

Optimal **Atmospheric** Excitation of AMOC  
as Estimated via Application of the FDT

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# (Simplified, Quasi-gaussian) Fluctuation Dissipation Theorem (Leith, 1975; Deker&Haake, 1975; Risken, 1984)

Suppose have a discretized dynamical system with noise and a F-P eqn with unique solutions. Also assume gradients of the system PDF are well approximated by a Gaussian fit. Then the PDF-averaged response to weak forcing  $f$  is

$$r(t) = \int_{t_0}^t C(t - \tau) C^{-1}(0) f(\tau) d\tau$$

for  $C(\tau) = \text{lag-}\tau$  cov matrix

Sufficient data to find  $C$

Atmospheric applications:

- \* Gritsun, Branstator (2007)
- \* Gritsun, Branstator, Majda (2008)
- \* Liu et al. (2012)

CCSM4

*T31, 3deg 8000 year control*

$$\begin{bmatrix} T(t) \\ S(t) \\ u(t) \\ v(t) \end{bmatrix} = r(t) = \mathbf{M}_t \bar{f} = \mathbf{M}_t \begin{bmatrix} \dot{T} \\ \dot{S} \\ \dot{u} \\ \dot{v} \end{bmatrix}$$

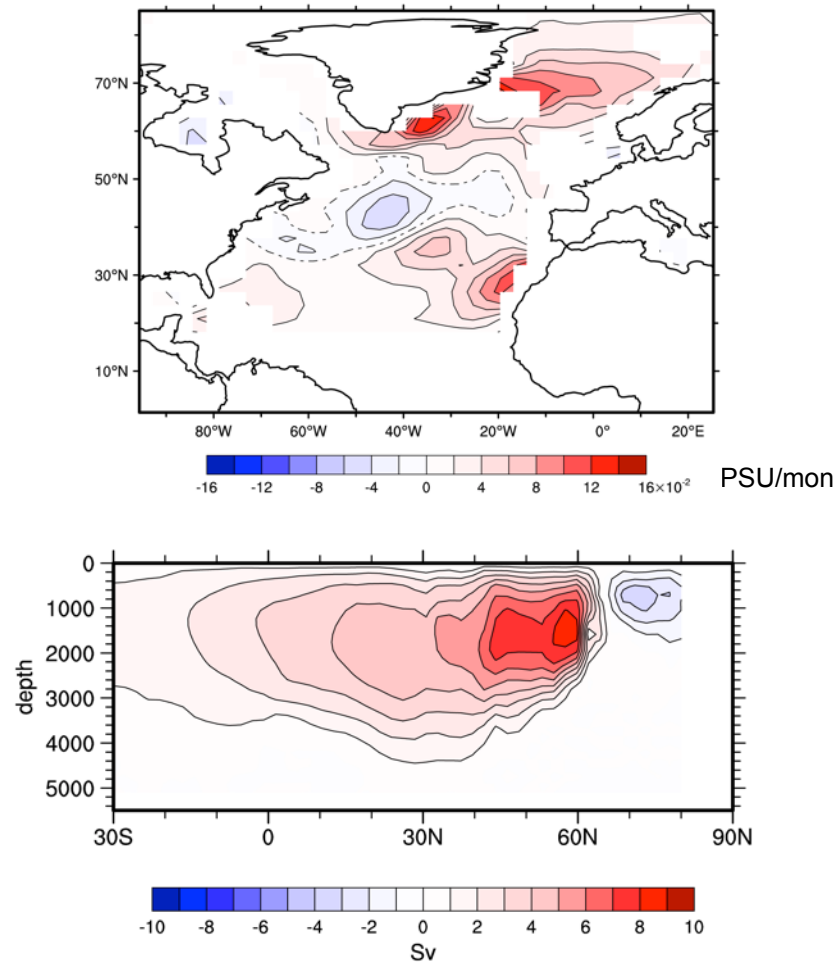
*state of multivariate 3D fields  
is represented by 675 EOFs*

