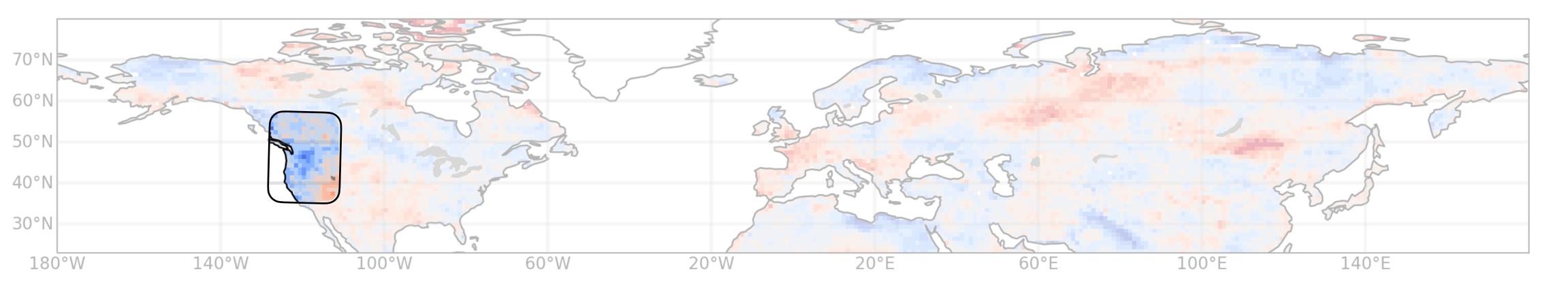




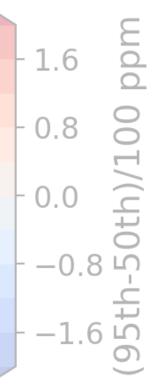




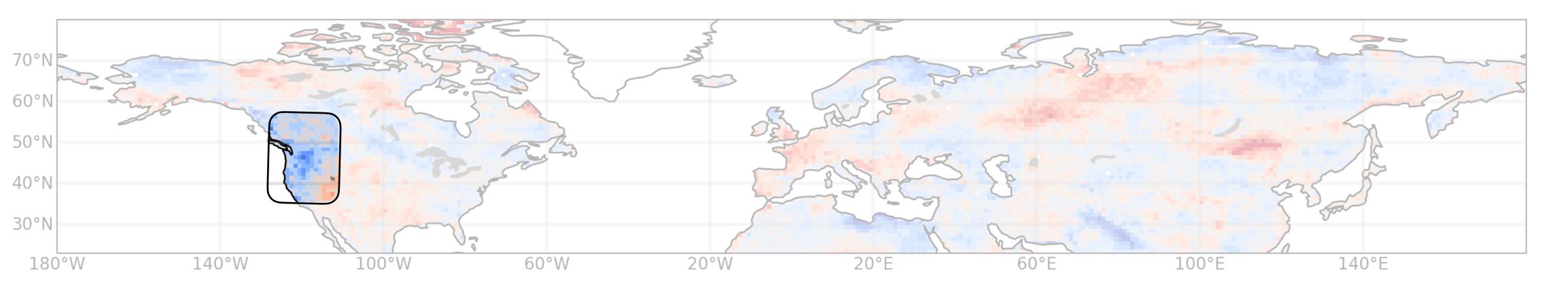
#### Qualitatively similar results with the 1959-2023 ERA5 analysis



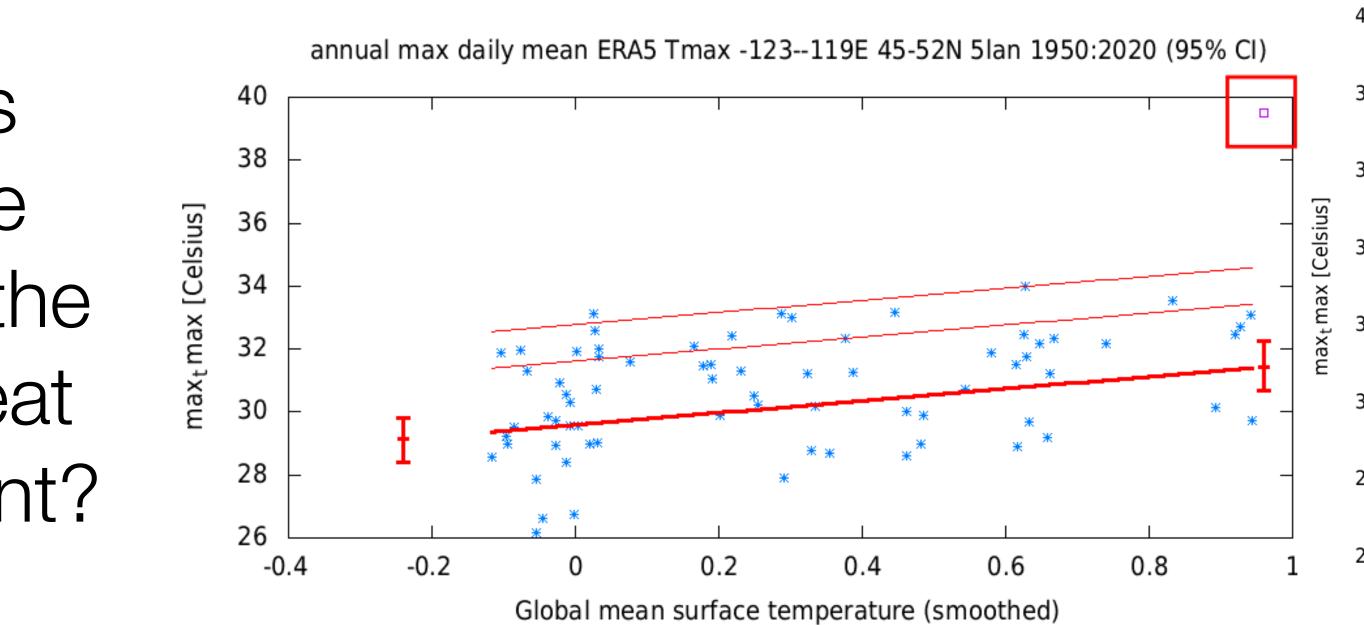
Assuming climate change has mostly shifted the temperature distribution, do we expect that the climate system can produce heat waves as large as the 2021 event?



#### Qualitatively similar results with the 1959-2023 ERA5 analysis



Assuming climate change has mostly shifted the temperature distribution, do we expect that the climate system can produce heat waves as large as the 2021 event?



Philip et al (2022) ESD