# Optimal N Atlantic Salinity Forcing of AMOC

5 year forcing; year 5 response

force 0-100m

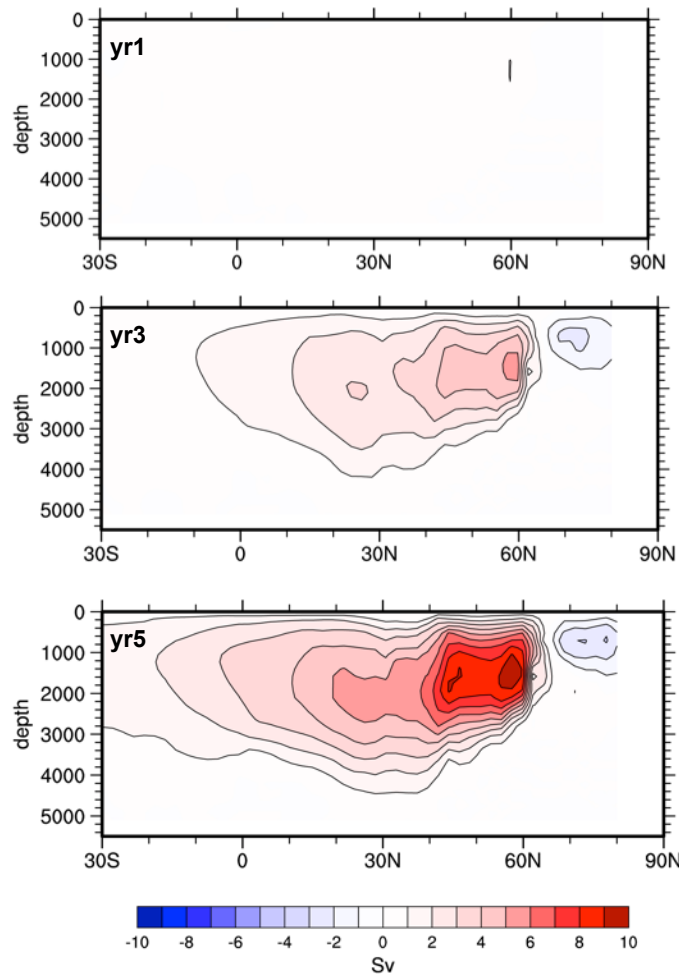
SV1 35x



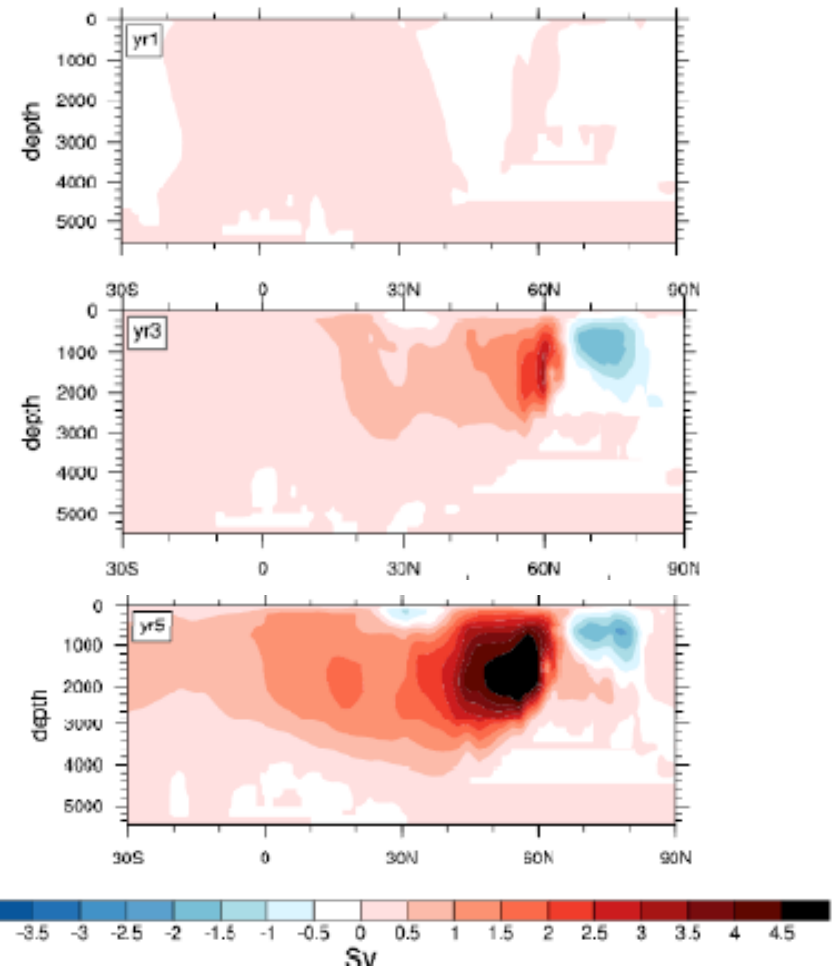
# Optimal & CCSM4 Response of AMOC to Salinity Forcing

force 0-100m

FDT response  
SV1



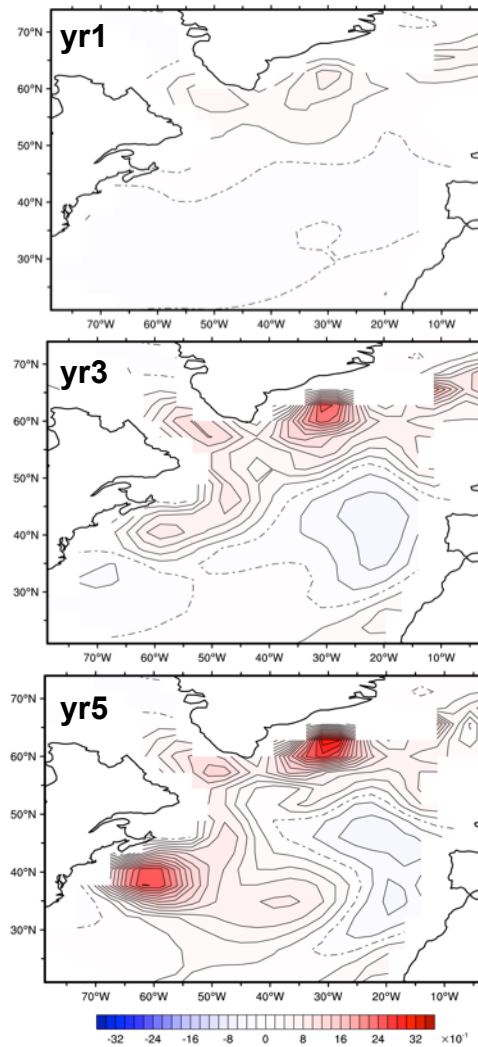
difference of two  
20 member CCSM4 ensembles



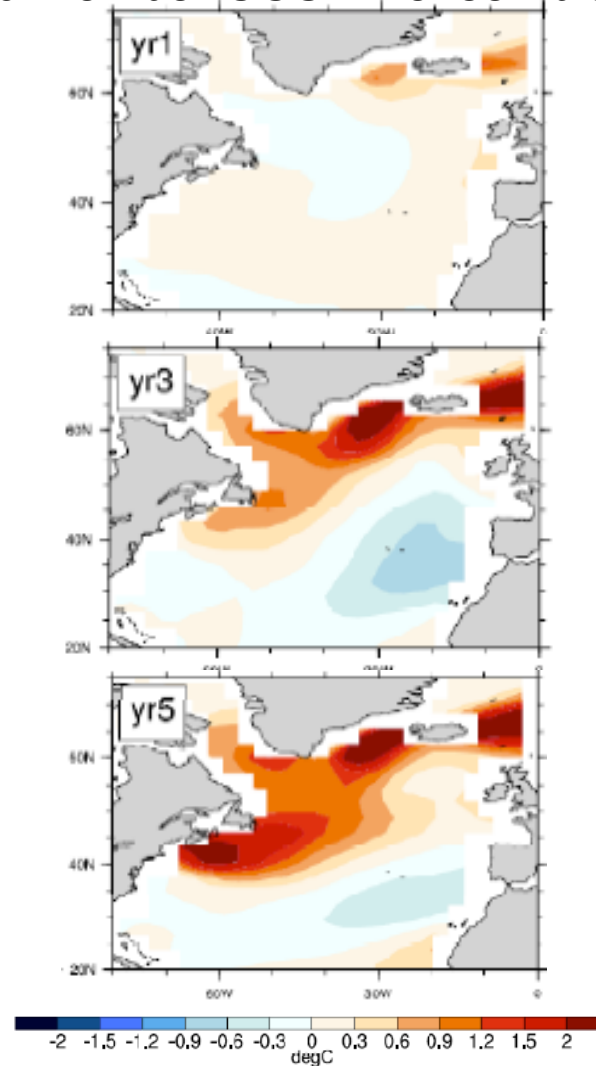
# FDT & CCSM4 SST Response to Optimal Salinity Forcing of AMOC

force 0-100m

FDT response



difference of two  
20 member CCSM4 ensembles



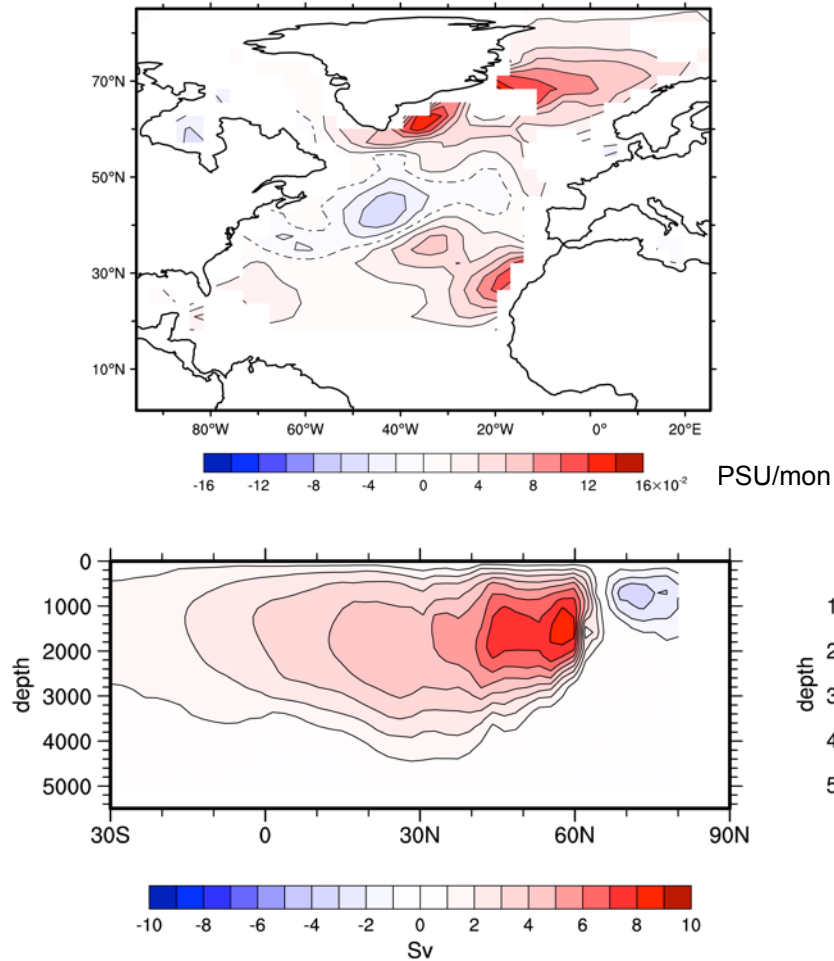
## Remember

- FDT can be used to systematically study ocean response
- The leading patterns of AMOC variability do not depend on the existence of special atmospheric structures
- The effect of a given atmospheric pattern on AMOC depends sensitively on details of its structure and of ocean dynamics

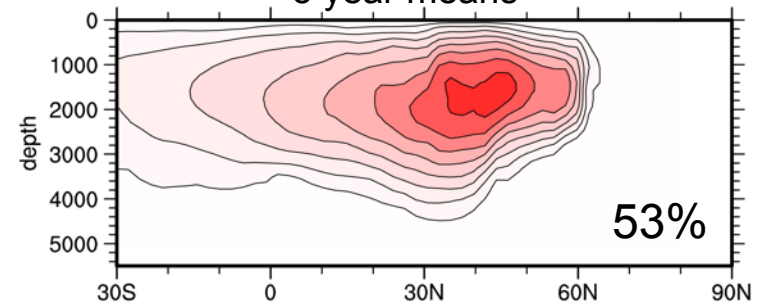
# Optimal Salinity Forcing of AMOC

5 year forcing; year 5 response  
force 0-100m

SV1 35x 62%



CCSM4 EOF1  
5 year means



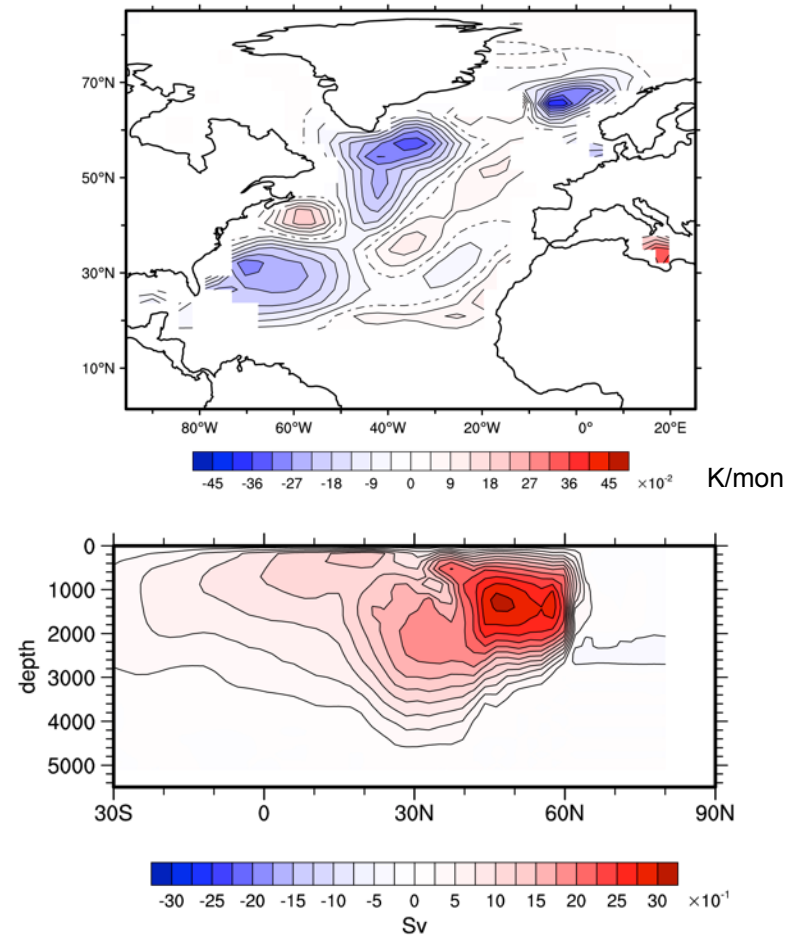


# Optimal North Atlantic Temperature Forcing of AMOC

5 year forcing; year 5 response

force 0-100m

SV1 34x

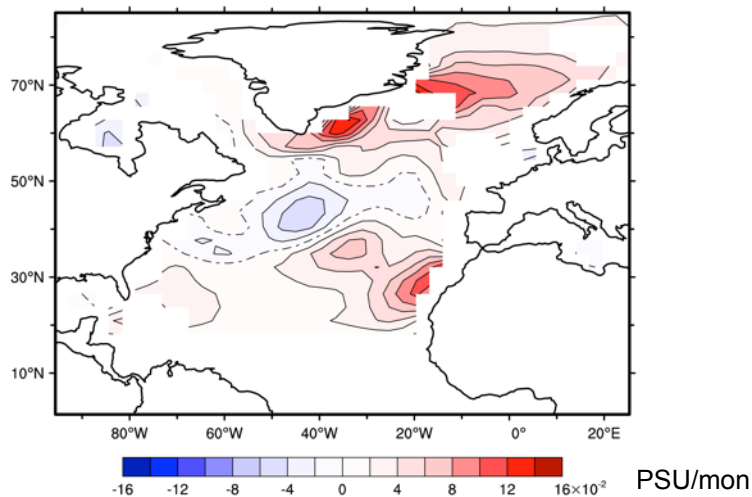


# Optimal Salinity & Temperature Forcing of AMOC

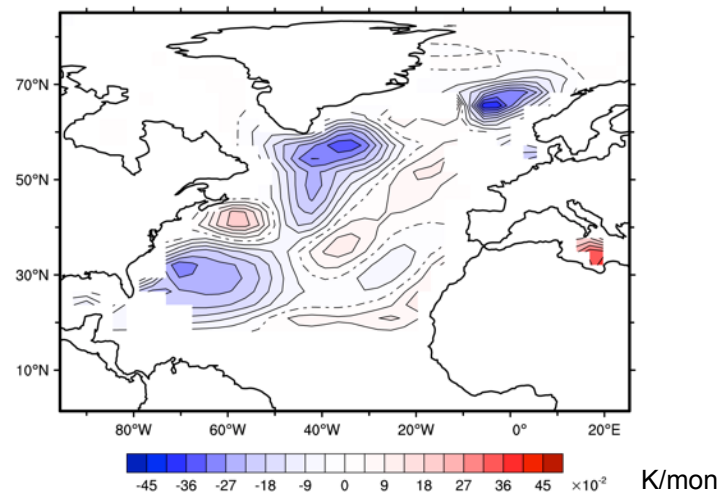
5 year forcing; year 5 response

force 0-100m

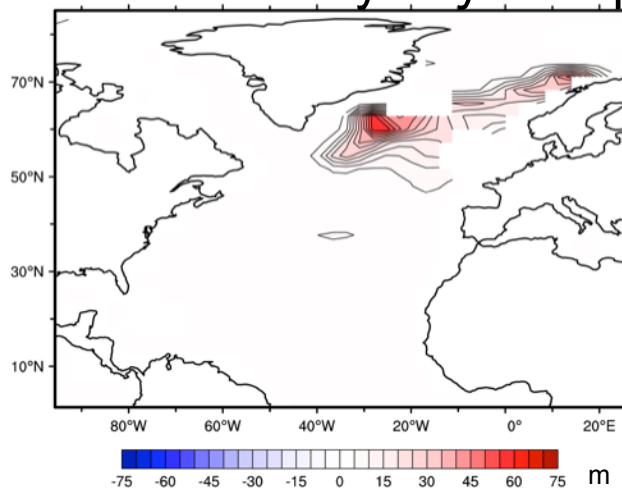
SV1 35x



SV1 34x



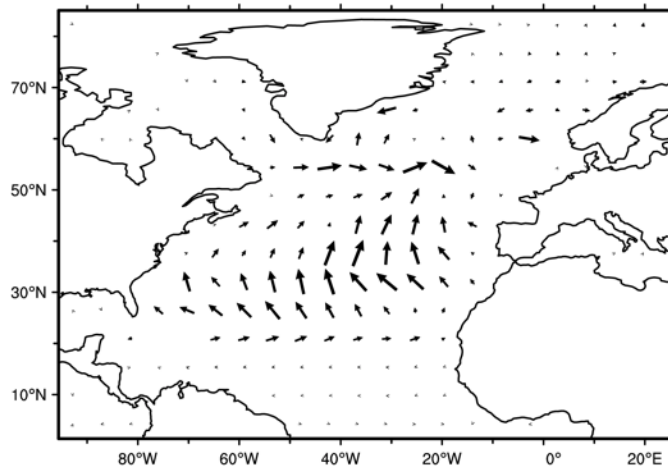
Std Dev Boundary Layer Depth



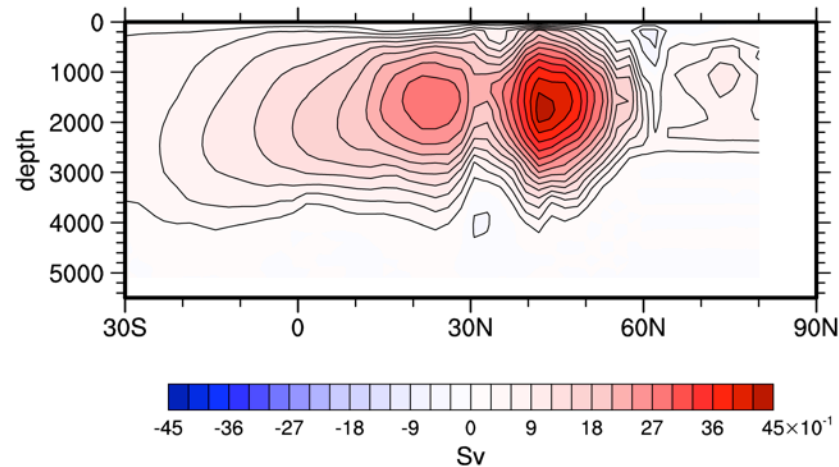
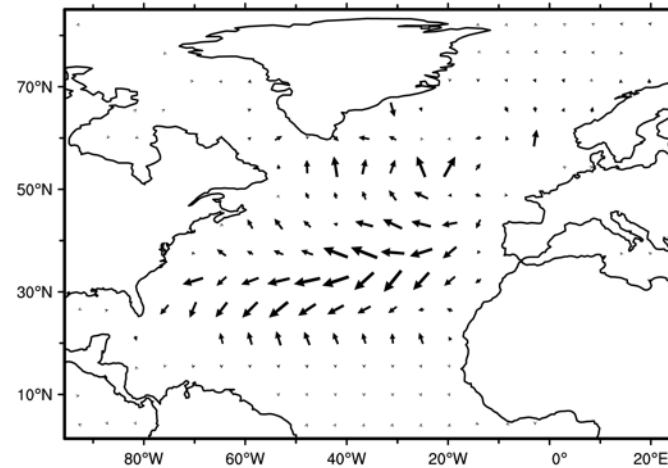
# Optimal Excitation of AMOC by Currents in the North Atlantic

SV1 35x

forcing of 0-100m currents



wind stress



## Remember

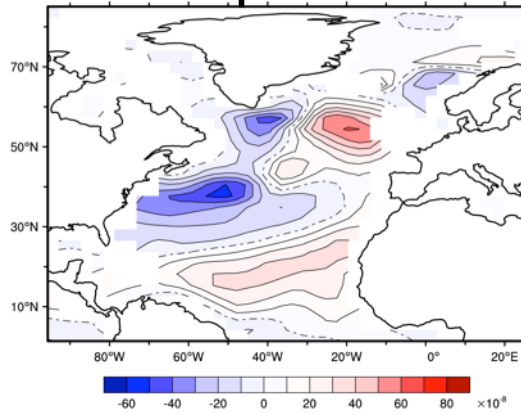
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# Comparing NAO Fluxes & Optimal Forcing

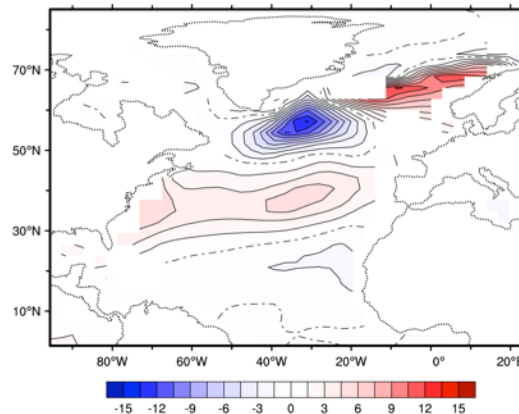
5 year forcing; year 5 response

NAO

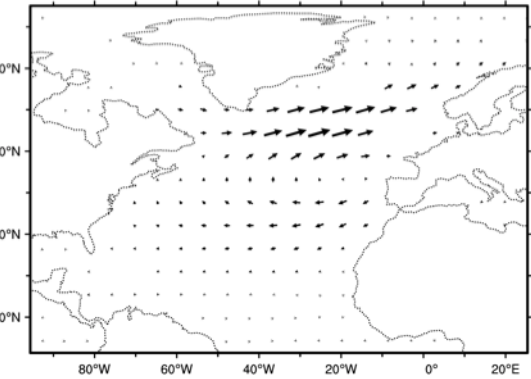
Evaporation



Surface heat flux

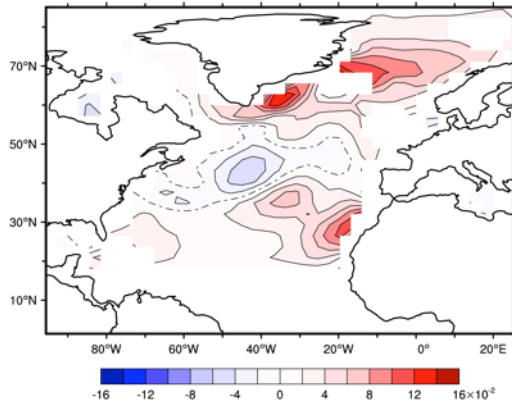


Wind stress

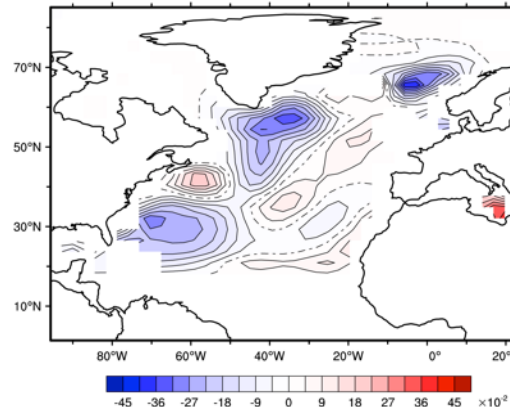


Optimal forcing  
force 0-100m

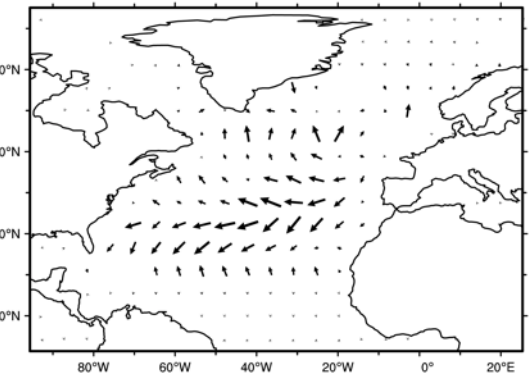
Salinity



Temperature



Wind stress



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